

$$Q\left[\begin{array}{c}1 + \frac{64}{12} \\ \frac{4.5}{100}\right] \rightarrow Q = 20$$

11. a bike is purchased by making a down payment of Rs 15000 and balance to be paid alongside interest at 5% for 2 yrs . Total amount paid is 28200 . Find the cash price of the bike

Loan amount P borrowed at the time of purchase amounted to repayment of A = 13200 incl. the interest at 5% for 2 years

$$13200 = P \begin{pmatrix} 1 + 2(5) \\ 100 \end{pmatrix} P = 12,000$$

Cash Price of the bike = Down payment of 15000 + P = 27,000

Q2

01. Find rate of interest if the amount owed after 6 months is ₹ 2100 , borrowed amount being ₹ 2000

 $2100 = 2000 \begin{pmatrix} 1 + 6 & r \\ 12 & 100 \end{pmatrix} \rightarrow r = 10\% p.a.$

02. Find rate of interest if the amount owed after 6 months is ₹ 1050 , borrowed amount being ₹ 1000

 $1050 = 1000 \begin{pmatrix} 1 + \underline{6} & \underline{r} \\ 12 & \underline{100} \end{pmatrix} \quad \rightarrow \quad r = 10\% \text{p.a.}$

- 03. 46875 was lent out at SI and at end of 1 yr 8 months, total amount was 50,000. Find rate of interest p.a. 50000 = 46875 $\begin{pmatrix} 1 + \frac{20}{12} & \frac{r}{100} \end{pmatrix} \rightarrow r = 4\%$ p.a.
- 04. If a sum triples in 15 years at simple rate of interest, the rate of interest p.a. will be

$$3P = P\left(\frac{1+15r}{100}\right) r = 13.33\% p.a.$$

Q3

2P

- 01. In how much time would SI on a certain sum be 0.125 times the principal at 10% p.a. $0.125P = P n.\underline{10} \rightarrow n = 1.25 \text{ yrs} = 1 \text{ yr 3 months}$ 100
- 02. Find number of years in which a sum doubles itself at the rate of 8% p.a.

$$= P \begin{pmatrix} 1+n(8) \\ 100 \end{pmatrix} \rightarrow n = 12.5 \text{ yrs}$$

03. In what time will ₹ 85000 amount to ₹ 1,57,675 at 4.5%p.a. SI

 $157675 = 85000 \left(\begin{array}{c} 1 + n \ \underline{4.5} \\ 100 \end{array} \right) \quad \rightarrow \quad n \ = \ 19 \ \text{years} \ .$

04. Rahul invested 70,000 in a bank at the rate of 6.5% p.a. SI . He received 85,925 after the end of term . Find out the period for which sum was invested by Rahul

 $85925 = 70000 \left(\begin{array}{c} 1 + n \ \underline{6.5} \\ 1 \ \underline{100} \end{array} \right) \quad \rightarrow \quad n = 3.5 \ \text{years} \ .$

Q4

01. sum doubles itself in 20 yrs . In how many years it will become 7 times

$$2P = P \begin{pmatrix} 1+20r \\ 100 \end{pmatrix} \rightarrow r = 5\%p.a. \rightarrow 7P = P \begin{pmatrix} 1+n(5) \\ 100 \end{pmatrix} \qquad n = 120yrs$$

02. sum doubles itself in 10 yrs . In how many years it will treble itself

$$2P = P \begin{pmatrix} 1+10r \\ 100 \end{pmatrix} \rightarrow r = 10\% p.a. \rightarrow 3P = P \begin{pmatrix} 1+n(10) \\ 100 \end{pmatrix} \qquad n = 20yrs$$

03. A sum of 3402 amounts to 6804 in 20 years . What sum will amount to 5200 in 6 years at same rate .

 $6804 = 3402 \begin{pmatrix} 1+20r\\100 \end{pmatrix} \rightarrow r = 5\% p.a \rightarrow 5200 = P \begin{pmatrix} 1+6(5)\\100 \end{pmatrix} P = 4000$

04. 8000 become 10000 in 2 yrs at simple interest . The amount that will become 6,875 in 3 yrs at the same rate of interest

 $10000 = 8000 \left(1 + \frac{2r}{100}\right) \rightarrow r = 12.5\% p.a \rightarrow 6875 = P \left(1 + \frac{3(12.5)}{100}\right) P = 5000$

Q5

01. A person lends 6000 for 4 years and 8000 for 3 years at simple interest . If he gets 2400 as total interest the rate of interest is

 $2400 = 6000.4.r + 8000.3.r \longrightarrow 2400 = 240r + 240r \longrightarrow r = 5\%p.a.$

02. Mr X takes a loan of 7000 for 8 yrs . After 3 yrs he takes a loan of 3000 more .Total interest paid at the end of 8 yrs is 3550 . Find the rate of interest

 $3550 = 7000(\underline{8})r + 3000(\underline{5})r \\ 100 100 r = 5\% p.a.$

03. the rate of simple interest on sum of money is 6% p.a. for first 3 years , 8% for the next 5 years and 10% for yrs beyond 8 yrs . If the simple interest accrued by the sum for a period of 10 yrs is 1560 . The sum is

 $1560 = \frac{P3(6)}{100} + \frac{P5(8)}{100} + P(2)\underline{10}$ 156000 = 18P + 40P + 20P $156000 = 78P \qquad P = 2000$

Q6

01. A person borrows 5000 for 2 years at 4% p.a. simple interest . He immediately lends it to another person at 6 ¼% p.a. for 2 years . Find his gain in the transaction per year

Gain = $5000.2.(\underline{6.25}) - 5000.\underline{2.(4)}$ = $5000.\underline{2}.(6.25-4)$ = 225 in 2 years 100 100 100

Gain/year = 112.50

02. Two equal sum was lent at simple interest at 11% p.a. for 3 $\frac{1}{2}$ yrs and 4 $\frac{1}{2}$ yrs respectively . If the difference in interest for two periods was 412.50 , then each sum is

412.50 = P. (4.5)<u>11</u> - P(3.5)<u>11</u>100 100<math display="block">41250 = 11P[4.5-3.5]P = 3750

03. A certain sum of money was invested at simple rate of interest for 3 years . If the same had been invested at the rate that was 7 percent higher , the interest amount would have been Rs 882 more . The amount of sum invested is

882 = P.3 (r+7) - P.3 r = 100 $88200 = 3Pr + 21P - 3Pr \qquad P = 4200$

04. if SI on 1400 for 3 yrs is less than SI on 1800 for same period by Rs 80, then rate of interest

 $80 = 1800.3.r - 1400.3.r \\ 100 100$

80 = 54r - 42r r = 6.67%

05 Mr X invest 90,500 in post office at 7.5% p.a. SI . While calculating the rate was wrongly taken as 5.7% p.a. . The difference in amounts of maturity is 9774 . Find the period for which the sum was invested .

NOTE – Difference in amounts of maturity is basically the difference in SI accrued as the principal remains same through

 $9774 = 90500.n.(\underline{7.5}) - 90500.n.(\underline{5.7})$ 100 100

9774 = 905n [7.5-5.7]

9774 = 1629n n = 6 years

Q7

01. a certain sum amounts to 7400 in 3 yrs and 8600 in 4 yrs . Find the sum and rate of interest

$$7400 = P + \frac{P3r}{100} \dots (1)$$

$$8600 = P + \frac{P4r}{100} \dots (2)$$

$$1200 = \frac{Pr}{100} \dots (3)$$
subs in (1)
$$P = 3800 , \quad \text{Subs in (3), } r = 31.57\%$$

02. What is the rate of simple interest if a sum of money amounts to 2784 in 4 yrs & 2688 in 3 yrs

$$2784 = P + \frac{P4r}{100} \dots (1)$$

$$2688 = P + \frac{P3r}{100} \dots (2)$$

$$\frac{Pr}{100} \dots (3) \qquad \text{subs in (1)} \quad P = 2400 \text{ , subs in (3) } r = 4\%$$

03. a certain sum amounts to 2800 in 2 yrs and 3250 in 5 yrs . Find the sum and rate of interest

 $2800 = P + \frac{P2r}{100} \dots (1)$ $3250 = P + \frac{P5r}{100}$ $450 = \frac{3Pr}{100}$ $150 = \frac{Pr}{100} \dots (3)$

subs in (1) P = 2500, Subs in (3), r = 6%

Q8

SI1

= SI₂

= SI₃

01. If a simple interest on a sum of money at 6% p.a. for 7 years is equal to TWICE of simple interest on another sum for 9 years at 5% p.a. . The ratio of sum invested will be

 $SI_1 = 2SI_2 \rightarrow P_1.7.\underline{6}_{100} = 2 P_2.9.\underline{5}_{100} \rightarrow 42P_1 = 90P_2 \rightarrow P_1:P_2 = 15:7$

02. a man invests an amount of 15680 in the names of his three sons A , B and C in such a way that they get the same SI after 2 , 3 and 4 years respectively . If the rate of interest is 5% , then the ratio of amount invested in the name of A , B and C is

$$P_{1.2.(5)} = P_{2.3.(5)} = P_{3.4.(5)}$$

$$10 P_{1} = 15P_{2} = 20P_{3}$$

$$P_{1} : P_{2} : P_{3}$$

$$6 : 4 : 3$$

$$2P_{1} = 3P_{2} = 4P_{3} = 12(say)$$

03. a sum of 44000 is divided into three parts such that the corresponding interest earned after 2 years , 3 years and 6 years may be equal . If the rates of simple interest are 6%p.a. , 8%p.a. and 6%p.a. respectively , then the smallest part of the sum will be

$P_{1.2.6} = P_{2.3.8} = P_{3.6.6}$	P1	: P2	: P3	
$\overline{100}$ $\overline{100}$ $\overline{100}$	6	3	2	11
$12P_1 = 24P_2 = 36P_3$			x 4000	x 4000
			8000	44000
$P_1 = 2P_2 = 3P_3 = 6(say)$				

04. Johnson left 1,00,000 with the direction that it should be divided in such a way that his minor sons Tom , Dick and Harry aged 9 , 12 and 15 years should each receive equally after attaining the age 25 years . Rate of interest 3.5% , how much each son receive after getting 25 years old

A = amount recvd by each son on attaining the age 25 yrs

SON 1 - A = $P_1[1+16(0.035)] = 1.56P_1$ $P_1 = A/1.56$ SON 2 - A = $P_2[1+13(0.035)] = 1.455P_2$ $P_2 = A/1.455$ SON 3 - A = $P_3[1+10(0.035)] = 1.35P_3$ $P_3 = A/1.35$ $P_1 + P_2 + P_3 = 100000$ A(0.6410) + A(0.6873) + A(0.7407) = 100000A(0.6410 + 0.6873 + 0.7407) = 100000

A = 48,332.53

6

COMPOUND INTEREST

Q1

01. Find amount for a sum of Rs 4000 at 8% p.a. for 5 yrs compounded annually

A = 4000[1+0.08]⁵ = ₹ 5877

- 02. Find CI for a sum of 16000 at 10% p.a. for 1 ½ yrs payable HALF YEARLY Since compounded HALF YEARLY , i = = 5% = 0.05 , n = 3 CI = 16000[1.05³ - 1] = ₹ 2522
- 03. Find CI for a sum of 8000 at 4% p.a. for 6 yrs compounded HALF YEARLY Since compounded HALF YEARLY , i = = 2% = 0.02 , n = 12 CI = 8000[1.02¹² - 1] = ₹ 2145.9 ≈ ₹ 2146
- 04. Find CI for a sum of 4000 for 6 months at 12% p.a. payable QUARTERLY Since compounded QUARTERLY , i = = 3% = 0.03 , n = 2 CI = 4000[1.03² - 1] = ₹ 243.60
- 05. Find CI for a sum of 40000 at 10% p.a. for 1 yr , interest payable QUARTERLY Since compounded QUARTERLY , i = = 2.5% = 0.025 , n = 4

 $CI = 40000[1.025^4 - 1] = \textbf{\textsterling} 4152.51$

06. Find amount & CI for a sum of 6000 at 12% p.a. for 3 yrs compounded QUARTERLY Since compounded QUARTERLY , i = 3% = 0.03 , n = 12

CI = $6000[1.03^{12} - 1]$ = ₹ 2554.6

07. Find amount for a sum of 10000 at 6% p.a. for 2 years compounded monthly

Since compounded MONTHLY , i = 0.5% = 0.005 , n = 24

A = 10000[1+0.005]²⁴ = ₹ 11271.6 ≈ ₹ 11271

08. An investment of 20000 on interest of 6% p.a. for first 4 yrs , 5% p.a. for next 3 yrs and 4% p.a. for next 2 yrs . Find value of investment after 9 yrs where interest is compounded annually

A = 20000 $[1.06^4]$. $[1.05^3]$ $[1.04^2]$ = ₹ 31614.62

09. The compound interest on half yearly basis on 10,000 the rate for the first and second years being 6% and for third year 9% p.a. is

FOR FIRST 2 YEARS - i = 0.03 , n = 4 COMPOUNDING SEMI ANNUALLY FOR THIRD YEAR - i = 0.045 , n = 2 COMPOUNDING SEMI ANNUALLY CI = 20000 [$(1.03)^4$. $(1.045)^2$ -1] = ₹ 2290.84

 A person deposited 5000 in a bank. The deposit was left to accumulate at 6% compounded quarterly for first 5 years and at 8% compounded semi-annually for next 8 years. The compound amount at the end of 13 years is

For first 5 years - i = 0.015 , n = 20 COMPOUNING QUARTERLY

For next 8 years - i = 0.04 , n = 16 COMPOUNDING SEMI ANNUALLY

A = 5000 [1.015²⁰]. [1.04¹⁶] = ₹ 12613.17

11. CI on any sum at the rate of 5% for two years is ₹ 512.50 then the sum would be

512.50 = P[1.05²-1] → P = ₹ 5,000

12. CI on any sum at the rate of 4% for two years is ₹ 102 . Find SI for the same period , same rate on the same sum

$$102 = P[1.04^2 - 1] \rightarrow P = ₹ 1250$$

SI = 1250 .2.(0.04) = ₹ 100

Q2

01. Find present value of 10000 due in 2 yrs at 5% p.a. compound interest paid ANNUALLY .

10000 = P[1.05]² → P = ₹ 9070.3

02. A certain sum invested at 4% p.a. compounded semi annually amounts to 78,030 at the end of one year . Find the sum .

Since compounded HALF YEARLY , n = 2 , i = 2% = 0.02

78030 = P[1.02]² → P = ₹ 75000

03. Find present value of 20000 due in 3 yrs at 6% p.a. CI paid HALF YEARLY .

Since compounded HALF YEARLY , n = 6 , i = 3% = 0.03

 $20000 = P[1.03]^6 \rightarrow P = ₹ 16749.68$

Q3

01. Difference between CI and SI at 5% p.a. for 2 yrs on a sum of 6000 is

CI - SI =
$$6000[1.05^2 - 1] - 6000 \ 2 \ (0.05)$$

= $6000 \ [1.05^2 - 1 - 0.1]$ = ₹ 15

02. Difference between CI and SI at 8% p.a. for 3 yrs on a sum of 50000 is

 $CI - SI = 50000[1.08^3 - 1] - 50000 3 (0.08)$

= $50000[1.08^3 - 1 - 0.24]$ = ₹ 985.6

03. Difference between CI and SI at 5% p.a. for 4 yrs on a sum of 10000 is

$$CI - SI = 10000[1.05^4 - 1] - 10000 4 (0.05)$$

 $= 10000[1.05^4 - 1 - 0.20] \qquad = ₹ 155.06$

04. Difference between SI and CI on 2400 at 5% p.a. for 2 yrs

$$CI - SI = 2400[1.05^2 - 1] - 2400 2 (0.05)$$

$$= 2400[1.05^2 - 1 - 0.10] =$$

05. the difference between SI and CI on a certain sum for 2 years at 10% p.a. is ₹ 10. Find the sum

₹ 6

CI - SI = 10

P[1.1² - 1 - 2(0.1)] = 10 P = ₹ 1000

06. a compound interest on a sum for 2 years is 30 more than the simple interest at the rate of 5% p.a., then sum is

CI - SI = 30

P[1.05² - 1 - 2(0.05)] = 30 P = ₹ 12000

07. the difference between SI and CI on a certain sum invested for 3 years at 6% p.a. is ₹ 110.16 Find the sum

CI - SI = 110.16

 $P[1.06^3 - 1 - 3(0.06)] = 110.16 \qquad P = ₹ 10000$

08. the difference between SI and CI on a certain sum for 3 years at 5% p.a. is ₹ 228.75 . The compound interest on the sum for 2 years at 5% p.a. is

CI - SI = 228.75

 $P[1.05^3 - 1 - 3(0.5)] = 228.75 \rightarrow P = ₹ 30000$

 $CI = 30000[1.05^2 - 1] = ₹ 3075$

Q4

01. A machinery is depreciated at 10% p.a. for 3 years costing Rs 50,000 . Find scrap value

Scarp val (Depreciated val.)

A = $50000[1-0.1]^3$ = ₹ 36450

02. Find depreciation if machinery worth ₹ 12000 is depreciated at 6% p.a. for 4 years

Depreciated value A = $12000[1-0.06]^4$ = ₹ 9369

Depreciation = P - A = 12000 - 9369 = ₹ 2631

03. The useful life of a machine is estimated to be 10 years and cost 10,000 . Rate of depreciation is 10%p.a. The scrap value at the end of its life is

Depreciated value A = $10000[1-0.1]^{10} = ₹ 3468.78$

04. A machinery worth 10000 is depreciated at the rate of 10% p.a. for first 3 years , 8%p.a for next 2 years. Find its value after 5 years

Depreciated value A = $10000[1-0.1]^3[1-0.08]^2 = ₹ 6170.26$

Q5

01. A sum of money at 5% p.a. CI doubles in

 $2P = P[1.05]^n$ n = 14 years (approx.)

02. a sum at a certain rate of interest compounded annually doubles in 5 yrs . In how many years will it become 8 times

 $2P = P[1+i]^5 \rightarrow 2 = [1+i]^5 \rightarrow 8 = [1+i]^{15} \qquad n = 15 \text{ years}$ $ALTERNATE METHOD \qquad t \ 0 \ 5 \ 10 \ 15 \ years$ $A \ P \ 2P \ 4P \ 8P$

03. a sum at a certain rate of interest compounded annually doubles in 4 yrs . In how many years will it become 32 times

 $2P = P[1+i]^4 \rightarrow 2 = [1+i]^4 \rightarrow 2^5 = ([1+i]^4)^5 \rightarrow 32 = [1+i]^{20} \quad n = 20 \text{ years}$ $ALTERNATE METHOD \qquad t \quad 0 \quad 4 \quad 8 \quad 12 \quad 16 \quad 20 \quad \text{years}$ $A \quad P \quad 2P \quad 4P \quad 8P \quad 16P \quad 32P$

04. A sum amounts to 1331 at a principal of 1000 at 10% compounded annually . Find the time

 $1331 = 1000[1.1]^n \rightarrow 1.1^n = 1.331 \rightarrow n = 3 \text{ yrs}$

05. the population of a town increases every year by 2% of the population at the beginning of that year. The number of years by which the total increase of population be 40% is

 $1.4P = P[1.02]^n \rightarrow 1.02^n = 1.4 \rightarrow n = 17 \text{ yrs}$

06. annual birth and death rates per 1000 are 39.4 and 19.4 respectively . The number of years in which the population will be doubled assuming there is no immigration or emigration

NET Growth rate = 39.4 - 19.4 = 20 per thousand = 2/100, i = 0.02

 $2P = P[1.02]^n$ n = 35 years

07. In what time will 8000 amount to 8820 at 10% p.a. interest compounded half yearly

Since compounding is done semi annually , i = 0.05 , n - no. of half years $8820 = 8000[1.05]^n$ $1.1025 = 1.05^n \rightarrow n = 2$ (HALF YEARS) = 1 yrs

08. 16000 invested at 10%p.a. compounded semi annually amounts to 18522 . Find the time period of investment

Since compounding is done semi annually , i = 0.05 , n - no of half years $18522 = 16000[1.05]^n$ $1.157625 = 1.05^n \rightarrow n = 3$ (HALF YEARS) = 1 ¹/₂ yrs

09. In what time will ₹ 390625 amount to ₹ 456976 at 8% p.a. when the interest is compounded semi – annually

Since compounding is done semi annually , i = 0.04 , n – no. of half years

 $456976 = 390625[1.04]^n$

 $1.1699 = 1.04^{n} \rightarrow n = 4 (HALF YEARS) = 2 yrs$

10. In how many years a sum of money trebles at 5%p.a CI payable on half yearly basis

Since compounding is done HALF YEARLY , i = 0.025 , n - no. of half years

 $3P = P[1.025]^{n}$

 $3 = [1.025]^{n}$

44 < n < 45 HALF YEARS

22 < n < 22.5 YRS SELECT THE OPTION ACCORDINGLY

11. How long will 12000 take to amount to 14000 at 5% p.a. converted quarterly

Since compounding is done quarterly , i = 5%/4 = 1.25% , n – no of Quarters

 $14000 = 12000[1.0125]^{n}$

 $1.1667 = 1.0125^{n}$

12 Quarters < n < 13 Quarters

3 years < n < 3.25 years

SELECT THE OPTION ACCORDINGLY

 A machine is depreciated at the rate of 20% on reducing balance. The original cost of the machine was 1,00,000 and its ultimate scrap value was 30,000. The effective life of the machine

 $30000 = 100000[1-0.2]^{n}$ $0.8^{n} = 0.3$ 5 years < n < 6 years

SELECT THE OPTION ACCORDINGLY

 a machine depreciates at 10% of its value at the beginning of a year. The cost and scrap value realized at the time of sale being 23240 and 9000 respectively. For how many years the machine was put to use

 $9000 = 23240[1-0.1]^n$ $0.9^n = 0.38726$

n = 9 years

14. a machine worth 4,90,740 depreciates at 15% on its opening value each year . When its value would reduce to 2,00,000

a) 4 yrs , 6 months b) 4 yrs , 7 months c) 4 yrs , 5 months d) 5 yrs , 7 months

 $200000 = 490740[1-0.15]^{n}$

 $0.85^{n} = 0.4075$

5 years < n < 6 years OPTION d

15. a machine worth 4,90,740 depreciates at 15% on its opening value each year. When its value would reduce by 90% a) 11 yrs, 6 months b) 11 yrs, 7 months c) 11 yrs, 8 months d) 14 yrs, 2 months 49074 = 490740[1-0.15]ⁿ 0.85ⁿ = 0.1 14 years < n < 15 years OPTION d</p>

- **Q6**
- 01. At what rate of CI will a sum of money become 16 times in four years if interest is calculated compounding annually

 $16P = P[1+i]^4$ $2^4 = [1+i]^4$

1+i = 2 $\therefore i = 1$ r = 100% p.a.

02. Find the rate percent p.a. if 2,00,000 amount to 2,31,525 in 1 $\frac{1}{2}$ year interest being compounded half yearly .

Since compounding is done semi annually , i = half yearly rate , n = 3 231525 = $20000[1+i]^3$

 $1.157625 = [1+i]^3$.

 $1.05^3 = [1+i]^3$. 1+i = 1.05, i = 0.05 = 5% (HALF YEARLY RATE)

10% p.a.

Q7

- 01. Effective annual rate of interest compounding at nominal rate at 6% p.a. payable half yearly is Since compounding is done semi annually , i = 3% , n = 2 (FOR ONE YEAR) $E = (1+i)^n - 1 = (1.03)^2 - 1 = 0.0609 = 6.09\%$
- 02. Effective annual rate of interest compounding at nominal rate at 8% p.a. payable half yearly is Since compounding is done semi annually , i = 4% , n = 2 (FOR ONE YEAR) $E = (1+i)^n - 1 = (1.04)^2 - 1 = 0.0816 = 8.16\%$
- 03. Effective annual rate of interest of 6% p.a. converted Quarterly Since compounding is done Quarterly , $i = \frac{6\%}{4} = 1.5\%$, n = 4 (FOR ONE YEAR) $E = (1+i)^n - 1 = (1.015)^4 - 1 = 0.0614 = 6.14\%$
- 04. Effective annual rate of interest of 7% p.a. converted Quarterly Since compounding is done Quarterly , $i = \frac{7\%}{4} = 1.75\%$, n = 4 (FOR ONE YEAR) $E = (1+i)^n - 1 = (1.0175)^4 - 1 = 0.0718 = 7.18\%$

05. Effective annual rate of interest of 8% p.a. converted monthly

Since compounding is done monthly , i = $\frac{8\%}{12}$ = 0.67% , n = 12 (FOR ONE YEAR) E = $(1+i)^n - 1 = (1.0067)^{12} - 1 = 0.0834 = 8.34\%$

06. Which is better investment

a) 9% p.a. compounded half yearly b) 9.23%p.a. SI Since compounding is done semi annually , i = 4.5% , n = 2 (FOR ONE YEAR) E = $(1+i)^n - 1 = (1.045)^2 - 1 = 0.0920 = 9.20\% < 9.23\%$ p.a. SI Hence OPTION (b) is better investment

- 07. Which is better investment
 - a) 3% p.a. compounded monthly
 - b) 3.2%p.a. SI

Since compounding is done monthly , $i = \frac{3\%}{12} = 0.25\%$, n = 12 (FOR ONE YEAR) E = $(1+i)^n - 1 = (1.0025)^{12} - 1 = 0.0304 = 3.04\% < 3.2\%$ p.a. SI Hence OPTION (b) is better investment

ANNUITY

Q1 ACCUMULATED AMOUNT OF ANNUITY (A)

01. The amount of annuity of ₹ 2000 payable at the end of each year for 5 years 8%p.a.

$$P = 2000$$
, $i = 8\%$, $n = 5$

$$A = 2000 \left[\frac{1.08^5 - 1}{0.08} \right] = 11733.20$$

02. The future value of an annuity of ₹ 5000 is made annually for 8 years at interest rate of 9% compounded annually [1.09⁸ = 1.99256]

$$P = 5000$$
, $i = 9\%$, $n = 8$

$$F.V.=5000\left(\frac{1.09^8-1}{0.09}\right) = 55142.22$$

03. The future value of an annuity of ₹ 1500 is made annually for 5 years at interest rate of 10% compounded annually

$$P = 1500$$
, $i = 10\%$, $n = 5$

$$F.V.=1500\left(\frac{1.1^5 - 1}{0.10}\right) = 9157.65$$

04. The future value of an annuity of ₹ 1000 is made annually for 5 years at interest rate of 14% compounded annually

$$F.V. = 1000 \left(\frac{1.14^5 - 1}{0.14} \right) = 6610.10$$

05. Mr Bean deposits ₹ 25000 at the end of every year at 12% p.a. CI . What amount would he receive at the end of 10 years

$$P = 25000$$
, $i = 12\%$, $n = 10$

$$A = 25000 \left[\frac{1.12^{10} - 1}{0.12} \right] = 438718.38$$

06. A person invests ₹ 500 at the end of each year with a bank which pays interest at 10% CI annually . The amount standing to his credit one year after he has made his yearly investment for the 12th time

amount at the end of
$$12^{\text{th}}$$
 year A = 500 $\left(\frac{1.1^{12} - 1}{0.1}\right)$ = 10,692.14

Amount at the end of 13^{th} year = 10692.14 x(1.1) = 11,761.36

07. The amount of annuity of ₹ 6000 payable at the end of each 3 months for 4 years compounded Quarterly at 8%p.a.

P = 6000, i = 2%, n = 16

$$A = 6000 \left[\frac{1.02^{16} - 1}{0.02} \right] = 111835.7$$

08. The value of amount at the end of 12 years of an annuity of ₹ 1200 payable at the BEGINNING of each year for 12 yrs at 8%p.a. CI ANNUITY DUE / ANNUITY IMMEDIATE P = 1200, i = 8%, n = 12

$$A = 1200 \left[\frac{1.08^{12} - 1}{0.08} \right] (1.08) = 24,594.35$$

09. Mr Piyush invest ₹ 10000 every year STARTING FROM TODAY for next 10 yrs rate of interest is 8% p.a. Find FV of annuity ANNUITY DUE / ANNUITY IMMEDIATE P = 10000 , i = 8% , n = 10

$$A = 10000 \left(\frac{1.08^{10} - 1}{0.08}\right) (1.08) = 156,454.87$$

GIVEN ACCUMULATED AMOUNT OF ANNUITY (A) – FINDING THE INSTALMENT SIZE

01. How much amount is required to be invested every year as to accumulate ₹ 6,00,000 at the end of 10 years , if interest is compounded annually at 10% rate of interest (GIVEN (1.1)¹⁰ = 2.59374)

A = 6,00,000 , i = 10% , n = 10
600000 = P
$$\left(\frac{1.1^{10}-1}{0.1}\right)$$
 P = 37647.30 \approx 37,647

02. a company establishes a sinking fund to provide for the payment of ₹ 2,00,000 debt maturing in 20 years . Contributions to the fund are to be made at the end of every year . Find the amount of each annual deposit if interest is 5% p.a.

A = 2,00,000 , i = 5% , n = 20
200000 = P
$$\left[\frac{1.05^{20}-1}{0.05}\right]$$
 P = 6048.52 \approx 6049

03. A company requires ₹ 20,00,000 at the end of 10 yrs to replace one of its assets . It is decided to create a sinking fund by investing a fixed amount every year in securities which gives 10% CI . Yearly investment is

$$A$$
 = 20,00,000 , i = 10% , n = 10

$$2000000 = P\left(\frac{1.1^{10}-1}{0.1}\right) \qquad P = 125,490.79$$

04. a sinking fund is created for redeeming debentures worth ₹ 5 lacs at the end of 25 years . How much provision needs to be made out of profits each year provided the sinking fund investments can earn interest at 4% p.a.

$$A = 5,00,000$$
, $i = 4\%$, $n = 25$

 $500000 = P\left(\frac{1.04^{25}-1}{0.04}\right) \qquad P = 12,006$

05. A company issued 10% cumulative debentures of ₹ 100 each , 5000 cumulative debentures are to be redeemed with 10% of interest for 5 yrs . For this a sinking fund is created and invested at 12% rate of CI . Sum to be transferred every year to sinking fund is

Amount to be paid on redemption of debentures

$$A = 5000 \times 100 \times (1.1)^5 = 805255$$

 $805255 = P \left[\underbrace{1.12^{5}-1}_{0.1} \right] \qquad P = 1,26,755$

06. A machine costing ₹ 5,20,000 with an estimated life of 25 years . A sinking fund is created to replace it by new model at 25% higher cost after 25 years with a scrap value realization of ₹ 25000 . What amount should be set aside every year if sinking fund investment at 3.5% CI p.a.

A =
$$520000 + 25\% - 25000 = 6,25,000$$

A = 625000 , i = 3.5% , n = 25
 $625000 = P\left[\frac{1.035^{25}-1}{0.035}\right]$ P = $16,046.27$

CHECK FOR NEAREST OPTION

07. Mr Yash wants ₹ 10,00,000 at the end of 5 yrs It opens recurring account with the post office at 10%p.a CI monthly . What money should be deposited at the end of every month ?

A = 10,00,000 , i =
$$10/12 = 0.83\%$$
 , n = 5 x 12 = 60

 $1000000 = P \left[\frac{1.0083^{60} - 1}{0.0083} \right] P = 12,927.37$ CHECK FOR NEAREST OPTION

08. Ratan aged 45 wishes his wife Ratna to have 40 lacs at his death . His expectation of life is another 30 years and he starts making equal annual investments COMMENCING NOW at 3% p.a . How much should he invest annually

ANNUITY DUE / ANNUITY IMMEDIATE A = 40,00,000, i = 3%, n = 30

$$4000000 = P \left(\frac{1.03^{30}-1}{0.03}\right) (1.03) \qquad P = 81,628.20$$

Q3 PRESENT VALUE OF ANNUITY (V)

01. The present value of an annuity of ₹ 3000 for 15 years at 4.5%p.a. CI is [1.045¹⁵ = 1.935282]

$$V = 3000 \left[\frac{1 - 1.045^{-15}}{0.045} \right] = 32,218.63$$

02. The present value of an annuity of ₹ 5000 per annum for 12 years at 4%p.a. CI

$$V = 5000 \left[\frac{1 - 1.04^{-12}}{0.04} \right] = 46,925.36$$

03. The present value of an annuity of ₹ 1000 payable at the end of each year for 10 years at 6%p.a. compounding annually [$1.06^{-10} = 0.5584$]

$$V = 1000 \left[\frac{1 - 1.06^{-10}}{0.06} \right] = 7360$$

04. Present value of annuity which pays ₹ 200 at the end of each 3 months for 10 years , assuming money to be worth 5% p.a. converted quarterly

Since quarterly , P = 200 , i = 1.25% , $n = 4 \times 10 = 40$ quarters

$$V = 200 \left[\frac{1 - 1.0125^{-40}}{0.0125} \right] = 6265.38$$

05. Pravin buys a house paying ₹ 50,000 in cash and balance in 20 installments of 8000 each at the end of each year . If interest is at 16% p.a. how much he should have paid if had purchased it cash down

Present value of annuity V = Loan amount borrowed

Down payment 50,000 + V = Present Price of the house

$$V = 8000 \left[\frac{1 - 1.16^{-20}}{0.16} \right] = 47,430 \quad , \text{ Price of house} = 50000 + 47430 = 97430$$

06. A person bought a house paying ₹ 20,000 cash down and ₹ 4000 at the end of each year for 25 years at 5% p.a. CI . The cash down price is

Loan amount =

 \sim

$$V = 4000 \left[\frac{1 - 1.05^{-25}}{0.05} \right] = 56,375.8 , \text{ Price of house} = 20000 + 56,376 = 76,376$$

07. a car is purchased for ₹ 1,00,000 down payment and an instalment of ₹ 6500 per month for 3 years . If rate of interest is 15% p.a. compound monthly , cash price is

Present value of annuity V = Loan amount borrowed Loan amount borrowed + down payment = cash price of car

Since monthly repayment , P = 6500, i = 15/12 = 1.25%, $n = 3 \times 12 = 36$ months

$$V = 6500 \left[\frac{1 - 1.0125^{-36}}{0.0125} \right] = 187507.23 \approx 187507$$

Cash price of car (Present price) = 1,00,000 + 187507 = 287507

08. A person retires at 60 years receiving a pension of ₹ 14400 a year paid in half yearly instalments for the rest of his life with his expectation to be 13 years and interest at 4% p.a. payable half yearly. What single sum is equivalent to his pension ?

PENSION OPTIONS :

- **OPTION 1** ON RETIREMENT , PERSON RECEIVES 7200 EVERY 6 MONTHS FOR NEXT 13 YEARS
- OPTION 2 SINGLE PAYMENT AT RETIREMENT EQUIVALENT TO ABOVE PENSION = PRESENT VALUE OF ANNUITY OF 7200 EVERY 6 MONTHS FOR 13 YEARS @ 4%P.A.

Since pension recvd is half yearly , P = 7200 , i = 2% , $n = 2 \times 13 = 26$

$$V = 7200 \left[\frac{1 - 1.02^{-26}}{0.02} \right] = 144871.45$$

CHECK FOR NEAREST OPTION

Q4 PRESENT VALUE OF ANNUITY – FIND THE INSTALMENT SIZE

01. A loan of ₹ 30,000 at the interest rate of 6% compounded annually is to be amortized by equal payments at the end of each year for 5 years . The annual payment

$$30000 = P\left(\frac{1-1.06^{-5}}{0.06}\right) \qquad P = 7121.89$$

02. A loan of ₹ 10,000 is to be paid back in 30 equal instalments . The amount of each installment to cover the principal and at 4% p.a. CI is

$$10000 = P\left[\frac{1 - 1.04^{-30}}{0.04}\right] \qquad P = 578.30$$

03. a man purchased house valued at ₹ 3,00,000 by making a payment of ₹ 2,00,000 at the time of purchase and agreed to pay balance with interest at 12% p.a. compounded half yearly in 20 equal half yearly instalments . If first installment is paid after 6 months from the date of purchase then amount of each instalment is

Loan amount V = 1,00,000, since instalments are paid half yearly i = 6%

$$100000 = P\left(\frac{1-1.06^{-20}}{0.06}\right) \qquad P = 8718.45$$

04. Vipul purchases a car for ₹ 5,50,000 . He gets a loan of ₹ 5,00,000 at 15% p.a. from a bank and balance ₹ 50,000 he pays at the time of purchase . He has to pay the whole amount of loan in 12 monthly instalments with interest starting from end of the first month . The money he has to pay at the end of every month [Given 1.0125¹² = 1.16075452]

Loan amount V = 1,00,000, since instalments are paid monthly i = 15/12% = 1.25%

 $500000 = P\left[\frac{1-1.0125^{-12}}{0.0125}\right] P = 45,129.15 CHOOSE THE NEAREST OPTION$

05. Mr Paul borrows ₹ 20,000 on condition to repay it with CI at 5% p.a. in annual instalments of 2000 each . The number of years for the debt to be paid off is

a. 10 years b. 12 years $20000 = 2000 \left[\frac{1 - 1.05^{-n}}{0.05} \right] \rightarrow 1.05^{-n} = 0.5$ $1.05^{n} = 2$ 14 < n < 15n = 14.2 years

Q5

LEASING -

ITS AN ARRANGEMENT UNDER WHICH OWNER OF ASSET (LESSOR) ALLOWS THE USER OF THE ASSET (LESSEE) TO USE THE ASSET FOR A DEFINED PERIOD OF TIME (LEASE PERIOD) BY PAYING FIXED RENT (LEASE RENTAL) OVER A GIVEN PERIOD OF TIME

CAPITAL EXPENDITURE (INVETMENT DECISION)

CAPITAL EXPENDITURE MEANS PURCHASING AN ASSET (WHICH RESULTS IN CASH OUTFLOW) TODAY IN ANTICIPATION OF BENEFITS (CASH INFLOW) EXAMPLE – LEASING AN ASSET ON RENT. IF THE PRESENT VALUE OF CASH INFLOWS IS GREATER THAN PRESENT VALUE OF CASH OUTFLOWS, DECISION SHOULD BE IN THE FAVOUR OF INVESTMENT

- 01. a company considering a proposal of purchasing a machine either by making a full payment of ₹ 4000 or by leasing it for four years at an annual rate of ₹ 1250. Which course of action is preferable, if the company can borrow money at 14% compounded annually [1.14⁴ = 1.68896]
 - OPTION 1 Leasing a machine for 4 years @ 1250 p.a

Present value of rental outflows

$$V = 1250 \left[\frac{1 - 1.14^{-4}}{0.14} \right] = 3642.14$$

OPTION 2 - Purchasing val. of m/c = ₹ 4000,

SINCE THE TOTAL PRESENT VALUE OF ALL THE FUTURE RENTAL OUTFLOWS IS LESS THAN THE PURCHASE VALUE OF M/C , LEASING THE M/c IS PREFERABLE

02. a company may obtain a machine either by leasing it for 5 years (USEFUL LIFE) at an annual rent of ₹ 2000 or by purchasing the machine for ₹ 8100. If the company can borrow money at 18% p.a., which alternative is preferable

OPTION 1 - Leasing a machine for 5 years @ annual rent of ₹ 2000

Present value of rental outflows

$$V = 2000 \left[\frac{1 - 1.18^{-5}}{0.18} \right] = 6254.34$$

OPTION 2 - Purchasing val. of m/c = ₹8100,

SINCE PRESENT VALUE OF ALL THE FUTURE RENTAL OUFLOWS IS LESS THAN PURCHASE VALUE OF MACHINE , LEASING THE M/C IS PREFERABLE

03. A person wants to lease out a machine costing 5,00,000 for a 10 year period . It has a fixed rental of 51,272 per annum payable annually starting from the end of first year . Suppose the rate of interest is 10% p.a. compounded annually on which money can be invested . To whom the agreement is favorable – LESSEE OR LESSOR

Present value of rental inflows $V = 51272 \left(\frac{1 - 1.1^{-10}}{0.1} \right) = 3,15,044$

Purchase val. of machine = ₹ 5,00,000

AGREEMENT IS NOT FAVORABLE TO LESSOR . SINCE ALL THE RENTAL INFLOWS WHEN DISCOUNTED TO PRESENT DATE SUMED UP TO ₹ 3,15,044 WHICH IS FAR LESS THAN THE PURCHASE VALUE OF M/C ₹ 5,00,000 .

KHADE KHADE AAJ HI LESSOR KO \approx 1,75,000 KA CHUNA LAG GAYA

AGREEMENT IS FAVORABLE TO LESSEE . SINCE ALL THE RENTAL OUTFLOWS WHEN DISCOUNTED TO PRESENT DATE SUMED UP TO ₹ 3,15,044 WHICH IS FAR LESS THAN THE PURCHASE VALUE OF M/C ₹ 5,00,000 . LESSEE SAYS TO HIMSELF "THEN WHY BUY , JUST LEASE IT – SASTA MEIN NIPTAO" LESSEE KA FAIDA , LESSOR KO NUKSAAN

04. ABC ltd wants to lease out an asset costing ₹ 360,000 for a 5 year period . It has a fixed rental of ₹ 1,15,000 per annum payable annually starting from the end of first year . Suppose rate of interest is 14% per annum compounded annually on which money can be invested by the company . Is this agreement favorable to the company .?

Present value of rental inflows
$$V = 1,15,000 \left(\frac{1 - 1.14^{-5}}{0.14} \right) = 3,94,804.31$$

Purchase val. of machine = ₹ 3,60,000

AGREEMENT IS FAVORABLE TO LESSOR . SINCE PRESENT VALUE OF CASH INFLOWS WHEN DISCOUNTED TO PRESENT DATE SUMED UP TO ₹ 3,94,804 WHICH IS MORE THAN THE PURCHASE VALUE OF M/C ₹ 3,60,000 (CASH OUTLFOW) STRAIGHT PROFIT OF 394804 – 360,000 = 34804 AT THE TIME OF PURCHASE OF M/C

05. A machine can be purchased for ₹ 50,000 . Machine will contribute 12000 per year for the next five years . Assume borrowing cost is 10% per annum compounded annually . Determine whether machine should be purchased or not

Present value of annual contribution $V = 12000 \left(\frac{1 - 1.1^{-5}}{0.1} \right) = 45,489.44$

Purchase val. of machine = ₹ 50,000

PRESENT VALUE OF TOTAL PROFITS CONTRIBUTED BY THE MACHINE IS LESS THAN THE PURCHASE VALUE OF THE MACHINE AND HENCE MACHINE SHOULD NOT BE PURCHASED IN SHORT – PURCHASE OF MACHINE WILL STRAIGHT BOOK A LOSS OF 50000 – 45490 = 4510 TODAY

06. A machine with a useful life of seven years cost ₹ 10,000 while another machine with useful life of 5 years cost ₹ 8000. The first machine saves labour expenses of ₹ 1900 annually and the second machine saves labour expenses of ₹ 2200 annually . Determine the preferred course of action . Assume cost of borrowing at 10% compounded per annum

MACHINE 1

V = 1900 $\left(\frac{1-1.1^{-7}}{0.1}\right)$ = 9250 < 10000 (COST OF M/c)
54
5/6
V = 2200 $\left[\frac{1-1.1^{-5}}{0.1}\right]$ = 8340 > 8000 (COST OF M/c)
HENCE 2 ND MACHINE IS PREFERABLE

PERPETUITY -

PERPETUITY IS AN ANNUITY IN WHICH THE PERIODIC PAYMENTS OR RECIEPTS BEGIN ON A FIXED DATE AND CONTINUE INDEFINITELY OR PERPETUALLY. FIXED COUPON PAYMENTS ON PERMANENTLY INVESTED SUM OF MONEY

PRESENT VALUE OF PERPETUITY (ANNUITY INFINITE)

$$PVA\infty = \frac{R}{1+i} + \frac{R}{(1+i)^2} + \frac{R}{(1+i)^3} + \dots = \frac{R}{1-\frac{1}{1+i}} = \frac{R}{i}$$
FOR AN INFINITE GP
$$S\infty = \frac{a}{1-r}$$

GROWING PERPETUITY

RECEIPTS / CASH INFLOWS MUST GROW AT CONSTANT RATE . LETS UNDERSTAND EXAMPLE – ASSUMING GROWTH RATE 5% AND FIRST RECEIPT (CASH INFLOW) R = 100 ,

> CASH INFLOWS AT THE END OF 1^{ST} YEAR = 100 2^{ND} YEAR = 100(1.05) = 105 3^{RD} YEAR = 100(1.05)² = 110.25

 4^{TH} YEAR = 100(1.05)³ = 115.7625∞

Г

PRESENT VALUE OF GROWING PERPETUITY (ANNUITY INFINITE)

LET i = DISCOUNT RATE, g = GROWTH RATE

							FUR AN	INFINITE GP
PVA∞=	$\frac{R}{1+i}$	+ R <u>(1+g)</u> + (1+i) ²	+ $R \frac{(1+g)^2}{(1+i)^3}$ +	∞ =	$\frac{R_{/1+i}}{1-1+g}$	= <u>R</u> i–g	$S\infty = \frac{a}{1-a}$	_ -r
					1 1 1 1			

01. P.V. of an annuity of ₹ 80 made at the end of each 6 months forever , if money worth 4% p.a is compounded semi- annually

Since cash flow = 80 at end of every 6 months, i = 4%/2 = 2% = 0.02

$$PVA\infty = \frac{R}{i} = \frac{80}{0.02} = 4000$$

02. A person desires to create a fund to be invested at 10% CI per annum to provide a prize of ₹ 300 every year . Find the deposit the person has to make today

$$PVA\infty = \frac{R}{i} = \frac{300}{0.1} = 3000$$

03. John wants to create a fund to donate ₹ 1800 every month to a deprived family . Rate of interest being 12% p.a. , find amount to be deposited

Since receipts R = 1800 are received every month , i = $\frac{12\%}{12} = 1\% = 0.01$

$$PVA\infty = \frac{R}{i} = \frac{1800}{0.01} = 180000$$

04. Determine the present value of perpetuity of ₹ 50,000 per month @ rate of interest 12% p.a. is

Since receipts are made monthly, $i = \frac{12\%}{12} = 1\% = 0.01$

 $PVA\infty = \frac{R}{i} = \frac{50000}{0.01} = 50,00,000$

05. Ramesh wants to retire and receive ₹ 3000 a month . He wants to pass this monthly payments to future generations after his death . He can earn an interest of 8% compounded annually . How much will he need to deposit today to start receiving the above starting from the end of first month . Also do find the deposit amount if Ramesh wants the payments to start immediately

Since receipts are made monthly , i = $\frac{8\%}{12}$ = 0.667% = 0.00667

$$PVA\infty = \frac{R}{i} = \frac{3000}{0.00667} = 4,49,775$$

If Ramesh wants payments to start today

PVA = 4,49,775 + 3000 = 4,52,775The extra 3000 deposit will provide the immediate payment of 3000 and rest 4,49,775 will take care of future 3000 payments

06. If the discount rate is 7% p.a , how much would you pay to receive ₹ 500 growing at 5% annually forever

 $PVA\infty = \frac{R}{i-g} = \frac{500}{0.07-0.05} = 25000$