



Marathon 3

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NISH10

Schedule

Date (Day)	Topic
12-06-2023 (Monday)	Time Value of Money
13-06-2023 (Tuesday)	Logical Reasoning
14-06-2023 (Wednesday)	Measures of Central Tendency and Dispersion
15-06-2023 (Thursday)	Ratio, Proportion, Indices, Logarithms; Linear Inequalities
16-06-2023 (Friday)	Equations; Statistical Description of Data
17-06-2023 (Saturday)	Sequence and Series
18-06-2023 (Sunday)	Sets, Relations, and Functions
19-06-2023 (Monday)	Correlation and Regression
20-06-2023 (Tuesday)	Index Numbers
21-06-2023 (Wednesday)	Permutations and Combinations
22-06-2023 (Thursday)	Probability
23-06-2023 (Friday)	Theoretical Distributions

Highlights



Conceptual Revision



Question Based Revision



Last Day Preparation Tips



Questions to Revise on the
day before ExamQuizzes

Chapter 14 – Measures of Central Tendency and Dispersion

Measures of Central Tendency and Dispersion

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graph TD; A[Measures of Central Tendency and Dispersion] --> B[Measures of Central Tendency]; A --> C[Measures of Dispersion];
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Measures of Central Tendency

Measures of Dispersion

Measures of Central Tendency

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graph TD; A[Measures of Central Tendency] --> B[Mean (Mathematical Averages)]; A --> C[Partition Values (Positional Averages)]; A --> D[Mode];
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Mean
(Mathematical Averages)

Partition Values
(Positional Averages)

Mode

Mean (Mathematical Averages)

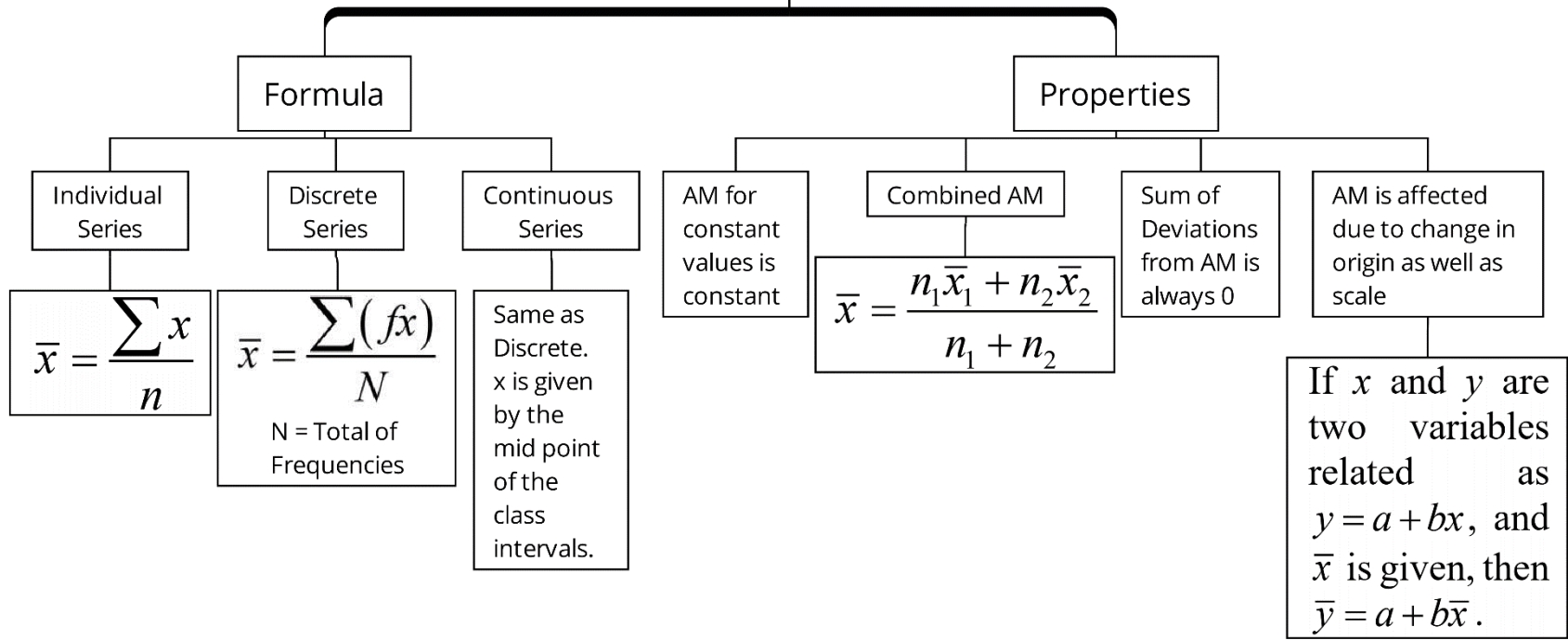
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graph TD; A["Mean (Mathematical Averages)"] --- B["Arithmetic Mean"]; A --- C["Geometric Mean"]; A --- D["Harmonic Mean"];
```

Arithmetic Mean

Geometric Mean

Harmonic Mean

Arithmetic Mean



Questions Based on Arithmetic Mean

Question 1 – ICAI SM

Find the mean from the following data:

Marks	Less than 10	Less than 20	Less than 30	Less than 40	Less than 50
No. of Students	5	13	23	27	30

(a) 19

(b) 20.45

(c) 21.12

(d) 22.33

Question 2 – ICAI SM

If there are 3 observations 15, 20, 25, then the sum of deviation of the observations from their AM is:

(a) 0

(b) 5

(c) -5

(d) None

Question 3 – ICAI SM

If the relationship between two variables u and v are given by $2u + v + 7 = 0$ and if the AM of u is 10, then the AM of v is:

(a) 17

(b) -17

(c) -27

(d) 27

Question 4 – ICAI SM

The average salary of a group of unskilled workers is ₹10,000 and that of a group of skilled workers is ₹15,000. If the combined salary is ₹12,000, then what is the percentage of skilled workers?

(a) 40%

(b) 50%

(c) 60%

(d) None

Question 5 – MTP November, 2021

At ABC ltd, the average age of employees is 36. Average age of male employees is 38 and that of females is 32. Find the ratio of female to male in the company.

(a) 1 : 3

(b) 2 : 1

(c) 1 : 2

(d) 3 : 1

Question 6 – MTP November, 2018

If the mean of a set of observations $x_1, x_2, x_3, \dots, x_n$ is \bar{x} , then the mean of the observations $x_i + ki$, where $i = 1, 2, 3, \dots, n$ is:

(a) $\bar{x} + k(n+1)$

(b) $\bar{x} + kn$

(c) $\bar{x} + \frac{k}{n}$

(d) $\bar{x} + \frac{k}{2}(n+1)$

Question 7 – PYQ

Two years ago, a team of four persons had an average age of 14. Now, a new member is added to the team and the average age of the team is 17. What is the age of the new member?

(a) 17

(b) 19

(c) 21

(d) 23

Question 8 – MTP June, 2013

The students of a class X^{th} have an average weight of 50 kg. The strength of the class is 49 students. On including the weight of the Principal, the average weight shoots up by 0.8 kg. Find the weight of the Principal.

(a) 75

(b) 90

(c) 85

(d) None

Question 9 – MTP June, 2013

The average of $(p + q)$ consecutive numbers starting from 1 is 'r'. If 's' is added to each of the numbers then the new average will be?

- (a) $r + s$ (b) $r + (s / 2)$ (c) $\{r + (p + q + s)\} / (p + q)$ (d) None

Question 10 – MTP June, 2013

The average weight of 40 people is increased by 2.4 kg when one man weight 73 kg is replaced by another man. Find the weight of the new man?

(a) 121

(b) 169

(c) 154

(d) 149

Question 11 – MTP June, 2013

The average salary of the whole employees in a company is ₹400 per day. The average salary of officers is ₹800 per day and that of clerks is ₹320 per day. If the number of officers is 40, then find the number of clerks in the company?

(a) 50

(b) 100

(c) 150

(d) 200

Question 12 – MTP June, 2013

The average of 6 numbers is 30. If the average of the first four is 25 and that of the last three is 35, the fourth number is:

(a) 25

(b) 30

(c) 35

(d) 40

Question 13 – MTP June, 2013

A student's marks were wrongly entered as 85 instead of 45. Due to that, the average marks for the whole class got increased by one-fourth. The no. of students in the class is:

(a) 80

(b) 160

(c) 40

(d) 20

Question 14 – MTP June, 2013

The mean of 100 observations is 50. If one of the observations which was 50 is replaced by 40, the resulting mean will be:

(a) 40

(b) 49.90

(c) 50

(d) None

Question 15 – MTP June, 2013

The mean annual salary of all employees in a company is ₹25,000. The mean salary of male and female employees is ₹27,000 and ₹17,000 respectively. Find the percentage of males and females employed by the company:

- (a) 60% and 40% (b) 70% and 25% (c) 70% and 30% (d) 80% and 20%

Geometric Mean

Formula

Individual Series

$$(x_1 \times x_2 \times \dots \times x_n)^{1/n}$$

Discrete Series

$$(x_1^{f_1} \times x_2^{f_2} \times \dots \times x_n^{f_n})^{1/N}$$

Properties

GM for constant values is constant

$$\log G = \frac{1}{r} \sum \log x$$

Here, r is the number of observations

To calculate average RATE, use GM

If $z = xy$, then
 $GM(z) = GM(x) * GM(y)$

If $z = x/y$, then
 $GM(z) = GM(x)/GM(y)$

Questions Based on Geometric Mean

Question 16 – ICAI SM

What is the GM for the numbers 8, 24 and 40?

(a) 24

(b) 12

(c) $8\sqrt[3]{15}$

(d) 10

Question 17 – ICAI SM

If GM of x is 10 and GM of y is 15, then the GM of xy is:

- (a) 150 (b) $\log 10 \times \log 15$ (c) $\log 150$ (d) None

Question 18

If GM of x is 10, and GM of y is 15, then GM of x/y is:

(a) 150

(b) $2/3$

(c) $\log 2/\log 3$

(d) None

Question 19 – MTP November, 2021

If the rates return from three different shares are 100%, 200% and 400% respectively. The average rate of return will be:

(a) 350%

(b) 233.33%

(c) 200%

(d) 300%

Question 20 – MTP November, 2018

The geometric mean of the series $1, k, k^2, \dots, k^n$, where k is a constant is:

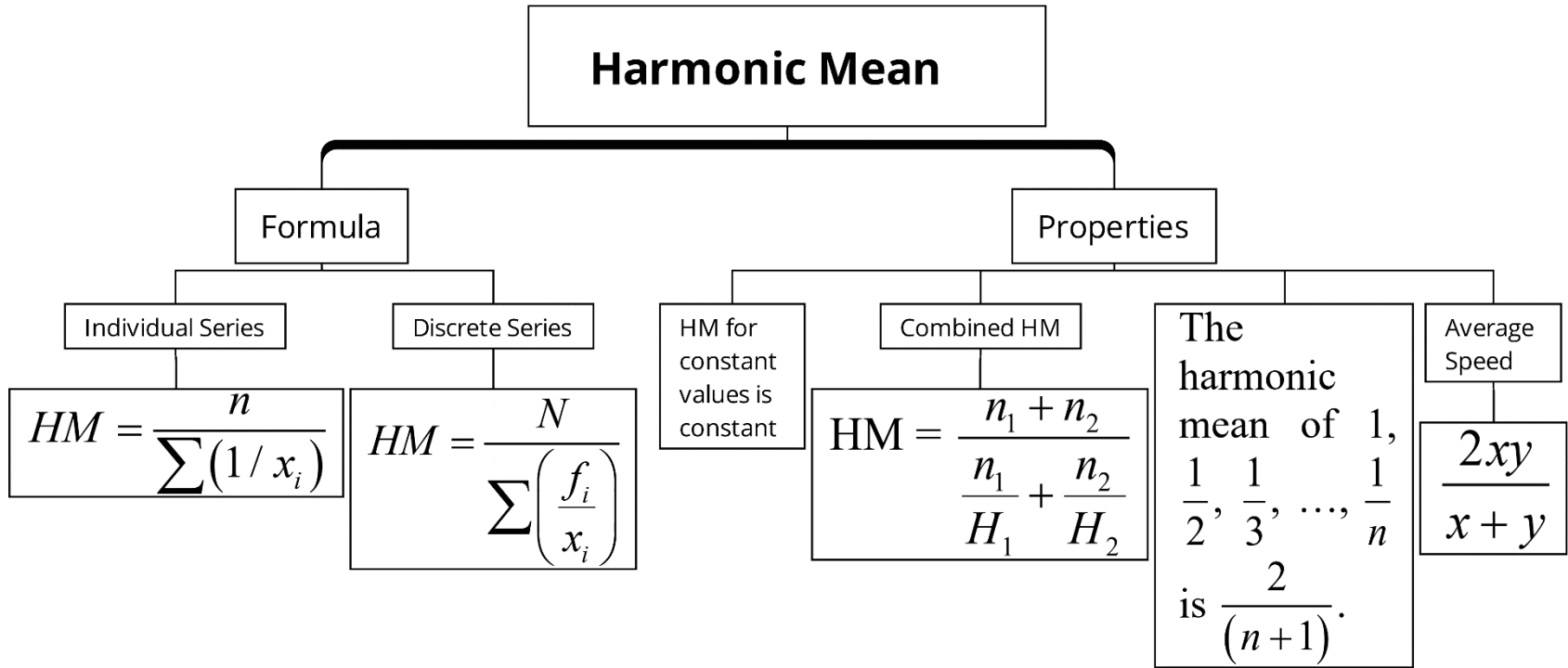
(a) $k^{(n+1)/2}$

(b) $k^{n+0.5}$

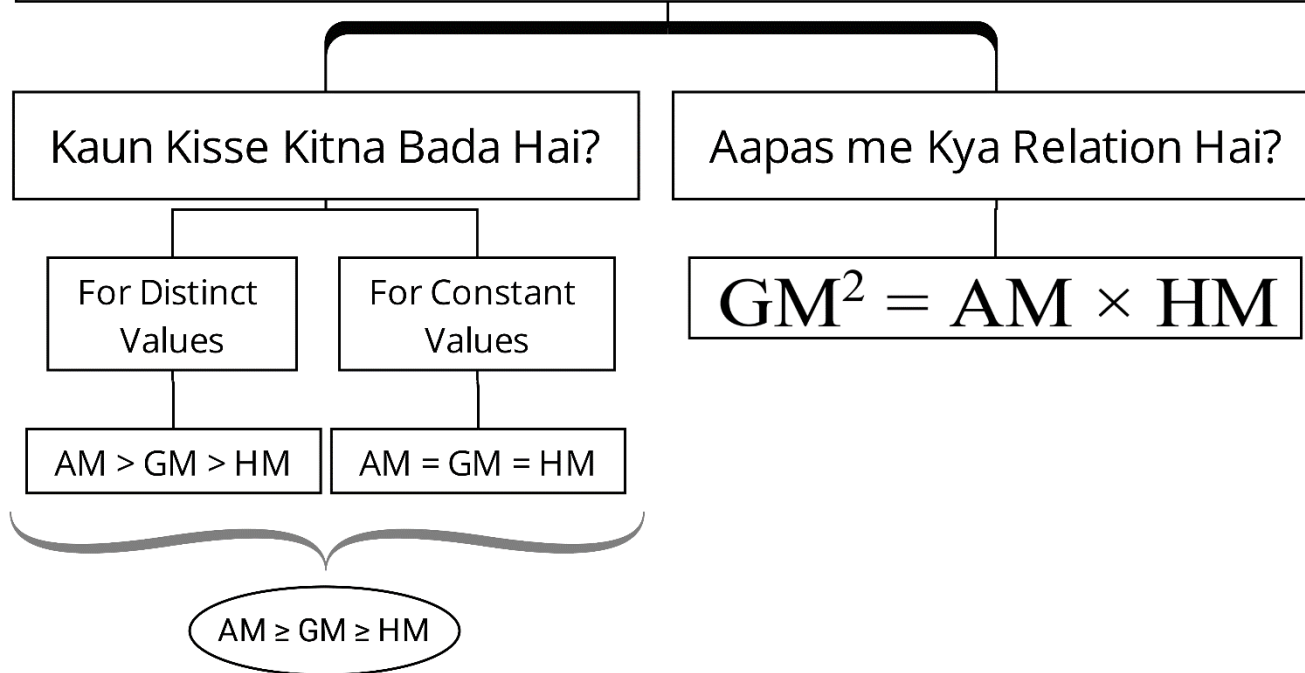
(c) k^{n+1}

(d) $k^{n/2}$

Harmonic Mean



Relationship between AM, GM, HM



Questions Based on Harmonic Mean

Question 21 – ICAI SM

Compute the HM for the numbers 6, 8, 12, 36.

(a) 9.93

(b) 5.77

(c) 6.77

(d) None

Question 22 – ICAI SM

If there are two groups with 75 and 65 as harmonic means and containing 15 and 13 observations then the combined HM is given by:

(a) 65

(b) 70.36

(c) 70

(d) 71

Question 23 – ICAI SM

An aeroplane flies from A to B at the rate of 500 km/hour and comes back from B to A at the rate of 700 km/hour. The average speed of the aeroplane is:

(a) 600 km per hour

(b) 583.33 km per hour

(c) $10\sqrt{35}$ km per hour

(d) 620 km per hour

Question 24 – ICAI SM

If the AM and HM for two numbers are 5 and 3.2 respectively then the GM will be

(a) 16.00

(b) 4.10

(c) 4.05

(d) 4.00

Question 25 – MTP June, 2013

AM and GM are both negative values, HM is equal to:

(a) $H = \frac{G}{A^2}$

(b) $H = \frac{G^2}{A}$

(c) $H = \frac{G^2}{\sqrt{A}}$

(d) None

Partition Values – Summary of Formulae

Partition Value	No. of Parts	No. of Partition Values	Symbol	Rank for Individual Series	Rank for Discrete Series	Rank for Continuous Series
Median	2	1	M	$\frac{n+1}{2}$	$\frac{N+1}{2}$	$\frac{N}{2}$
Quartile	4	3	Q_1 to Q_3	$Q_1 = \frac{n+1}{4},$ $Q_3 = \frac{3(n+1)}{4}$	$Q_1 = \frac{N+1}{4},$ $Q_3 = \frac{3(N+1)}{4}$	$Q_1 = \frac{N}{4},$ $Q_3 = \frac{3N}{4}$

Decile	10	9	D_1 to D_9	$D_1 = \frac{n+1}{10}$, $D_5 = \frac{5(n+1)}{10}$ and so on...	$D_1 = \frac{N+1}{10}$, $D_5 = \frac{5(N+1)}{10}$ and so on...	$D_1 = \frac{N}{10}$, $D_5 = \frac{5N}{10}$ and so on...
Percentile	100	99	P_1 to P_{99}	$P_1 = \frac{n+1}{100}$, $P_5 = \frac{5(n+1)}{100}$ and so on...	$P_1 = \frac{N+1}{100}$, $P_5 = \frac{5(N+1)}{100}$ and so on...	$P_1 = \frac{N}{100}$, $P_5 = \frac{5N}{100}$ and so on...

The formula for any partition value of a continuous series is $l + \frac{\text{Rank} - c}{f} \times i$

Property of a Median/Quartile/Decile/Percentile

If x and y are two variables related by $y = a + bx$ for any two constants a and b , then the median of y is given by $y_{me} = a + bx_{me}$.

Questions Based on Median

Question 26

What is the median for the following observations?

5, 8, 6, 9, 11, 4

(a) 6

(b) 7

(c) 8

(d) None

Question 27

Find the median of the following data:

Variable (x)	10	50	40	30	20
Frequency (f)	50	20	30	10	40

(a) 20

(b) 30

(c) 40

(d) None

Question 28 – ICAI SM

What is the value of median for the following data?

Marks	5 – 14	15 – 24	25 – 34	35 – 44	45 – 54	55 – 64
No. of Students	10	18	32	26	14	10

(a) 28

(b) 30

(c) 32.94

(d) 33.18

Question 29 – MTP May, 2020

Two variables x and y are given by $y = 2x - 3$. If the median of x is 20, what is the median of y ?

(a) 20

(b) 40

(c) 37

(d) 35

Questions Based on Quartiles

Question 30 – ICAI SM

What is the value of the first quartile for observations 15, 18, 10, 20, 23, 28, 12, 16?

(a) 17

(b) 16

(c) 12.75

(d) 12

Question 31 – ICAI SM

The third quartile for the following data are:

Profits in '000 ₹	Less than 10	10 – 19	20 – 29	30 – 39	40 – 49	50 – 59
No. of Firms	5	18	38	20	9	2

(a) ₹33,500

(b) ₹33,000

(c) ₹33,600

(d) ₹33,250

Questions Based on Decile

Question 32 – ICAI SM

The third decile for the numbers 15, 10, 20, 25, 18, 11, 9, 12 is:

(a) 13

(b) 10.70

(c) 11

(d) 11.50

Question 33 – ICAI SM

Following distribution relates to the distribution of monthly wages of 100 workers. Compute D_7 .

Profits in '000 ₹	Less than 500	500 – 699	700 – 899	900 – 1099	1100 – 1499	More than 1500
No. of Firms	5	23	29	27	10	6

(a) ₹1,032.83

(b) ₹1,048.96

(c) ₹995.80

(d) None

Questions Based on Percentile

Question 34 – ICAI SM

Following are the wages of the labourers: ₹82, ₹56, ₹90, ₹50, ₹120, ₹75, ₹75, ₹80, ₹130, ₹65. Find P_{82} .

(a) 62.75

(b) 81.20

(c) 120.20

(d) None

Question 35 – ICAI SM

The 65th percentile for the following data are:

Profits in '000 ₹	Less than 10	10 – 19	20 – 29	30 – 39	40 – 49	50 – 59
No. of Firms	5	18	38	20	9	2

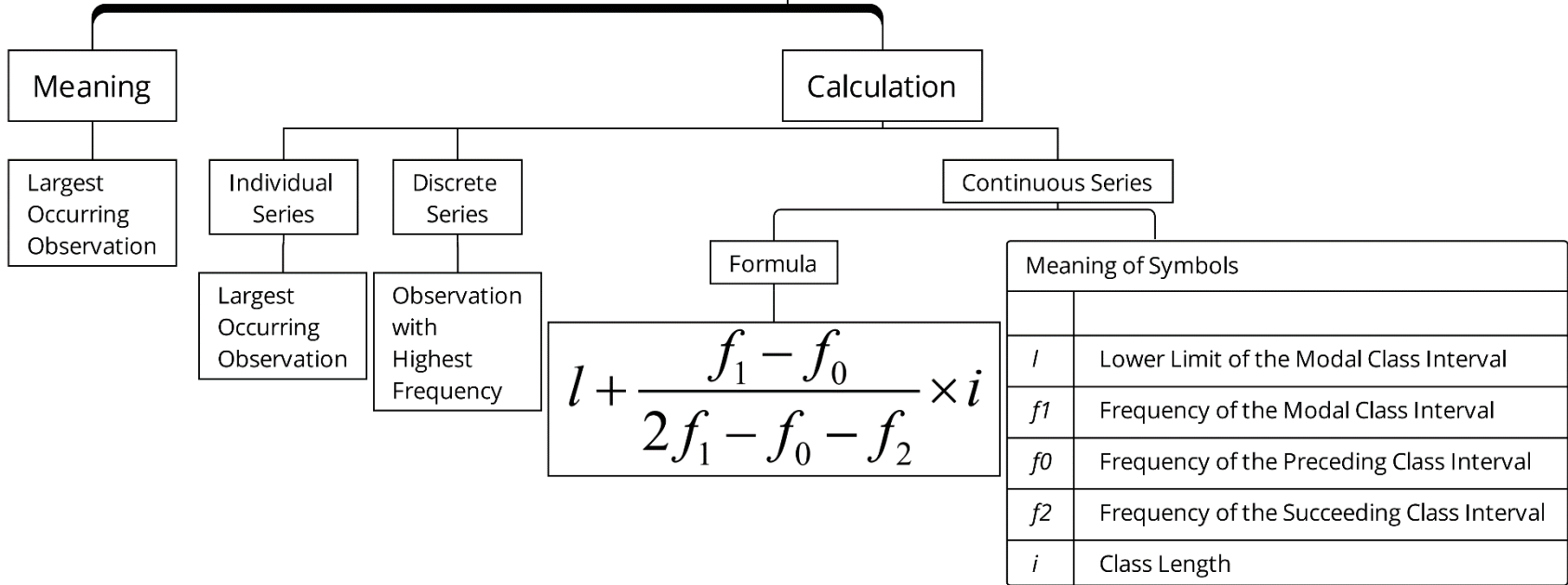
(a) ₹29,000

(b) ₹28,680

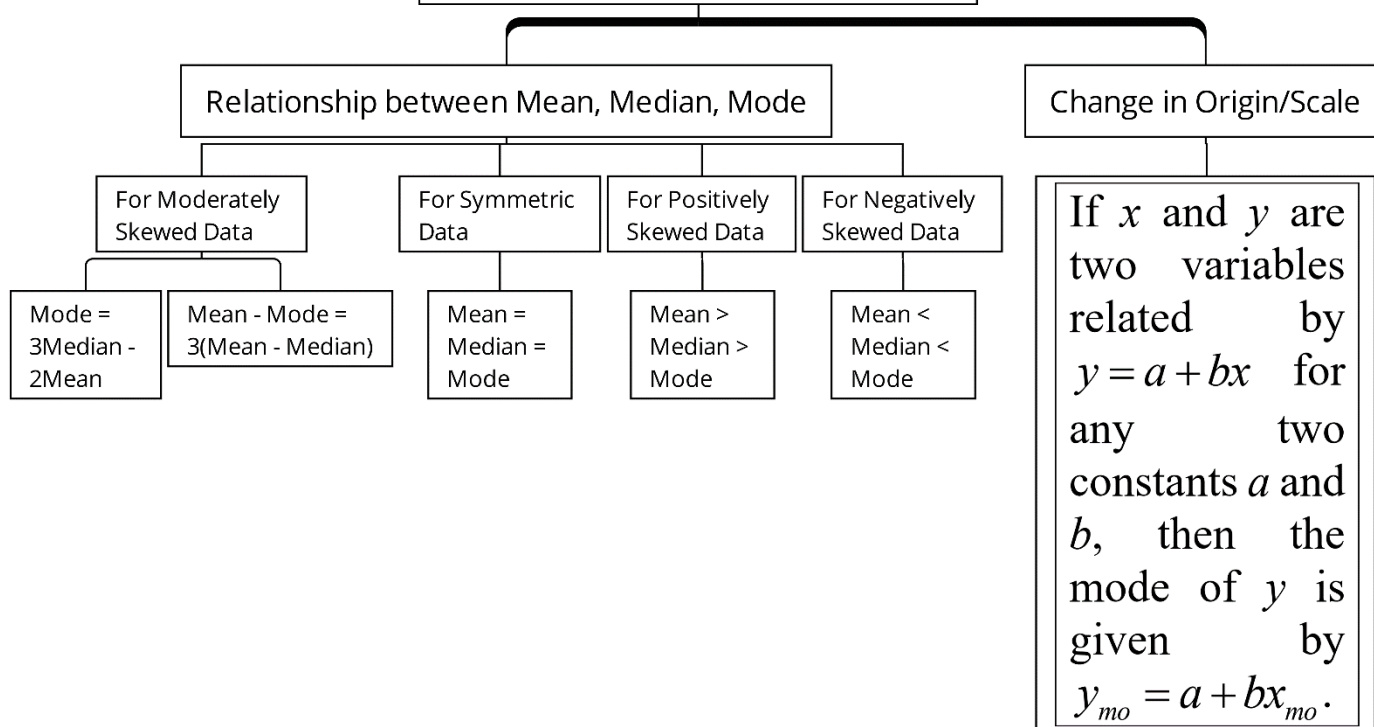
(c) ₹29,184

(d) ₹29,250

Mode



Properties of Mode



Questions Based on Mode

Question 36 – ICAI SM

The modal profits for the following data is:

Profit in ₹ '000	Below 5	Below 10	Below 15	Below 20	Below 25	Below 30
No. of Firms	10	25	45	55	62	65

(a) 11.50

(b) ₹11267

(c) ₹11667

(d) 11.67

Question 37 – ICAI SM

If $y = 2 + 1.50x$, and mode of x is 15, what is the mode of y ?

(a) ₹64.00

(b) 24.50

(c) ₹63.21

(d) ₹64.25

Question 38 – ICAI SM

For a moderately skewed distribution of marks in statistics for a group of 200 students, the mean mark and median mark were found to be 55.60 and 52.40. What is the modal mark?

(a) 20

(b) 13

(c) 46

(d) 23

Question 39 – PYQ

Given that for a distribution, the mean, median and mode are 23, 24, and 25.5. It is most likely that the distribution is _____ skewed.

- (a) Positively (b) Symmetrically (c) Asymptotically (d) Negatively

Question 40 – MTP June, 2013

Which of the following is the correct relation between mean, median and mode?

(a) $\text{Median} = \text{Mode} + \frac{2}{3}(\text{Mean} - \text{Mode})$

(b) $2\text{Mean} = \text{Mode} - 3\text{Median}$

(c) $2\text{Mean} = \text{Mode} + 3\text{Median}$

(d) $\text{Mode} = 3\text{Median} + 2\text{Mean}$

Question 41 – MTP June, 2013

If mean (\bar{x}) is 10, and mode (z) is 7, find out the value of median (M).

(a) 9

(b) 17

(c) 3

(d) 4.33

Measures of Dispersion

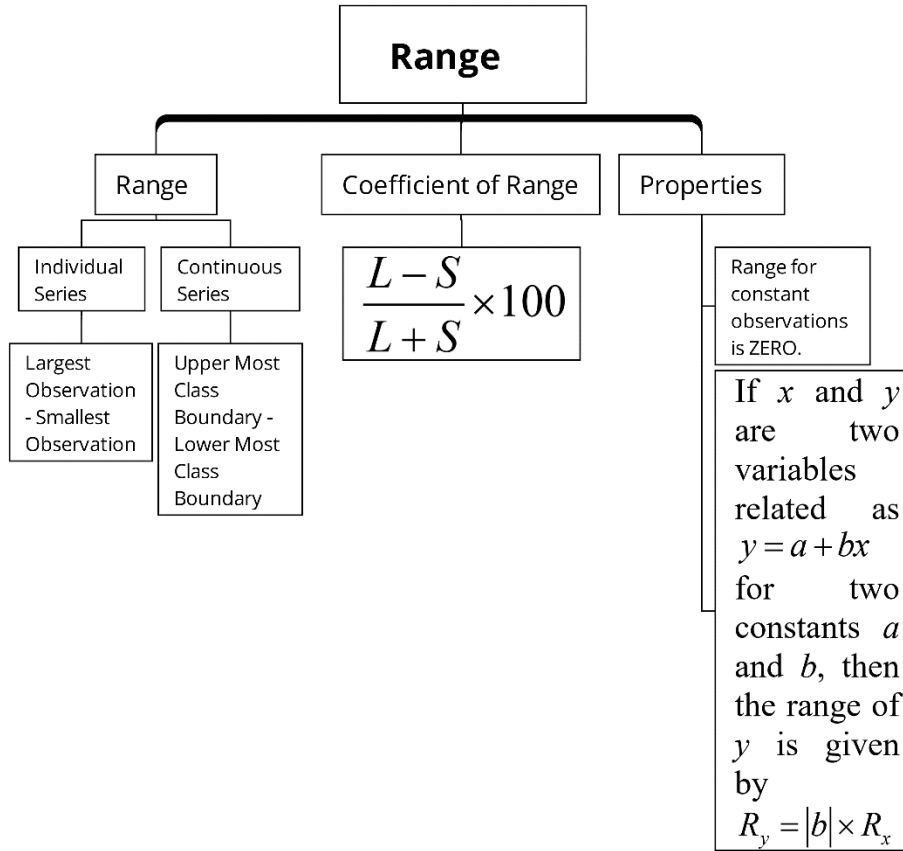
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graph TD; A[Measures of Dispersion] --> B[Range]; A --> C[Mean Deviation]; A --> D[Standard Deviation]; A --> E[Quartile Deviation];
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Range

Mean Deviation

Standard Deviation

Quartile Deviation



Questions Based on Range

Question 42 – ICAI SM

What is the coefficient of range for the following wages of 8 workers?

₹80, ₹65, ₹90, ₹60, ₹75, ₹70, ₹72, ₹85.

(a) ₹30

(b) ₹20

(c) 30

(d) 20

Question 43 – ICAI SM

What is the coefficient of range for the following distribution?

Class Interval	10 – 19	20 – 29	30 – 39	40 – 49	50 – 59
Frequency	11	25	16	7	3

(a) 22

(b) 50

(c) 72.46

(d) 75.82

Question 44 – ICAI SM

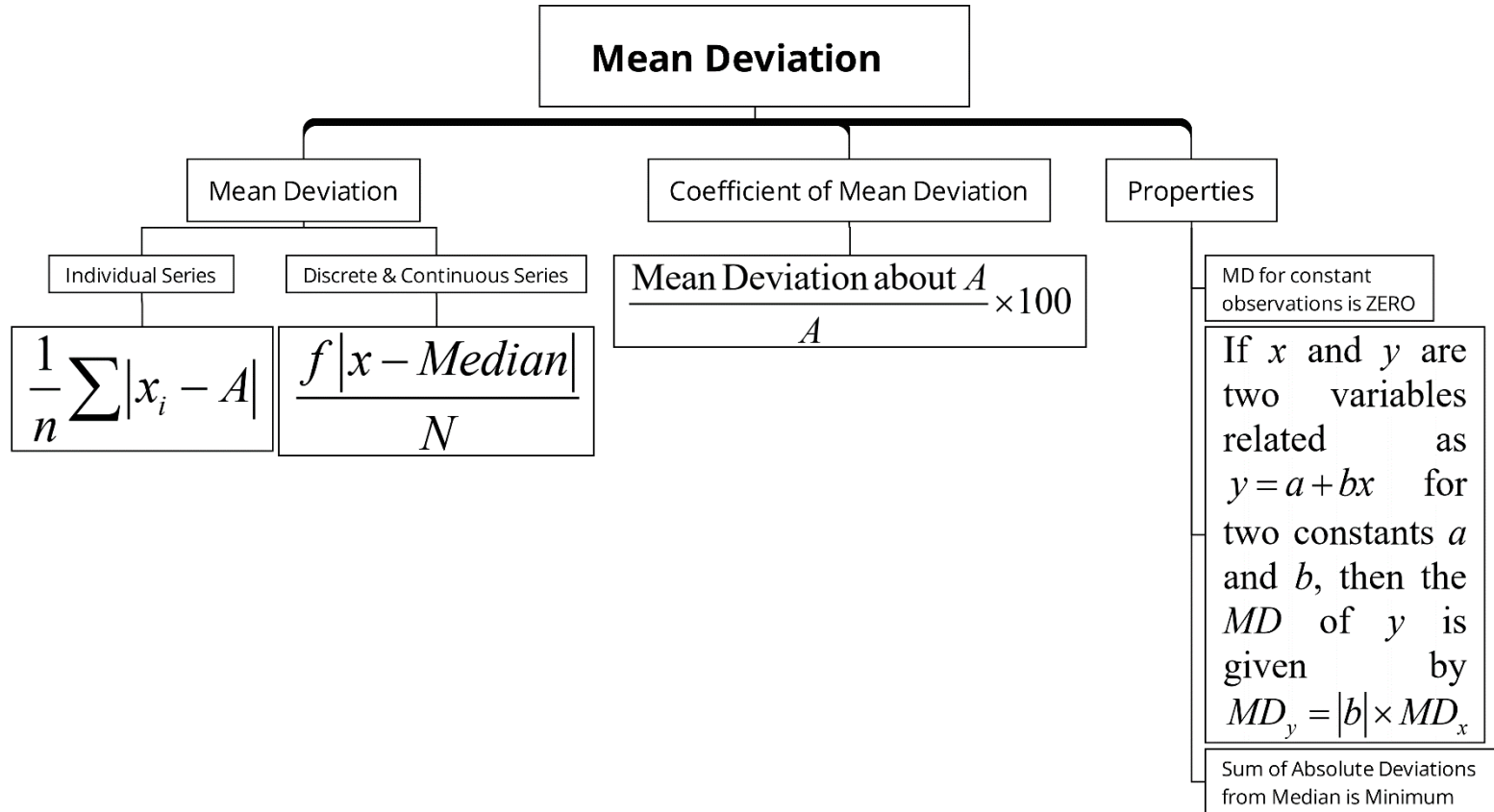
If the relationship between x and y is given by $2x + 3y = 10$, and the range of x is ₹15, what would be the range of y ?

(a) ₹20

(b) ₹5

(c) ₹15

(d) ₹10



Questions Based on Mean Deviation

Question 45

The mean deviation about mode for the numbers

$4/11, 6/11, 8/11, 9/11, 12/11, 8/11$ is:

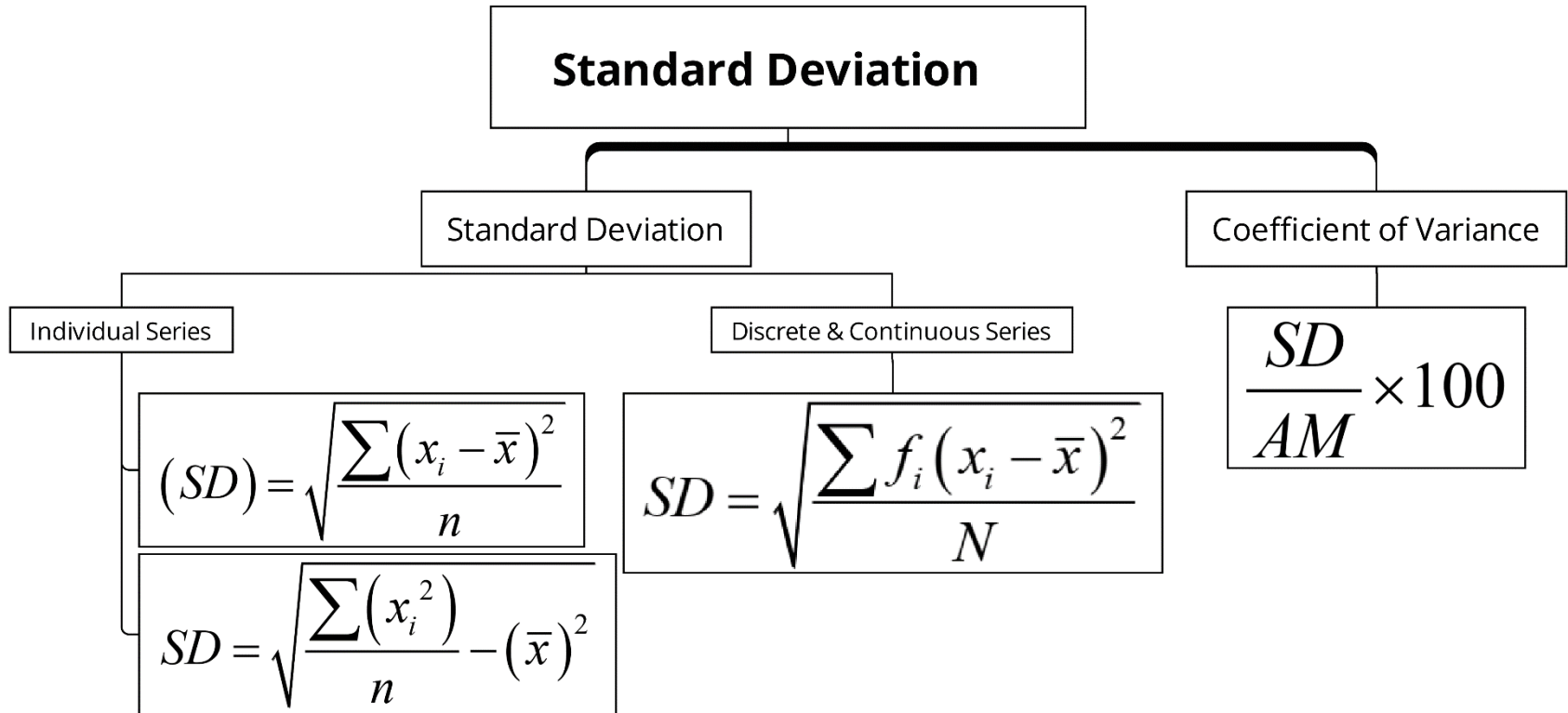
(a) $1/6$

(b) $1/11$

(c) $6/11$

(d) $5/11$

Standard Deviation



Properties of Standard Deviation

SD for constant observations is ZERO

If x and y are two variables related as $y = a + bx$ for two constants a and b , then the SD of y is given by $SD_y = |b| \times SD_x$

For any two numbers a and b , standard deviation is given by $\frac{|a-b|}{2}$

For the first n natural numbers, standard deviation is given by $\sqrt{\frac{n^2-1}{12}}$.

Combined Standard Deviation

$$SD = \sqrt{\frac{n_1 s_1^2 + n_2 s_2^2 + n_1 d_1^2 + n_2 d_2^2}{n_1 + n_2}}$$

where,

$$d_1 = \bar{x}_1 - \bar{x}$$

$$d_2 = \bar{x}_2 - \bar{x}$$

$$\bar{x} = \frac{n_1 \bar{x}_1 + n_2 \bar{x}_2}{n_1 + n_2}$$

Questions Based on Standard Deviation

Question 47 – ICAI SM

What is the coefficient of variation of the following numbers?

53, 52, 61, 60, 64.

(a) 8.09

(b) 18.08

(c) 20.23

(d) 20.45

Question 48 – ICAI SM

A student computes the AM and SD for a set of 100 observations as 50 and 5 respectively. Later on, she discovers that she has made a mistake in taking one observation as 60 instead of 50. What would be the correct mean and SD if the wrong observation is replaced by the correct observation?

(a) 49.90; 6.91

(b) 49.40; 4.91

(c) 49.90; 4.90

(d) None

Question 49 – ICAI SM

If the SD of the first n natural numbers is 2, then the value of n must be:

(a) 2

(b) 7

(c) 6

(d) 5

Question 50 – ICAI SM

If AM and coefficient of variation of x are 10 and 40 respectively, what is the variance of $15 - 2x$?

(a) 8

(b) 64

(c) 74

(d) None

Question 51 – ICAI SM

If the mean and standard deviation of x are a and b respectively, then the SD of $\frac{x-a}{b}$ is:

(a) -1

(b) 1

(c) ab

(d) a/b

Question 52 – ICAI SM

If x and y are related by $2x + 3y + 4 = 0$ and SD of x is 6, then SD of y is:

(a) 22

(b) 4

(c) $\sqrt{5}$

(d) 9

Question 53 – ICAI SM

If two samples of sizes 30 and 20 have means as 55 and 60 and variances as 16 and 25 respectively, then what would be the SD of the combined sample of size 50?

(a) 5.00

(b) 5.06

(c) 5.23

(d) 5.35

Question 54 – ICAI SM

The standard deviation is independent of change of:

- (a) Scale (b) Origin (c) Both (a) and (b) (d) None

Question 55 – ICAI SM

The best statistical measure used for comparing two series is:

- (a) Mean Deviation (b) Range (c) Coefficient of Variation (d) Standard Deviation

Question 56 – MTP May, 2021

If sum of squares of the values = 3390, $N = 30$ and standard deviation = 7, find out the mean.

(a) 113

(b) 210

(c) 8

(d) None

Question 57 – MTP May, 2021

The standard deviation of 10, 16, 10, 16, 10, 10, 16, 16 is:

(a) 4

(b) 6

(c) 3

(d) 0

Question 58 – MTP May, 2021

The of mean and SD of a series is $a + b$, if we add 2 to each observation of the series then the sum of the mean and SD will be:

(a) $a + b + 2$

(b) $6 - a + b$

(c) $4 + a - b$

(d) $a + b + 4$

Question 59 – MTP June, 2013

There are two startups in ecommerce sector struggling to acquire the market. Following data is for Mean and Standard Deviation of billing amount of bought items per month on their website:

Startup	No. of Customers/Month	Mean Billing Amount	SD of Billing Amount
A	40	₹2,500	₹10
B	30	₹2,200	₹11

Which startup has a better consistency when it comes to sales numbers?

- (a) Startup A (b) Startup B (c) Both A and B (d) Need More Information

Question 60 – MTP June, 2013

If the coefficient of variation and standard deviation are 60 and 12 respectively, then the arithmetic mean of the distribution is:

(a) 40

(b) 36

(c) 20

(d) 19

Question 61 – MTP June, 2013

If the sum of square of the value equals to 3390, number of observations are 30 and Standard deviation is 7, what is the mean value of the above observation?

(a) 14

(b) 11

(c) 8

(d) 5

Question 62 – MTP June, 2013

If the variance of random variable x is 18, then what is variance of $y = 2x + 5$?

(a) 34

(b) 39

(c) 68

(d) 72

Question 63 – MTP June, 2013

In a given set, if all data are of same value, then variance would be:

- (a) 0 (b) 1 (c) -1 (d) 0.5

Quartile Deviation

Quartile Deviation

Individual, Discrete,
Continuous Series

$$QD = \frac{Q_3 - Q_1}{2}$$

Coefficient of Quartile Deviation

$$\frac{Q_3 - Q_1}{Q_3 + Q_1} \times 100$$

Properties

If x and y are two variables related as $y = a + bx$ for two constants a and b , then the QD of y is given by

$$QD_y = |b| \times QD_x$$

Questions Based on Quartile Deviation

Question 64 – ICAI SM

The quartiles of a variable are 45, 52 and 65 respectively. Its quartile deviation is:

(a) 10

(b) 20

(c) 25

(d) 8.30

Question 65 – MTP June, 2013

In the equation $4x + 2y = 3$, quartile deviation for y is 3. Find the quartile deviation for x .

(a) 4.5

(b) 6

(c) 1.5

(d) None

Question 66 – ICAI SM

The mean and SD for a , b , and 2 are 3 and $\frac{2}{\sqrt{3}}$ respectively. The value of ab would be?

(a) 5

(b) 6

(c) 11

(d) 3

Question 67 – ICAI SM

Which one is an absolute measure of dispersion?

- (a) Range (b) Mean Deviation (c) Standard Deviation (d) All these measures

Question 68 – MTP June, 2013

If Quartile deviation is 7, find the value of x from the arranged series: 2, x , 6, 7, 9, 16, 18.

(a) 5

(b) 2

(c) 8

(d) 6