

MATHEMATICS OF FINANCE

Methods of Interest Calculations

Simple Interest



Interest paid each year is same
Interest is charged on principal value

$$SI = P \times R \times T$$

$$A = P + SI$$

$$A = P(1 + RT)$$

Calculator tricks:-

$$(x)^n = ? \quad (2)^5$$

$$2 \times = = = 32$$

$$[x] \text{ (time)} [=] \text{ (n-1) times}$$

$$\text{Rate of interest} = \frac{\text{Int. of 1\%}}{\text{Principal}}$$

For Accrue principle in SI

$$T = \frac{1}{R}$$

$$R = \frac{1}{T}$$

Compound Interest



Interest on each year is not same
Interest is charged on principal and interest on interest is also calculated

$$CI = P[1 + R]^T$$

$$A = P + CI$$

SI = Simple Interest

CI = Compound Interest

R = Rate of interest

T = time

P = Principal

Get triple principal in SI

$t = \frac{2}{r}$	$r = \frac{2}{t}$
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Get four times of principal in SI

$t = \frac{3}{r}$	$r = \frac{3}{t}$
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$$A = P \left[1 + \frac{r}{m} \right]^{t \times m}$$

- (12m) Annually $m=1$
- (6m) Semiannually $m=2$
- (3m) Quarterly $m=4$
- (1mon) monthly $m=12$

Calculate Tricks:

- $(x^5) \Rightarrow x \times \dots \times =$
- $(5^5) \Rightarrow 5 \times \dots \times = 3125$
- $x^{-1} \Rightarrow x \div =$
- $x^{-n} \Rightarrow x \times (n-1) \text{ times } \div 1 \div =$
- $2^{-1} \Rightarrow 2 \div =$
- $2^{-5} \Rightarrow 2 \times \dots \times \div 1 \div = 0.03125$
- $(1.03)^{10 \times 4} \Rightarrow 1.03 \times = (4 \text{ times}) \times = (3 \text{ times})$
- $(x)^{1n} \Rightarrow \sqrt[n]{12 \text{ times} - 1 \div (n) + 1} [x =] 12 \text{ times}$
- $(20)^{13} \Rightarrow 20 \sqrt[12 \text{ times} - 1 \div 3 + 1] [x =] 12 \text{ times} [2.7150]$
- $(30)^{27} \Rightarrow 30 \sqrt[12 \text{ times} - 1 \times 2.7 + 1] [x =] 12 \text{ times} [969.76]$
- $(x)^{12} \Rightarrow \sqrt[x]{(x)^{12}} \Rightarrow \sqrt{\sqrt{x}} / (x)^{12} \Rightarrow \sqrt{\sqrt{\sqrt{x}}}$
- log of any number
- $\rightarrow \sqrt[19 \text{ times} - 1 \times 227695]$
- $\log(30) = 30 \sqrt[19 \text{ times} - 1 \times 227695] = 1.4771$
- $\sqrt[13 \text{ times} - 1 \times 3558]$

7 yrs + 0.87 yrs $0.87 \times 12 = 10.44$ months years $\rightarrow$ months	$0.44 \times 30 = 13.2$ days
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For 2 years

$$CI - SI = Px^2$$

$$\text{Value of asset} = \text{cost} [1 - x\%]^t$$

(Scrap value)

For 3 years

$$CI - SI = Px^2 (x+3)$$

Population

$$A = P(1+x)^t$$

Effective Rate

Ye or E

↓

Annually Rate

$$Ye = \left(1 + \frac{x}{m}\right)^m - 1$$

Nominal rate (x)

↓

monthly / quarterly /
semi annually / daily

CI → P

$$CI = P(1+x)^n - 1$$

$$A = P \left(1 + \frac{x}{m}\right)^{tm}$$

$$PV = \frac{FV}{\left(1 + \frac{x}{m}\right)^{tm}}$$

$$FV = PV \left(1 + \frac{x}{m}\right)^{tm}$$

Types of Annuity

↓

Ordinary Annuity

(Regular)

end of the period

Immediate Annuity

(Annuity due)

Beginning of the period

$$FV = R \left[\frac{(1+i)^n - 1}{i} \right]$$

$$i = \frac{x}{m}, n = t \times m$$

$$FV = R \left[\frac{(1+i)^n - 1}{i} \right] (1+i)$$

$$i = \frac{x}{m}, n = t \times m$$

$PV = R \left[\frac{1 - (1+i)^{-n}}{i} \right]$	$PV = R \left[\frac{1 - (1+i)^{-n}}{i} \right]$
Regular Annuity	Immediate Annuity

Price:-

1.06 ÷ = = = then less

GIT X 100000 [267301]

PV = Investment

PV = 10000

Cost of Asset > PV of all rent

lessor's favourable
(cost of the asset)

Cost of Asset < PV of all rent

favourable for owner of
the asset (lessor)

$$NPV = PV \text{ of all inflow} - PV \text{ of outflow}$$

$$\text{Value of Bond} = \left[\begin{array}{c} PV \text{ of all} \\ \text{interest} \\ \text{(annuity)} \end{array} \right] + \left[\begin{array}{c} PV \text{ of maturity} \\ \text{amount} \end{array} \right]$$

Leasability

Regular

$$PV = \frac{R}{i}$$

Immediate

$$PV = \frac{R}{i} (1+i)$$

growing perpetuity

$$PV = \frac{R}{i+g}$$

$g = \text{growth}$

GAGR

$$x = \left(\frac{A}{P} \right)^{1/x} - 1$$

$$\left(\frac{\text{current } y}{\text{base } y} \right)^{-1/\text{time}} - 1$$

= Rate

$$\text{Real Rate} = \text{Nominal Rate} - \text{Inflation}$$

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"If you don't sacrifice what you want,
what you want becomes the sacrifice."