

Measures of Central Tendency & Dispersion

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- If all the values assumed by a variable are constant say k , then AM also k .

eg. $\frac{3+3+3}{3} = \frac{9}{3} = 3$ etc.

- The algebraic sum of deviations of a set of observation from their AM is zero.

$$\frac{3+4+5+6+7}{5} = \frac{25}{5} = 5$$

3-5
4-5
6-5
5-5
7-5

$$\sum (x - \bar{x}) = 0$$

always for individual series

for discrete/continuous series

$$\sum f(x - \bar{x}) = 0$$

- Change in origin means - some value added or subtracted from observation
- Scale - multiplied or divided from observation

- In continuous series upper limit - lower limit = class length

- If question asks about CF than (+), otherwise in F (-)
- If question don't tell about less than type or more than then ^{use less than}

- Formula of AM = $\frac{\sum_{i=1}^n x_i}{n}$ for individual & discrete series

- $\frac{\sum fx}{\sum f}$ for discrete series & continuous series

- If there are 3 observations, then the sum of deviation of the observation from AM is zero.

- AM is affected due to change in scale, as well as due to change in origin.

If two variables x and y are related as $y = a + bx$, where a and b are constants, and \bar{x} is known, then

$$\bar{y} = a + b\bar{x}$$

eg. $\bar{x} = 10$ $\bar{y} = ?$

$$2\bar{x} + \bar{y} + 7 = 0$$

$$2 \times 10 + \bar{y} + 7 = 0$$

$$20 + 7 + \bar{y} = 0$$

$$\bar{y} = -27$$

$$\bar{y} = a + b\bar{x}$$

$$\bar{y} = -7 + (-2 \times 10)$$

$$\bar{y} = -7 + (-20) = \bar{y} = -27$$

- If there are two groups containing n_1 and n_2 observations with respective means as \bar{x}_1 and \bar{x}_2 , then combined \bar{x} is given by -

$$\bar{x} = \frac{n_1\bar{x}_1 + n_2\bar{x}_2}{n_1 + n_2}$$

eg. Module Q. 11 Set B Pg. 1427

Let, the no. of total workers is = 100

+ skilled worker (K.O.) (a) 40

$$\text{So, } n_1 = 15000 \quad n_2 = 10000$$

$$x_1 = 40 \quad x_2 = 60$$

$$\frac{n_1\bar{x}_1 + n_2\bar{x}_2}{n_1 + n_2} = \frac{(15000 \times 40) + (10000 \times 60)}{60 + 40}$$

$$= \frac{600000 + 600000}{100}$$

$$= \frac{1200000}{100}$$

$$\bar{x} = \frac{1200000}{100} = 12000$$

Geometric mean

Geometric mean is used to calculate the average of rates & Percentages.

$$\text{formula} = (x_1 \times x_2 \times x_3 \times \dots)^{\frac{1}{n}}$$

eg. $(1 \times 9 \times 27)^{\frac{1}{3}} = 6.24$

• GM of discrete series is calculated as-

$$GM = (x_1^{f_1} \times x_2^{f_2} \times x_3^{f_3} \times \dots)^{1/n}$$

eg.
$$\begin{matrix} x & 2 & 4 & 8 & 16 \\ f & 2 & 3 & 3 & 2 \end{matrix}$$

$$(2^2 \times 4^3 \times 8^3 \times 16^2)^{1/10} = 5.66 \text{ Ans}$$

• If all the values assumed by a variable are constant, say, K, then the GM is also K

eg. $(5 \times 5 \times 5 \times 5)^{1/4} = 5$

• GM of product of two numbers is the product of their GM's. In other words, if there are two variables x and y and there is another variable z, such that $z = xy$, then GM of x x GM of y

eg. If GM of x is 10 & GM of y is 15, then GM of xy is-

$$\begin{aligned} GM(xy) &= GM \text{ of } x \times GM \text{ of } y \\ &= 10 \times 15 \\ &= 150 \text{ Ans} \end{aligned}$$

• GM of the ratio of two numbers is the ratio of their GMs. In other words, if there are two variables x and y and there is another variable z, such that $z = \frac{x}{y}$

then $GM \text{ of } z = \frac{GM \text{ of } x}{GM \text{ of } y}$

eg. GM of x is 10, GM of y is 15, the GM of x/y is-

$$= \frac{10}{15} = \frac{2}{3} \text{ Ans}$$

• ~~GM of~~ Logarithm of GM for a set of ~~obs~~ observations is the AM of the logarithm of the observations

$$\log GM = \frac{\sum \log n}{n}$$

$n \rightarrow$ means n

eg. 3, 6, 12

$$(3 \times 6 \times 12)^{1/3} = 6$$

and $\log 6 = 0.7782$

From that, AM of $\log n$ is same as $\log 6$

$$\log 3 = 0.4471, \log 6 = 0.7782, \log 12 = 1.076$$

$$AM = \frac{0.4471 + 0.7782 + 1.076}{3} = 0.7782$$

Simple h, jo $(3, 6, 12)^{1/3}$ ka GM dena me ayega wahi in sab ke log ki value jese AM ki value me ayega

Harmonic mean - It is used to calculate the average of speeds.

It is given by the reciprocal of the arithmetic mean of the reciprocal of the observations.

$$\text{Formulae} = HM = \frac{n}{\sum \left(\frac{1}{x} \right)}$$

eg. 2, 6, 10

$$\frac{3}{\frac{1}{2} + \frac{1}{6} + \frac{1}{10}} = \frac{3}{\frac{15+5+3}{30}} = \frac{3}{\frac{23}{30}}$$

$$= \frac{90}{23} \quad \underline{\text{Ans}}$$

Continuous / Discrete series of Harmonic mean -

$$HM = \frac{N}{\sum \left(\frac{f}{x} \right)} \quad \text{or} \quad \frac{\sum f}{\sum \left(\frac{f}{x} \right)}$$

eg.

x	2	4	8	16
f	2	3	3	2

$$HM = \frac{2+3+3+2}{\frac{2}{2} + \frac{3}{4} + \frac{3}{8} + \frac{2}{16}} = \frac{10}{\frac{16+(2+6+2)}{16}} = \frac{10}{\frac{36}{16}}$$

$$\frac{160}{36} = 4.44 \quad \underline{\text{Ans}}$$

- If all the values assumed by a variable are constant, say, k , then the harmonic mean is also k .

eg. 9, 9, 9

$$HM = \frac{N}{\sum \left(\frac{1}{x}\right)} = \frac{3}{\frac{1}{9} + \frac{1}{9} + \frac{1}{9}} = \frac{3}{\frac{3}{9}} = \frac{27}{3} = 9$$

Ans

- If there are two groups containing n_1 and n_2 observations with respective harmonic means as H_1 and H_2 , the combined HM is given by-

$$HM = \frac{n_1 + n_2}{\frac{n_1}{H_1} + \frac{n_2}{H_2}}$$

eg. $n_1 = 75$ $n_2 = 65$ $H_1 = 15$ $H_2 = 13$

$$= \frac{15 + 13}{\frac{75}{15} + \frac{65}{13}} = \frac{28}{\frac{18}{5} + \frac{13}{13}} = \frac{28}{\frac{18}{5} + 1} = \frac{28}{\frac{18+5}{5}} = \frac{28 \times 5}{23} = \frac{140}{23} \approx 6.087$$

$$= \frac{28}{2.5} = \frac{140}{5} = 28$$

Ans

- The HM of $1, \frac{1}{2}, \frac{1}{3}, \dots, \frac{1}{n}$ is given by -

$$\frac{2}{n+1}$$

- In order to calculate average speed, use Harmonic mean. The HM of two numbers is given by -

$$\frac{2xy}{x+y}$$

eg. Exercise set B of Pg. 14 Pg. 11.27

$$x = 500 \quad y = 700$$

$$\text{Average Speed} = \frac{2xy}{x+y} = \frac{2 \times 500 \times 700}{500 + 700} = \frac{700000}{1200} \approx 583.33$$

$$\text{Or } HM = \frac{2}{\frac{1}{x} + \frac{1}{y}} = \frac{2}{\left(\frac{1}{500} + \frac{1}{700}\right)} = \frac{2}{0.00343} \approx 583.33$$

Ans

Relationship between AM, GM, HM

- If ques. asks about constant = AM = GM = HM observation, then
- If ques. asks about distinct = AM > GM > HM observations, then
- If ques. asks about rel. = AM > GM > HM between AM, GM, HM, then

eg. from Exercise Set B of 20 Pg. 14.27
 Answer is 15 because AM = GM = HM
 15 = 15 = 15

- $GM^2 = AM \times HM$
 → This relationship holds true only for positive observations.

eg. Set B of 7 Pg. 14.26

$$GM^2 = AM \times HM$$

$$GM^2 = 5 \times 3.2$$

$$GM = \sqrt{16}$$

$$GM = 4 \text{ Ans}$$

Partition values (Positional Averages)

- There are values such as medians, quartiles, decile and percentiles divides a given series into equal no. of parts
- median divides a series into 2 equal parts
- Quartile ————— 4 —————
- Decile ————— 10 —————
- Percentile ————— 100 —————

Median-

A median divides a series into two equal parts

eg. 2, 9, 4, 6, 10

First set in Ascending order - compulsory when find median

2, 4, 6, 9, 10
↓

6 is median because this divide a series into two equal parts

eg. 2, 4, 6, 9, 10, 12
↓

Take AM = $\frac{6+9}{2} = 7.5$ So, 7.5 is median

Rank - This is used to know the place of the no. like 1, 2, 3, 4. So, 1 is in the 1st rank + 2nd is in 2nd rank and so on.

eg. 2, 4, 6, 9, 10

formula of Rank = $\frac{n+1}{2} = \frac{5+1}{2} = \frac{6}{2} = 3$ Ans

- For the series of odd no.s
- For even no.s taking the middle two no.s + add them + divide by 2, their average is median

→ These all points work in individual series

Discrete series of Median -

- Arrange series into ascending order
- Calculate Cumulative frequency (CF always less than)
- Calculate the rank of the median as $\frac{n+1}{2}$ (N = total of freq.)
- Check the CF which is just greater than the Rank
- The value of x corresponding to this CF would be median.

eg. $\frac{x}{f}$ $\frac{F}{CF}$

Rank = $\frac{N+1}{2} = \frac{150+1}{2} = 75.5$

Median	20	40	90	→ CF greater than Rank
	30	10	150	
	40	30	130	
	50	20	150	
		150 = N		

So answer is 20
median

Continuous series median -

- Make sure that the series is exclusive
- Arrange the series in ascending order
- Calculate CF
- Calculate Rank as $\frac{N}{2}$
- Check the CF which is just greater than Rank
- The class interval corresponding to this cumulative freq. is known as median class interval

Median

~~is~~ is calculated by formula

$$\text{Median} = l + \frac{\text{Rank} - C}{f} \times i$$

Here,

- l is the lower limit of the median class interval
- C is the CF of the class interval preceding the median class interval
- f is the frequency of the median class interval.
- i is the class length of the median class interval.

eg. CI

CI	F	CF
349.5 - 369.5	23	23
369.5 - 389.5	38	61
389.5 - 409.5	58	119
409.5 - 429.5	82	201
429.5 - 449.5	65	266
449.5 - 469.5	31	297
469.5 - 489.5	11	308
	308 = N	

Rank = $\frac{N}{2} = \frac{308}{2} = 154$

\rightarrow is just greater than 154

\therefore Median = $l + \frac{\text{Rank} - C}{f} \times i$

$$= 409.5 + \frac{154 - 119}{82} \times 20$$

$$= 418.036$$

- Mean is affected due to change in ~~score~~ scale, as well as due to a change in origin.
- If two variables x and y are related as $y = a + bx$, where a and b are constants, and x_{me} is known, then $y_{me} = a + bx_{me}$

eg. Exercise. let B of 16 Pg. 14 & 24
 median of $x = 20$, median of y is $y = 2x - 3$
 $y = a + bx$
 $y = -3 + 2x$
 $y = -3 + 2 \times 20$
 $y = -3 + 40$
 $y = 37$ Aus

Imp.
 For a set of observations, the sum of absolute deviations is minimum when the deviations are calculated from median.

Quantile-

- A quantile divides a series into 4 equal parts.
- There are three quantiles Q_1, Q_2, Q_3



- Arrange series in ascending order
- Rank of $Q_1 = \frac{n+1}{4}$
- Rank of $Q_2 = 2 \times \text{Rank of } Q_1$

- Rank of $Q_3 = 3 \times \text{Rank of } Q_1$

eg. 50, 56, 65, 75, 75, 80, 82, 90, 120, 130
 $N = 10$

Rank = $\frac{n+1}{4} = \frac{10+1}{4} = \frac{11}{4} = 2.75 \Rightarrow$ this also written as $2 + 0.75$

We are finding Q_1 so, what less $+ 0.75$ (3rd term - 2nd term)
 $56 + 0.75 (65 - 56)$
 $56 + 6.75 = 62.75$ Ans

If any doubt about finding quartile then read down
Suppose Rank is 7.7

So, split it = $7 + 0.7$

Specific formula hai bata rahi kyuki wo unnecessary
h yaha se jese samajh sako bitkul
correct h

Quartile's Discrete Series -

- Arrange series in ascending order.
- Find cumulative frequency.
- Rank as same as in individual series Q_1, Q_2, Q_3
- Find the cumulative frequency just greater than the rank.
- The observation corresponding to this cumulative frequency is required quartile.

X	2	4	6	8	12
F	1	2	4	3	2
CF	1	3	7	10	12

$$\text{Rank of } Q_1 = \frac{N+1}{4} = \frac{12+1}{4} = 3.25$$

CF greater than rank

The observation corresponding to CF is 6 and it is quartile

Ans

Quartile ka continuous series

- Make sure that series is exclusive
- Arrange the series into ascending order.
- Find CF
- Rank of $Q_1 = \frac{N}{4}$, $Q_2 = 2 \times \text{Rank of } Q_1$, $Q_3 = 3 \times \text{Rank of } Q_1$
- Find the cumulative frequency just greater than the Rank
- The observation corresponding to this cumulative frequency is quartile class interval.

$$\text{Quartile Rank} = 1 + \frac{\text{Rank} - C}{f} \times i$$

eg. Pg. 14.29 Ex-6 Q. 6 (1)

Profit	RF	CF
-0.5-9.5	5	5
9.5-19.5	18	23
19.5-29.5	38	61
29.5-39.5	20	81
39.5-49.5	9	90
49.5-59.5	2	92
	92	

$$Q_1 = \frac{92}{4} = 23$$

$$Q_3 = 23 \times 3 = 69$$

$$Q_3 = J + \frac{R-C}{f} \times i$$

$$= 29.5 + \frac{69-61}{20} \times 10$$

$$= 33.5 \text{ in thousand}$$

$$\therefore, 33.5 \times 1000 = 33500 \text{ Ans}$$

Decile -

A decile divides a series into 10 equal parts

- Therefore, there are nine deciles $\rightarrow D_1, D_2, D_3, \dots, D_9$

Decile of individual series -

- Average the series in ascending or descending order

- Rank of $D_1 = \frac{n+1}{10}$ as same $D_2 = 2 \times D_1$ -----

eg. 50, 56, 65, 75, 80, 82, 90, 120, 130

$$D_1 = \frac{10+1}{10} = \frac{11}{10} = 1.1$$

assumed,

$$D_7 = 1.1 \times 7 = 7.7 = 7^{\text{th}} \text{ term} + 0.7 (8^{\text{th}} \text{ term} - 7^{\text{th}} \text{ term})$$

$$= 82 + 0.7(90 - 82)$$

$$82 + 5.6$$

$$D_7 = 87.6 \text{ Ans}$$

Discrete series - Decile

- Average the series in ascending order
- Find CF
- Rank of $D_1 = \frac{N+1}{10}$ ----- same -----
- Find the CF just greater than Rank.
- The observation corresponding to the CF is required Decile.
eg. same as quantile

Decile of continuous series -

- Make sure that series is exclusive
- Arrange the series in ascending order.
- Find CF
- Rank of $D_1 = \frac{N}{10}$ ————— same —————
- Find CF just greater than Rank.
- The observation corresponding to this CF is decile CI.

Percentile -

- It divides a series into 100 equal parts
- Therefore, there are 99 percentiles $P_1, P_2, P_3, \dots, P_{99}$

Individual series $\frac{N+1}{100}$ Discrete series $\frac{N+1}{100}$ Continuous $\frac{N}{100}$

eg. ~~82, 85, 90, 95~~ 50, 56, 65, 75, 75, 80, 82, 90, 120, 130
 $P_{82} = ?$

$$P_1 = \frac{10+1}{100} = \frac{11}{100} = 0.11$$

$$P_{82} = 0.11 \times 82 = 9.02$$

$$= 9^{\text{th}} + 0.02(10^{\text{th}} - 9^{\text{th}})$$

$$120 + 0.02(130 - 120)$$

$$120 + 0.2$$

$$= 120.20 \text{ Ans}$$

eg. Profit

F	CF	$P_1 = \frac{92}{100} = 0.92$
-0.5-9.5	5	
9.5-19.5	23	$P_{65} = 0.92 \times 65 = 59.8$
19.5-29.5	61	
29.5-39.5	81	$P_{65} = 19.5 + \frac{59.8 - 23}{38} \times 10$
39.5-49.5	90	
49.5-59.5	92	$29.184 \text{ in } 1000$

9.5-19.5 18 23

19.5-29.5 38 61

29.5-39.5 20 81

39.5-49.5 9 90

49.5-59.5 2 92

$N = 92$

$29.184 \text{ in } 1000$

$= 29.184$

Mode-

To value apke data me sabse jaada baar occur karta hai uska mode.

Mode of individual series-

It can be calculated by simple observation.

eg. 1) $\underline{25}, 20, \underline{25}, 35, \underline{25}, 15, 21, 19$
25 is mode

2) $\underline{9}, 12, \underline{20}, 17, \underline{20}, \underline{9}, 25$
20 + 9 is mode

3) $\underline{9}, 12, \underline{15}, \underline{15}, 12, \underline{9}, \underline{15}, \underline{9}, 12$

There is no mode because full series values are occurring in same quantity

Mode of discrete series-

- Mode of discrete series is the observations with the highest frequency.

eg.

x	f
5	25
7	35
9	45

So Ans is 9. because it occurs 45 times which is highest.

Mode of continuous series-

- make sure that series is exclusive
- Locate the class interval with highest frequency, that is the modal class interval.
- Mode is calculated by using this formula -

$$L + \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \times i$$

Here,

L = lower limit of modal class interval

f₁ = frequency

f₀ = frequency of the preceding class interval

f₂ = frequency of succeeding class interval

i = class length / class size

eg. Exercise, Set C (p. 3(2)) Pg. 1428

Profit	CF	F	
0-5	10	10	
5-10	25	15	f_0
10-15	45	20	f_1
15-20	55	10	f_2
20-25	62	7	
25-30	65	3	

Modal class = 10-15

$$f_0 = 15, f_1 = 20$$

$$f_2 = 10, h = 5$$

$$h = 10$$

$$\text{Mode} = h + \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \times h$$

$$= 10 + \frac{20 - 15}{2 \times 20 - 15 - 10} \times 5$$

$$= 10 + \frac{5}{15} \times 5$$

$$= 10 + \frac{5}{3} \times 1$$

$$= 11.66 \text{ Ans}$$

$$\text{In 000} = 11666$$

- Mode is affected due to change in scale, as well as due to change in origin.

$$y = a + bx$$

$$\bar{y} = a + b\bar{x}$$

$$y_{\text{med}} = a + bx_{\text{med}}$$

$$y_{\text{mo}} = a + bx_{\text{mo}}$$

- If two variables x and y are related as $y = a + bx$, where a and b are constants, and x_{mo} is known then $y_{\text{mo}} = a + bx_{\text{mo}}$

eg. $y = 2 + 1.50x$

mode of $x = 15$

So,

$$y = 2 + 1.50 \times 15$$

$$y = 2 + 22.5$$

$$y = 24.5 \text{ Ans}$$

Relationship between Mean, Median, Mode

Imp. • For symmetric data, mean = median = mode

Imp. • For skew-symmetric data (Moderately skewed data),

~~mean = median~~

$$\text{mean} - \text{mode} = 3(\text{mean} - \text{median}) \text{ or}$$

$$\text{mode} = 3\text{median} - 2\text{mean}$$

- For positively skewed data, $\text{mean} > \text{median} > \text{mode}$
- For negatively skewed data, $\text{mean} < \text{median} < \text{mode}$

Measures of Dispersion-

Dispersion means the scatteredness of the data

- Every measure of dispersion has a coefficient and it is always unit free measure.

Range - scatteredness of data

eg. 2, 4, 6, 8, 10, 15, 20

Simple h, human data 2 se dotak phelaku h to humani range, $20 - 2 = 18$ hai means hum 2 se 18 jada tak jaa sakte

- Range is calculated by subtracting the smallest observation of data from largest observation.

Individual series of Range-

- Make sure that series is in ascending order.
- $\text{Range} = \text{largest obs.} - \text{smallest obs.}$
- $\text{Coefficient of Range} = \frac{L - S}{L + S} \times 100$

eg. • 50, 52, 65, 70, 70, 75, 82, 96 Find Range & coefficient
 $\text{Range} = \text{largest obs.} - \text{smallest obs.}$
 $96 - 50 = 46$ Ans

$$\text{Coefficient of Range} = \frac{L - S}{L + S} \times 100 = \frac{96 - 50}{96 + 50} \times 100 = \frac{46}{146} \times 100$$

$$\text{Ans} = 31.51$$

Remember that this is unit free measure

(and as same as in discrete series)
 no need to explanation

Continuous Series of Range

- Make sure that the series is exclusive
- Range = Upper most class boundary - Lower most class boundary
- Coefficient of Range = $\frac{UMCB - LMCB}{UMCB + LMCB} \times 100$

In	Inclusive	Exclusive
ex-	0-9 10-19 20-29	eg. 0.5-9.5 9.5-19.5 19.5-29.5
	↓ ↓ ↓	↓ ↓ ↓
	Lower limit upper limit	Lower boundary upper boundary

eg. Weight

49.5-54.5

54.5-59.5

59.5-64.5

64.5-69.5

69.5-74.5

Find Range and its coefficient?

Range = $UMCB - LMCB$

$$= 74.5 - 49.5$$

$$= 25 Ans$$

Coefficient = $\frac{UMCB - LMCB}{UMCB + LMCB} \times 100$

$$= \frac{74.5 - 49.5}{74.5 + 49.5} \times 100$$

$$= \frac{25}{124} \times 100$$

$$= 20.16 Ans$$

- Dispersion are only effected with change in scale not from origin.
- Range is not affected change in origin.

eg. 2, 4, 6, 8, 10 Range = $10 - 2 = 8$ $\times 10$
 $\times 10 = 20, 40, 60, 80, 100$ Range = $100 - 20 = 80$

means scale change, same se Range change hoti h

eg. 2, 4, 6, 8, 10 Range = $10 - 2 = 8$ same
 $+2 = 4, 6, 8, 10, 12$ Range = $12 - 4 = 8$
 means origin se Range effect nai hota

- Range remains unaffected due to change in origin but affected in same ratio due to change in scale.
- If there are two variables x and y related to each other as $y = a + bx$ and Range of x is known then Range of y is given by $R_y = |b| \times R_x$ where $| |$ means modulus function

eg. Range of x is 2, then range of $-3x + 50$

$$y = -3x + 50$$

$$y = -3 \times 2$$

$$y = -6$$

$$y = 6$$

Mean Deviation -

- Mean deviation is the average of the absolute deviations from an appropriate measure of central tendency.
- This appropriate measure of central tendency could be mean, median or mode
- Coefficient of mean deviation = $\frac{\text{mean deviation about } A \times 100}{A}$ (A means mean)
- Here, A is the appropriate measure of central Tendency.

mean deviation means - deviation from mean
difference from mean

eg. 1, 2, 3, 4, 5, 6, 7, 8, 9

what is ^{coefficient of} mean deviation about a mean?

$$\text{mean} = \frac{45}{9} = 5$$

$$\text{mean deviation} = \frac{20}{9}$$

$$\text{Coefficient of M.D.} = \frac{\text{MD about } A \times 100}{A}$$

$$= \frac{20}{9/5} \times 100 = 44.44\%$$

Individual series -

$$\text{mean deviation} = \frac{\sum |x - \bar{x}|}{n}$$

Discrete series ka mean deviation -

$$\frac{\sum f |x - \bar{x}|}{N}$$

- Mean deviation remains unaffected due to change of origin but affected in the same ratio due to change in scale.
- If there are two variables x and y related to each other as $y = a + bx$, and mean deviation of x is known, the mean deviation of y is given by $MD_y = |b| \times MD_x$
- Mean deviation is minimum when the deviations are taken from median.

Standard deviation

- It is the square root of variance.

MD = Absolute deviation ka mean

Variance = Deviation ke squares ka mean

e.g. 2, 3, 4, 5 $\bar{x} = \frac{14}{4} = 3.5$

$$\text{variance} = \frac{(3.5-2)^2 + (3.5-3)^2 + (3.5-4)^2 + (3.5-5)^2}{4} = 1.25$$

- Standard deviation is the square root of variance.
- Variance is the average of square of deviation from mean.
- Coefficient of variation = $\frac{SD}{AM} \times 100$

$$SD = \sqrt{\frac{\sum (x - \bar{x})^2}{n}} \quad \text{or} \quad SD = \sqrt{\frac{\sum x^2}{n} - (\bar{x})^2}$$

Discrete series / Continuous series

$$SD = \sqrt{\frac{\sum f(x - \bar{x})^2}{N}} \quad \text{or} \quad SD = \sqrt{\frac{\sum f x^2}{N} - (\bar{x})^2}$$

- If all the observations assumed by a variable are constant, standard deviation is zero. This is true for Range, mean deviation and Quartile deviation.
- Standard deviation of first n natural no. is calculated as-

$$SD = \sqrt{\frac{n^2 - 1}{12}}$$

- Standard deviation of only two nos is given by $\frac{|a - b|}{2}$
- Standard deviation remains unaffected due to a change of origin but affected in the same ratio due to a change in scale. If there are two variables x and y related to each other as $y = a + bx$, + standard deviation of x is known, then standard deviation of y is given by $SD_y = |b| \times SD_x$

$$\text{Variance of } y = (SD_y)^2$$

- If there are two groups containing n_1 and n_2 observations with the respective means as \bar{x}_1 and \bar{x}_2 and standard as s_1 and s_2 , then the combined standard deviation is given by:

$$SD = \sqrt{\frac{n_1 s_1^2 + n_2 s_2^2 + n_1 d_1^2 + n_2 d_2^2}{n_1 + n_2}}$$

Here,

- $d_1 = \bar{x}_1 - \bar{x}$
- $d_2 = \bar{x}_2 - \bar{x}$

Quantile Deviation -

- $\text{Quantile deviation} = \frac{Q_3 - Q_1}{2}$
- $\text{Coefficient of quantile deviation} = \frac{Q_3 - Q_1}{Q_3 + Q_1} \times 100$
- In measure of dispersion, quantile deviation is best for open ended data.
- Most appropriate measures of central tendency is median for an open ended data or classification.