ALL FORMULAS CA FOUNDATION STATICS

(100 formulas)

Use this PDF with Formula Revision Marathon

Marathon Link: https://youtu.be/cZJHcOf6OUs

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> Class Limits (CL): CL is the minimum and maximum value the class interval may contain

$$CL = UCL - LCL$$

UCL: Upper Class Limit

LCL: Lower Class Limit

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Class Boundary (CB): These are actual class limits of a class interval

> In case of Mutually Exclusive Classification

Class Boundary = Class Limit

> In case of Mutually Inclusive Classification

$$UCB = UCL + 0.5$$
$$LCB = LCL - 0.5$$

Mid Point of Class Interval: average of LCL and UCL or average of LCB and UCB

Mid point is also called as Mid Value of a class or Class Mark

Class Length / Width of Class / Size of Class

UCB - LCB

Frequency Density

Frequency of a class

Class length of that class

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Relative Frequency

Frequency of class

Total Frequency of distribution

Percentage Frequency

Frequency of class
Total Frequency of distribution ×100



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Arithmetic Mean of Discrete Distribution:

$$\overline{x} = \frac{x_1 + x_2 + x_3 + \dots + x_n}{n}$$

$$\overline{x} = \frac{\sum x}{n}$$

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Arithmetic Mean in case of Frequency Distribution :

$$\overline{x} = \frac{\sum fx}{N}$$

Here,

x will be equal to mid point of class interval when frequency distribution is grouped.

N is number of observations which is also equal to total of all frequencies.

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AM using Assumed Mean / Step Deviation Method

$$\overline{x} = A + \frac{\sum fd}{N} \times C$$

where
$$d = \frac{x - A}{C}$$

A = assumed mean, C = class length



Property of AM

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the algebraic sum of deviations of a set of observations from their AM is zero

$$\sum (x - \overline{x}) = 0$$

Property of AM

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Combined AM

- If there are two groups containing $n_1 \& n_2$ observations with AMs as $\overline{x_1} \& \overline{x_2}$ respectively then the combined AM is given by

$$\overline{x}_{c} = \frac{n_{1}\overline{x}_{1} + n_{2}\overline{x}_{2}}{n_{1} + n_{2}}$$

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Median in case of discrete distribution

- If n = odd, then middle term
- If n = even, average of two middle terms

Same formula will be used for Simple Frequency distribution



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Median in case of Grouped Frequency Distribution

- **Step 1**: Prepare a less than type cumulative frequency distribution.
- Step 2: Calculate N/2 and check between which class boundaries it falls and call it as Median Class.
- Step 4: Find l_1 = LCB of Median Class, N_u as Cum Freq. of Median Class, N_l as Cum. Freq. of Pre Median Class, $C = Class\ length\ of\ Median\ Class$
- Step 3: Apply the below formula

$$Me = l_1 + \left(\frac{\frac{N}{2} - N_l}{N_u - N_l}\right) \times C$$

Property of Median

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For a set of observations, the sum of absolute deviations is minimum, when the deviations are taken from the median.

Quartiles (in case of discrete observations)

Quartiles

$$Q_1 = \left((n+1) \times \frac{1}{4} \right)^{th} term$$

$$Q_2 = \left((n+1) \times \frac{2}{4} \right)^{th} term$$

$$Q_3 = \left((n+1) \times \frac{3}{4} \right)^{th} term$$

Deciles (in case of discrete observations)

Deciles

$$D_1 = \left((n+1) \times \frac{1}{10} \right)^{th} term$$

$$D_2 = \left((n+1) \times \frac{2}{10} \right)^{th} term$$

$$Q_9 = \left((n+1) \times \frac{9}{10} \right)^{th} term$$

Percentiles (in case of discrete observations)

Percentiles

$$P_1 = \left((n+1) \times \frac{1}{100} \right)^{th} term$$

$$P_2 = \left((n+1) \times \frac{2}{100} \right)^{th} term$$

$$P_{99} = \left((n+1) \times \frac{99}{100} \right)^{th} term$$

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Quartiles (Grouped FD)

- For first Quartile Q_1
 - \rightarrow Find Q_1 class
 - > Use Formula:

$$Q_1 = l_1 + \left(\frac{\frac{N}{4} - N_l}{N_u - N_l}\right) \times C$$

- For third Quartile Q_3
 - \rightarrow Find Q_3 class
 - > Use Formula :

$$Q_3 = l_1 + \left(\frac{3N}{4} - N_l \over N_u - N_l\right) \times C$$

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> Deciles (Grouped FD)

- For first Decile D₁
 - \rightarrow Find D_1 class
 - > Use Formula:

$$D_1 = l_1 + \left(\frac{\frac{N}{10} - N_l}{N_u - N_l}\right) \times C$$

- For ninth Decile D₉
 - > Find D₉ class
 - > Use Formula:

$$D_9 = l_1 + \left(\frac{\frac{9N}{10} - N_l}{N_u - N_l}\right) \times C$$

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> Percentiles (Grouped FD)

- For first Percentile P₁
 - \rightarrow Find P_1 class
 - > Use Formula:

$$P_1 = l_1 + \left(\frac{\frac{N}{100} - N_l}{N_u - N_l}\right) \times C$$

- For 99th Percentile P₉₉
 - > Find P₉₉ class
 - > Use Formula:

$$P_{99} = l_1 + \left(\frac{\frac{99N}{10} - N_l}{N_u - N_l}\right) \times C$$

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Mode in case of discrete observation

Observation repeating for maximum no. of times/ max frequency

- > When all observations have same frequency : No Mode
- > When two observations have max frequency: Bimodal Observation
- > In general, if we have two or more modes: Multi Modal Observation

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- > Mode in case of grouped frequency distribution
 - First find modal class i.e. class with highest frequency
 - Now, Find
 - \rightarrow $f_0 = frequency of the modal class,$
 - $f_{-1} = frequency of pre modal class,$
 - $f_1 = frequency of the post modal class$
 - Apply formula

$$Mo = l_1 + \left(\frac{f_0 - f_{-1}}{2f_0 - f_{-1} - f_1}\right) \times C$$

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Relationship between Mean, Median and Mode

In case of symmetrical Distribution

Mean = Median = Mode

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Relationship between Mean, Median and Mode

In case of moderately skewed distribution

Mean - Mode = 3 (Median - Median)

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Geometric Mean (in case of discrete positive observations)

$$G = (x_1 \times x_2 \times ... \times x_n)^{1/n}$$

Geometric Mean (in case of frequency distribution)

$$G = (x_1^{f_1} \times x_2^{f_2} \times x_3^{f_3} \times \dots \times x_n^{f_n})^{1/N}$$

Harmonic Mean (in case of discrete observations)

$$H = \frac{n}{\Sigma(1/\chi)}$$

Harmonic Mean (in case of frequency distribution)

$$H = \frac{N}{\Sigma(f/\chi)}$$

Combined HM

$$\bar{x}_c = \frac{n_1 + n_2}{\frac{n_1}{H_1} + \frac{n_2}{H_2}}$$

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> Relationship between AM, GM and HM

When to use	Relationship
When all the observations are same	AM = GM = HM
When all the observations are distinct	AM > GM > HM
In General	$AM \ge GM \ge HM$



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Range (in case of Discrete Observations)

L - S

L = Largest Observation

S = Smallest Observation



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Range (in case of Grouped FD)

L - S

L = UCB of last class interval

S = *LCB* of first class interval

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Coefficient of Range

$$\frac{L-S}{L+S} \times 100$$

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Mean Deviation (in case of discrete observations)

$$MD_A = \frac{1}{n}\Sigma|x - A|$$

Here A is mean or median or mode as given in question

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Mean Deviation (in case of grouped frequency distributions)

$$MD_A = \frac{1}{N} \Sigma f |x - A|$$

Here A is mean or median or mode as given in question

Coefficient of Mean Deviation

Mean Deviation about A × 100

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Standard Deviation (in case of discrete observations)

$$\sigma_{x} = SD_{x} = \sqrt{\frac{\sum (x - \overline{x})^{2}}{n}}$$

$$\sigma_{x} = SD_{x} = \sqrt{\frac{\sum x^{2}}{n} - (\overline{x})^{2}}$$

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Standard Deviation (in case of grouped frequency observations)

$$\sigma_{x} = SD_{x} = \sqrt{\frac{\sum f(x - \overline{x})^{2}}{N}}$$

$$\sigma_{x} = SD_{x} = \sqrt{\frac{\sum fx^{2}}{N} - (\overline{x})^{2}}$$

Coefficient of Variation

$$\frac{SD_x}{\overline{x}} \times 100$$

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For any two numbers, SD = half of range

$$SD = \frac{|a-b|}{2}$$

> Standard Deviation of first n natural numbers

$$s = \sqrt{\frac{n^2 - 1}{12}}$$

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Combined SD

$$SD_{c} = \sqrt{\frac{n_{1}s_{1}^{2} + n_{2}s_{2}^{2} + n_{1}d_{1}^{2} + n_{2}d_{2}^{2}}{n_{1} + n_{2}}}$$

$$d_1 = \overline{x}_c - \overline{x}_1$$

$$d_2 = \overline{x}_c - \overline{x}_2$$

Property of SD

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If all the observations are constant, SD is Zero

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Property of SD

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No effect of change of origin but affected by change of scale in the magnitude (ignore sign)

Quartile Deviation

$$QD_x = \frac{Q_3 - Q_1}{2}$$

Coefficient of Quartile Deviation

$$\frac{Q_3 - Q_1}{Q_3 + Q_1} \times 100$$

Relationship between SD, MD, QD Downloaded From www.castudynotes.com

For a moderately skewed distribution

$$4SD = 5MD = 6QD$$

$$SD:MD:QD=15:12:10$$

Basic formula of Probability

$$P(A) = \frac{(no.of\ favorable\ events\ to\ A)}{Total\ no.of\ events}$$

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Odds in Favor of Event A

no. of favorable events

no. of unfavorable events

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> Odds against an Event

no. of unfavorable events no. of favorable events

> No. of total outcome of a random experiment

If an experiment results in p outcomes and if it is repeated q times then

Total number of outcomes is





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Relative Frequency Probability

Relative Frequency = $\frac{\text{no. of times the event occurred during experimental trials}}{\text{total no. of trials}} = \frac{f_A}{n}$

Probability by this method is defined as

$$P(A) = \lim_{n \to \infty} \frac{f_A}{n}$$



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> Set Based Probability

$$P(A) = \frac{\text{no.of sample points in A}}{\text{no.of sample points in S}} = \frac{n(A)}{n(S)}$$



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Addition Theorem 1

In case of two mutually exclusive events A and B

$$P(A \cup B) = P(A+B) = P(A \text{ or } B) = P(A) + P(B)$$

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Addition Theorem 2

In case of two or more mutually exclusive events

$$P(A_1 \cup A_2 \cup A_3 \cup \cdots) = P(A_1) + P(A_2) + P(A_3) + \dots$$

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Addition Theorem 3

For any two events

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

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Addition Theorem 4

In case of any three events

$$P(A \cup B \cup C)$$

$$= P(A) + P(B) + P(C) - P(A \cap B) - P(B \cap C)$$

$$-P(A\cap C) + P(A\cap B\cap C)$$

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Conditional Probability of Event B knowing that Event A is already occurred

$$P\left(\frac{B}{A}\right) = \frac{P(B \cap A)}{P(A)}$$

 $provided P(A) \neq 0$

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Conditional Probability of Event A knowing that Event B is already occurred

$$P\left(\frac{A}{B}\right) = \frac{P(A \cap B)}{P(B)}$$

$$provided P(B) \neq 0$$



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Compound Theorem

In case of two dependent events

$$P(A \cap B) = P(B) \times P(A/B)$$
 or

$$P(A \cap B) = P(A) \times P(B/A)$$



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Compound Theorem

In case of two independent events

$$P(A \cap B) = P(A) \times P(B)$$

Same thing applies for two or more independent events

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Expected value of a Probability Distribution

$$E(x) = \sum p_i x_i$$

$$E(x) = \mu$$



Variance of Probability Distribution

$$V(x) = \sigma^2$$

$$E(x - \mu)^2 = E(x)^2 - \mu^2$$

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Probability Mass Function in case of Binomial Distribution

$$f(x) = P(X = x) = {}^{n}C_{x} p^{x} q^{n-x}$$

Mean and Variance in case of Binomial Distribution

$$\mu = np$$

$$\sigma^2 = npq$$

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Mode in case of Binomial Distribution

Calculate
$$(n+1)p$$

if the resulting value is integer then Bi-modal

If the resulting value is non- $\mu_0 = la$ integer then Uni-modal

$$\mu_0 = (n+1)p \text{ and}$$

$$[(n+1)p-1]$$

$$\mu_0 = \text{largest integer contained in}$$

$$(n+1)p$$



Probability Mass Function in case of Poisson Distribution

$$f(x) = P(X = x) = \frac{(e^{-m}.m^x)}{x!}$$

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Mean, Variance and SD in case of Poisson Distribution

$$\mu = m$$

$$\sigma^2 = m$$

$$\sigma = \sqrt{m}$$

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Mode in case of Poisson Distribution

if the value of m is integer	$\mu_0 = m \ and$
then Bi-modal	[m-1]
If the value of m is non-	$\mu_0 = largest integer$
integer then Uni-modal	contained in m



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Probability Density Function in case of Normal Distribution

$$f(x) = \frac{1}{\sigma\sqrt{2\pi}} \times e^{-(\frac{x-\mu}{\sigma})^2 \times \frac{1}{2}}$$



Mean Deviation in case of Normal Distribution

$$MD = 0.8 \sigma$$

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Quartiles in case of Normal Distribution

$$Q_1 = \mu - 0.675\sigma$$

$$Q_3 = \mu + 0.675\sigma$$



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Quartile Deviation in case of Normal Distribution

$$QD = 0.675\sigma$$

Points of Inflexion

$$\mu - \sigma & \mu + \sigma$$

Ratio between

QD : MD : SD = 10:12:15

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Conditions of Standard Normal Distribution

Mean μ	0	
Standard Deviation o	1	



Z Value

$$Z = \frac{x - \mu}{\sigma}$$

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Area under Normal Curve

From	То	Area/Probability
μ	+σ	34.135%
+σ	+2σ	13.59%
+20	+3σ	2.14%
3σ	∞	0.135%

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For a bivariate frequency distribution

No. of marginal distributions = 2

No. of conditional distributions = m + n

Karl Pearson's Product Moment Correlation Coefficient

$$r_{xy} = \frac{Cov(x, y)}{\sigma_x. \sigma_y}$$

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Covariance

$$Cov(x,y) = \frac{\Sigma(x-\bar{x})(y-\bar{y})}{n} or \frac{\Sigma xy}{n} - \bar{x}.\bar{y}$$

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Spearman's Rank Correlation Coefficient

$$r_R = 1 - \frac{6\Sigma d^2}{n(n^2 - 1)}$$

here d means difference in ranks

Adjustment value in case of Tie

$$\Sigma \frac{(t^3 - t)}{12}$$

Coefficient of Concurrent Deviations

$$r_c = \pm \sqrt{\pm \frac{2c - m}{m}}$$

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Regression Coefficients

$$b_{yx} = r. \frac{\sigma_y}{\sigma_x}$$
 or $b_{yx} = \frac{Cov(x,y)}{\sigma_x^2}$

$$b_{xy} = r \cdot \frac{\sigma_x}{\sigma_y} \text{ or } b_{xy} = \frac{Cov(x,y)}{\sigma_y^2}$$

Regression Property

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$$r = \pm \sqrt{b_{xy} \times b_{yx}}$$

 b_{xy} , b_{yx} and r all will have same sign

π .

Regression Property

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- > Change of Origin and Scale
 - Origin: No Impact
 - Scale: If original pair is x, y and modified pair is u, v

then,

$$b_{vu} = b_{yx} \times \frac{change \ of \ scale \ of \ y}{change \ of \ scale \ of \ x}$$

$$b_{uv} = b_{xy} \times \frac{change\ of\ scale\ of\ x}{change\ of\ scale\ of\ y}$$

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Regression Property

- > Intersection of two regression lines:
 - Two regression lines (if not identical) will intersect at the point [means]

$$(\overline{x}, \overline{y})$$



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Coefficient of determination

Explained Variance
Accounted Variance

 r^2

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Coefficient of non-determination

Unexplained Variance
Unaccounted Variance

 $1 - r^2$

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Probable Error

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$$0.6745 \times \frac{1 - r^2}{\sqrt{N}}$$

- where, r = correlation coefficient, N = no. of pairs of observation

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Limits of Population Correlation Coefficient Downloaded From www.castudynotes.com

Index Relatives

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Price Relative	$Price \ Relative = \frac{P_n}{P_0}$
Quantity Relative	Quantity Relative = $\frac{Q_n}{Q_0}$
Value Relative	Value Relative = $\frac{V_n}{V_0} = \frac{P_n Q_n}{P_0 Q_0}$
Link relative	$\frac{P_1}{P_0}, \frac{P_2}{P_1}, \frac{P_3}{P_2}, \dots, \frac{P_n}{P_{n-1}}$ Same can be created for quantities also
Chain relatives	When the above relatives are in respect to a fixed base period these are also called the chain relatives $\frac{P_1}{P_0}, \frac{P_2}{P_0}, \frac{P_3}{P_0}, \dots, \frac{P_n}{P_0}$

Simple Aggregative Method of Index Downloaded From www.castudynotes.com

Price Index is expressed as total of commodity prices in a given year as a percentage of total of commodity prices in the base year

> Formula

$$\frac{\Sigma P_n}{\Sigma P_0} \times 100$$



Simple Average of Relatives – Method of Index Downloaded From www.castudynotes.com

- > Under this method, we invert the actual price for each variable into percentage of the base period. These percentages are called relatives.
- > Formula

$$\frac{\sum \frac{P_n}{P_0}}{N}$$



Weighted Index Methods

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> Laspeyres' Index

$$\frac{\Sigma P_n Q_0}{\Sigma P_0 Q_0} \times 100$$

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> Passche's Index

$$\frac{\Sigma P_n Q_n}{\Sigma P_0 Q_n} \times 100$$

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> Marshall-Edgeworth Index

$$\frac{\Sigma P_n(Q_0 + Q_n)}{\Sigma P_0(Q_0 + Q_n)} \times 100$$



Weighted Index Methods Downloaded From www.castudynotes.com

> Fisher's Index

(GM of Laspeyres' and Paasche's)

$$\sqrt{\frac{\sum P_n Q_0}{\sum P_0 Q_0}} \times \frac{\sum P_n Q_n}{\sum P_0 Q_n} \times 100$$



Deflated Value

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Deflated Value =
$$\frac{\text{Current Value}}{\text{Price Index of the current year}}$$