

- 1) Regression analysis aims establishing the average relationship between two variables.
- 2) It is used to predict unknown variable with the help of known variable.
- 3) There are two types are regression lines:
 - a) Regression line of x on y
 - b) Regression line of y on x

Feature	x on y	y on x
1) Regression line general form	$X = a + bY$	$Y = a + bX$
2) Dependent or Explained or Regressed	X	Y
3) Independent or Explanatory or Regressor	Y	X
4) Regression Equation	$X - \bar{X} = r \cdot \frac{\sigma_x}{\sigma_y} (Y - \bar{Y})$	$X - \bar{X} = r \cdot \frac{\sigma_y}{\sigma_x} (X - \bar{X})$
5) Regression Coefficient	$b_{XY} = r \cdot \frac{\sigma_x}{\sigma_y} = \frac{\text{COV}(X, Y)}{\sigma_y^2}$	$b_{YX} = r \cdot \frac{\sigma_y}{\sigma_x} = \frac{\text{COV}(X, Y)}{\sigma_x^2}$
6) Deviations from mean	$b_{xy} = \frac{\sum(x - \bar{x})(y - \bar{y})}{\sum(y - \bar{y})^2}$	$b_{yx} = \frac{\sum(x - \bar{x})(y - \bar{y})}{\sum(x - \bar{x})^2}$
7) No deviation	$b_{xy} = \frac{n \sum xy - \sum x \cdot \sum y}{n \sum y^2 - (\sum y)^2}$	$b_{yx} = \frac{n \sum xy - \sum x \cdot \sum y}{n \sum x^2 - (\sum x)^2}$
8) Deviation from assumed mean	$b_{xy} = \frac{n \sum dx \cdot dy - \sum dx \cdot \sum dy}{n \sum dy^2 - (\sum dy)^2}$	$b_{yx} = \frac{n \sum dx \cdot dy - \sum dx \cdot \sum dy}{n \sum dx^2 - (\sum dx)^2}$
9) Identification of regression equation by the value of $\left \frac{x \text{ coefficient}}{y \text{ coefficient}} \right $	Maximum	Minimum

PROPERTIES OF REGRESSION COEFFICIENTS:

- 1) The coefficient of correlation will have the same sign as that of regression coefficients. i.e., r , b_{YX} and b_{XY} will have same sign.

r	b_{YX}	b_{XY}
-	-	-
+	+	+
0	0	0

- 2) Arithmetic mean of regression coefficients is greater than the correlation coefficient i.e.,

$$\frac{b_{yx} + b_{xy}}{2} \geq r. \text{ [AM} \geq \text{GM]}$$

- 3) G.M of two Regression Coefficients is Correlation Coefficient i.e., $r = \pm \sqrt{b_{xy} \times b_{yx}}$

- 4) If one of the regression coefficients is greater than one other must be less than one i.e., $\sqrt{b_{xy} \cdot b_{yx}} \leq 1$

- 5) Regression Coefficients are Independent of change of Origin but not Scale.

$$\text{If } U = a + bx, V = c + dy \text{ then } b_{uv} = \frac{b}{d} \times b_{xy} \text{ and } b_{vu} = \frac{d}{b} \times b_{yx}$$

- 6) In case of perfect correlation, two regression coefficients are reciprocal to each other.

$$\text{i.e., if } r = \pm 1 \text{ then } r^2 = 1 \Rightarrow b_{yx} \cdot b_{xy} = 1 \Rightarrow b_{yx} = \frac{1}{b_{xy}}$$

$$\text{or } b_{xy} = \frac{1}{b_{yx}}$$

- 7) If $\sigma_x = \sigma_y$ then $r = b_{XY} = b_{YX}$.

- 8) Symmetry property does not hold i.e.,

$$b_{XY} \neq b_{YX}$$

PROPERTIES OF REGRESSION LINES:

If two lines of regression are coincided (Angle between the two lines is 0°)	$r = \pm 1$
If two regression lines are perpendicular (Angle between the two lines is 90°)	$r = 0$
Two regression lines meet at	(\bar{X}, \bar{Y})