

Chapter 5

Sequence & Series

 Arithmetic Progression
 Geometric Progression

⇒ Arithmetic progression. [AP]

 • diffⁿ of two consecutive terms is same.
 एक के बाद एक

 $a, a+d, a+2d, \dots$

1, 2, 3

 $(a-d), a, (a+d)$

$$t_n = a + (n-1)d$$

 $t_n = \text{last term} \rightarrow n^{\text{th}} \text{ term.}$
 $a = \text{1st term}$
 $n = \text{no. of terms}$
 $d = \text{common diff}^n$

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_n = \frac{n}{2} [a + l]$$

 $l = \text{last term.}$
 ~~$S_1 = a$~~

$$t_1 = S_1$$

 ~~$S_2 = a + (a+d)$~~

$$t_2 = S_2 - S_1$$

$$1\text{ ₹} = 100\text{ paise}$$

* term निकालने के लिये $\rightarrow t_n$ formula
* Sum निकालने के लिये $\rightarrow S_n$ formula

$$[A.M] \text{ Arithmetic Mean} = \frac{\text{1st term} + \text{last term}}{2}$$

$$AM = \frac{a+b}{2}$$

$$t_p = q$$

$$t_q = p$$

$$t_r = ?$$

$$t_r = p + q - r$$

$$t_m = n$$

$$t_n = m$$

$$t_r = ?$$

$$t_r = n + m - r$$

STAT

former $\rightarrow$ आगेवाला

Succeeding $\rightarrow$ आगेवाला
Preceding $\rightarrow$ पीछेवाला

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find numbers from 100 to 300 which are divisible by 7.

$$100 \xrightarrow{\div 7} 14.2$$

$\downarrow$ Perfect no. (नियत)

$$105 \leftarrow \times 7 \quad 15$$

$$300 \xrightarrow{\div 7} 42.85$$

$\uparrow$ Perfect no. (नियत)

$$294 \leftarrow \times 7 \quad 42$$

from
 $\rightarrow$ 1st & last
लेना है

Between

$\rightarrow$ only बीच वाले

00
~~400~~ ~~500~~ ~~600~~
divisible by 4 + by 5 - Common

and,
Common one only.

natural no. $\rightarrow$ 1 to ∞

whole no. $\rightarrow$ 0 to ∞

⇒ Geometric Progression [GP]

- ratio of two consecutive no will be constant
same

$$a, ar, ar^2, \dots$$

$$a, ar, ar^2, \dots$$

$$\frac{t_2}{t_1} = \frac{ar}{a} = r$$

$$1, 2, 4$$

$$\frac{a}{r}, a, ar$$

$$a, ar, ar^2$$

$$a, 2a, 4a$$

$$t_n = a \cdot r^{n-1}$$

$$t_n =$$

$$a = \text{1st no.}$$

$$r = \text{Common ratio}$$

$$n = \text{no. of terms}$$

$$S_n = \frac{a(r^n - 1)}{r - 1}$$

$$S_\infty = \frac{a}{1-r} \quad [r < 1]$$

[GM] Geometric Mean = $\sqrt{ab}$

$$\pm \sqrt{3} = 3\frac{1}{2}$$

$$x^2 - 1 \rightarrow (x-1)(x+1)$$

Sum of squares of natural no.

$$1^2, 2^2, 3^2, 4^2, \dots, n^2$$

$$\sum n^2 = S_n \Rightarrow \frac{n(n+1)(n+2)}{6}$$

Sum of cubes of natural no.

$$1^3, 2^3, 3^3, 4^3, \dots, n^3$$

$$\sum n^3 = S_n \Rightarrow \left[\frac{n(n+1)}{2} \right]^2$$

Sum of natural no.

$$1, 2, 3, 4, \dots, n$$

$$\sum n = n \Rightarrow \frac{n}{2} (n+1)$$