CA-FOUNDATION BUSINESS MATHEMATICS, STATISTICS & LOGICAL REASONING

Revise all Formulas at a Glance

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BUSINESS MATHEMATICS CHART BY MAYANK MAHESHWARI

INDICES	LOGARITHMS	RATIO	PROPORTION	EQUATIONS
• a x a x a x upto n terms = a ⁿ	• $\log_a 1 = 0$ (where a $\neq 0$)	• Ratio = $\frac{a}{-}$ or a : b where b $\neq 0$	• Equality of two ratios is called	• An equation of degree 1 is called
where a = Base	• $\log_a a = 1$	h	proportion.	linear equation
where n = the index of power	• $\log_a a^x = x$	where, a = First term or Antecedent	If a. b. c. d are said to be in	• An equation of degree 2 is called
• $a^{-m} = 1/a^{m}$ and $1/a^{-m} = a^{m}$	$\log_a \alpha^x = \chi \log_a \alpha$	b = Second term or Consequent	proportion then $a \cdot b = c \cdot d$	auadratic equation
• $(2^{m})^{n} = 2^{m}$	• $\log u = x \log a$	• Both terms of ratio can be multiplied	Here a and d are Extremes : h and c	quadratic equation.
• (d) - d	• $\log_a y = \log y / \log a = 1 / \log_y a$	or divided by the same (non-zero)	are Moons	e.g. $ax^2 + bx + c = 0$, where, a, b and c
• (a. b) ''' = a '''. b '''	• $\log_a\left(\frac{1}{m}\right) = -\log_a m$	number	a c	are constants and a $\neq 0$
• $(a / b)^{n} = a^{n} / b^{n}$	• $\log h = \log h / \log a$	• If a quantity increases or decreases in	$\frac{1}{b} = \frac{1}{d} \rightarrow ad = bc$	\circ If b = 0, then the equation is
• $\sqrt[n]{a = a^{1/n}}$	$\log_a b = \log_c b + \log_c a$	the ratio a : b then	 Product of extremes = Product of 	called pure quadratic equation
• a ^m x a ⁿ = a ^{m + n} (base must be same)	• $\log_a b - \log_c b \times \log_a c$		means (Cross product rule)	\circ If b ≠ 0, then the equation is
• $a^m / a^n = a^{m-n}$ (base must be same)	• $\log_a y = \log y / \log a =$	a a conginal Qty.	• If a h c are in continuous	called a mixed or affected
• $a^0 = 1$	m log y / m log a = log y^m / log a^m	The reciprocal of a given ratio is	• If a, b, c are in continuous	quadratic equation
• $a^{x} - a^{y} - b^{x} - y$ (base must be same)	$= \log_a m y^m$	called Inverse ratio	proportion then a : b = b : c	• A supportion equation has two vests
• $a^{-} = a^{-} = x - y$ (base must be same)	• $\log_{a^n} y^m = \frac{m}{n} \log_a y$	• The ratio compounded of the two	• b ² = a c (by cross product rule)	• A quadratic equation has two roots
• $a^{*} = b^{*} \rightarrow a = b$ (power must be	• $\log a + \log b = \log a b$	ratios a : b & c : d is ac : bd	 a:b=c:d → b:a=d:c (Invertendo) 	(i.e. x has two values)
same)	$\log a - \log b - \log \frac{a}{a}$	• The duplicate ratio of $a : b$ is $a^2 : b^2$	 a:b=c:d → a:c=b:d (Alternendo) 	• Roots of a quadratic equation ax ² +
• $a^{*} = b^{*} \& a \neq b \rightarrow \text{ when } x = 0$	• $\log a = \log b = \log \frac{b}{b}$	• The triplicate ratio of $a \cdot b$ is $a^3 \cdot b^3$	 a:b=c:d → (a+b):b=(c+d):d 	$bx + c = 0$, where $a \neq 0$
• $a^x = y \rightarrow a = y^{1/x}$	• $\log a + \log b - \log c = \log \frac{a \times b}{c}$	The sub-duplicate ratio of a this a this day	(Componendo)	$-h + \sqrt{h^2 - 4ac}$
	• $\log h \times \log a = 1$		• a:b=c:d → (a-b):b=(c-d):d	$x = \frac{-b + \sqrt{b} - 4uc}{2}$
PERMUTATION	$\int \log_a b \times \log_b a = \log_a a$	Vb or $a^{\overline{2}}$: $b^{\overline{2}}$	(Dividendo)	2a $-b$
• Number of Permutations when r	• $\log_c b \times \log_b a - \log_c a$	• The sub-triplicate ratio of a : b is $\sqrt[3]{a}$:	 a:b=c:d → (a+b):(a-b)=(c+d):(c-d) 	• Sum of roots $(x_1 + x_2) = \frac{1}{a}$
objects are chosen out of n different	• II $\log_a x = \log_a y$, then $x = y$	$\frac{3}{h}$ or $\frac{1}{h}$, $h^{\frac{1}{h}}$	(Componendo & Dividendo)	• Product of roots $(x, x) = \frac{c}{c}$
abjects Depeted by $^{\text{DD}}$ – $n!$	• $a_{\text{log}b} = b_{\text{log}a}$			a
objects. Denoted by $P_r = \frac{1}{(n-r)!}$	 Log_an = x, then a^x = n 	SEQUENCE & SERIES		 Discriminant (D) = b² – 4ac
Or	• $e^{\log a} = a$	ARTHWETIC PROGRESSION:	• a:b=c:d → (a-c):(b-d)	• If 2 roots of a quadratic equation are
${}^{n}P_{r} = n (n-1) (n-2) \dots (n-r+1).$		• A sequence $a_1, a_2, a_3, \dots, a_n$ is called	(Subtrahendo)	given, then quadratic equation is
where the product has exactly r		an arithmetic progression when a_2 -	Formula for inverse variable	X ² – (Sum of roots) x + Product of roots = 0
factors	PRT = P[1 + RT] = P + C	$a_1 = a_3 - a_2$.	If y is inversely proportional to x	
• $1y_1 + 2y_2 + 2y_2 + + +$	$3I - \frac{1}{100}$, $A = P \left[1 + \frac{1}{100} \right]$, $A = P + SI$	• $t_n = a + (n-1) d$	i.e. $y \propto 1/x$, then, $y = (k/x)$	Nature of Roots:
$= (n+1) 1 c_1 \sum_{n=1}^{n} c_1 \sum_{n=1}^{n} c_n \sum_{n=1}^{n} $		Where, a = first term	Here, K is the constant of proportionality	If D > 0 but not a perfect square then
$-(n+1) = 1$ or $\sum_{r=1}^{n} r$. $P_r = \cdots P_{n+1} - 1$	COMPOUND INTEREST	n = number of terms	LINEAR INEQUALITY	the roots are real, irrational and
• (n-1)! = n!/n	$A = P \left(1 + \frac{R}{m} \right)^{T * m}$	d = common difference	• The Inequality is not affected by	unequal
• ${}^{n}P_{r} = {}^{n}C_{r} r!$ where, $n \ge r$	100 * m	t_n = last term/ n th term	adding/subtracting any number.	If D < 0 then the roots are imaginary
• ${}^{n}P_{r} = {}^{n-1}P_{r} + r. {}^{n-1}P_{r-1}$	$CI = P \left \left(1 + \frac{R}{100} \right)^2 - 1 \right $	$n = \frac{n}{n} \left[2 \frac{n}{n} + \frac{n}{n} \right]$	The Inequality is not affected by	or not real
The no_of arrangements when things	Where D-Dringingly D-Dates T-Time	• $S = \frac{1}{2} [2a + (n-1) d] \text{ or } \frac{1}{2} [a + t_n]$	multiplying/dividing by a pop zero	If D = 0 then reats are real and equal
can be repeated is n	SI – Simple Interest	Where, S = Sum of n terms	nositive number	If D > 0 and perfect severe the other
Linear normutations of a articles have	CI-Compound Interest	a = first term	When is inequality is multiplicate	- II D > 0 and perfect square then the
Linear permutations of n articles having	m-No. of conversion pariod	n = number of terms	divided by a nequality is multiplied/	roots are real, rational and unequal
some articles of same nature	Conversion Period	d = common difference	divided by a negative number the	
• Arrangements = $\frac{n!}{n!}$	Compounded deily	$t = \text{last term}/\text{n}^{\text{th}}$ term	inequality symbol is reversed.	
Repetition!	Compounded daily 365	$t_n = 1$ as the first product numbers	SETS, RELATIONS & FUNCTIONS	INTEGRATION
Sum of all possible arrangements of	Compounded monthly 12	• Sum Snor the first in natural numbers	• Sub Sets: A subset of a main set is a	Integration is the reverse process of
given digits	Compounded quarterly 4	= n(n+1)/2	set which is formed by choice of any	differentiation.
1111 (no. of digits) x sum of digits x	Compounded bi-monthly 6	• Sum S_n of first n odd numbers = n^2	number of elements from the main	
(no. of digits-1)!	Compounded semi-annually 2	• Sum of the Squares of the first n	set. Number of possible subsets = 2 ⁿ	$f(x) \rightarrow Differentiate \rightarrow f'(x)$
Sum of digits containing 0.		natural numbers = $S = n(n + 1)(2n + 1)$	where n = no. of elements.	$f'(x) \rightarrow Integrate \rightarrow f(x)$
[1111 (no. of digits) x sum of digits x (no.	EFFECTIVE RATE OF INTEREST	1)/6	Also, in all possible sets, one is	
of digits-1)!] - [111 (no. of digits -1) x	Effective Rate = $\left(1 + \frac{R}{100 \times m}\right)^m - 1$	• Sum of the cubes of first n natural	improper subset and remaining are	Integration Formulas:
sum of digits x (no. of digits-2)!]	100*///	numbers = $[n(n+1)/2]^2$	nroner Subsets	1. $\int 1 dx = x + C$
Sum of digits containing repetitive digits	FUTURE VALUE (FV)	GEOMETRIC PROGRESSION:	Therefore Proper subsets = $2^n - 1$	$\frac{1}{2} \int \frac{1}{2} dx = 2x + 0$
1111 (no. of digits) x sum of digits x (no.	$\Gamma_{V} = DV \left(1 + \frac{R}{R}\right)^{T*m}$	• A sequence a, ar, ar^2 , ar^3 , ar^n is	and improper subset = 1	2. $\int d dx - dx + C$
· · · · · · · · · · · · · · · · · · ·	$FV = PV \left[1 + \frac{1}{100} \right]$			3. $ x'' dx = ((x''^{+1})/(n+1)) + C$
of digits-1)! / Repetitions!	(100* <i>m)</i>	called Geometric Progression.	• Dewer Cet The collection of all	3 ((<i>n</i> (<i>n</i>)
of digits-1)! / Repetitions! • The number of circular permutations	PRESENT VALUE (PV)	called Geometric Progression.	• Power Set: The collection of all	4. $\int (1/x) dx = \log x + C$
 of digits-1)! / Repetitions! The number of circular permutations of n different things chosen at a time 	PRESENT VALUE (PV) PV = FV / $\left(1 + \frac{R}{m}\right)^{T*m}$	 called Geometric Progression. nth term of GP: t_n = a rⁿ⁻¹ 	• Power Set : The collection of all possible subsets of a given set A is	4. $\int (1/x) dx = \log x + C$ 5. $\int e^x dx = e^x + C$
 of digits-1)! / Repetitions! The number of circular permutations of n different things chosen at a time is (n = 1)! 	PRESENT VALUE (PV) PV = FV / $\left(1 + \frac{R}{100 * m}\right)^{T * m}$	 called Geometric Progression. nth term of GP: t_n = a rⁿ⁻¹ Where, a = first term 	• Power Set : The collection of all possible subsets of a given set A is called the power set of A, to be	4. $\int (1/x) dx = \log x + C$ 5. $\int e^x dx = e^x + C$ 6. $\int e^{ax} dx = e^{ax} / a + C$
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[Sum of infinite terms] DIFFERENTIATION & APPLICATION $= \frac{d}{dx} (a^n) = nx^{n-1}$ $= \frac{d}{dx} (constant) = 0$ $= \frac{d}{dx} (logx) = 1/x$	 Power Set: The collection of all possible subsets of a given set A is called the power set of A, to be denoted by P(A). No of elements in power set = n[P(A)] = 2ⁿ No. of elements in Power set of a power set n[P(P(A))] = 2^{2ⁿ} n(AXB) = n(A) × n(B) FORMULAS - n(AUBUC) = n(A) + n(B) + n(C) - n(A∩B) - n(B∩C) - n(C∩A) + n(A∩B∩C) [Not disjoint sets] n(AUBUC) = n(A) + n(B) + n(C) [If A and B are disjoint sets] n(AUB) = n(A) + n(B) - n(A∩B) [If A and B are not disjoint sets] n(AUB) = n(A) + n(B) - n(A∩B) [If A and B are disjoint sets] n(AUB) = n(A) + n(B) [If A and B are disjoint sets] n(AUB) = n(A) + n(B) [If A and B are disjoint sets] n(A∪B) = n(A) - n(A∩B) n(A'∪B') = n[(A∩B)'] = n(S) - n(A∩B) n(A'∩B') = n[(A∪B)'] = n(S) - n(A∪B) (P ∪ Q)' = P' ∩ Q' (P ∩ Q)' = P' ∪ Q' FUNCTIONS One-One Function (Injective): Let f : A → B. 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[Sum of infinite terms] DIFFERENTIATION & APPLICATION $\frac{d}{dx} (x^n) = nx^{n-1}$ $\frac{d}{dx} (a^x) = a^x \log_e a$ $\frac{d}{dx} (constant) = 0$ $\frac{d}{dx} (e^{\alpha x}) = ae^{\alpha x}$ $\frac{d}{dx} (log x) = 1/x$ $\frac{d}{dx} f(x) = f'(x)$ Product Rule: $\frac{d}{dx} f(\frac{u}{v}) = \frac{u'v - uv'}{v^2}$ APPLICATION Cost Function =C(x)	 Power Set: The collection of all possible subsets of a given set A is called the power set of A, to be denoted by P(A). 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Onto function (Surjective): A function f defined from the set X to set Y (i.e. f : X → Y) is said to be an onto function. 	4. $\int (1/x) dx = \log x + C$ 5. $\int e^x dx = e^{3x} / a + C$ 7. $\int a^x dx = (a^x/\log a) + C; a>0, a\neq 1$ 8. $\int c f(x) dx can be written as cf(x) dx$ 9. $\int f(x) dx \pm g(x) dx can be written as cf(x) dx$ 9. $\int f(x) dx \pm g(x) dx can be written as cf(x) dx$ STANDARD FORMULA a) $\int \frac{dx}{x^2 - a^2} = \frac{1}{2a} \log \frac{x-a}{a+x} + c$ b) $\int \frac{dx}{a^2 - x^2} = \frac{1}{2a} \log \frac{a+x}{a-x} + c$ c) $\int \frac{dx}{\sqrt{x^2 - a^2}} = \log x + \sqrt{x^2 + a^2} + c$ d) $\int \frac{dx}{\sqrt{x^2 - a^2}} = \log x + \sqrt{x^2 - a^2} + c$ e) $\int e^x [f(x) + f'(x)] dx = e^s f(x) + c$ f) $\int \sqrt{x^2 + a^2} dx = \frac{x}{2} \sqrt{x^2 + a^2} + \frac{a^2}{2} \log (x + \sqrt{x^2 - a^2}) + c$ h) $\int \frac{f(x)}{f(x)} dx = \log f(x) + c$ INTEGRATION BY PARTS $\int uv dx = u \int v dx - \int [\frac{d(u)}{dx} \int v dx] dx$ where u and v are two different functions of x INTEGRATION BY PARTS 1 If Marginal Cost = C'(x) then Total cost $C(x) = \int C'(x)$ 1 If Marginal Revenue = R'(x) then Total revenue R(x) = \int R'(x) 1 If Marginal profit = P'(x) then Total Profit P(x) = \int P'(x)
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Denoted by- $^{n}C_{r} = \frac{n!}{r!(n-r)!}$ & $0 \le r \le n$ Or $^{n}C_{r} = [n (n-1) (n-2)(n-r+1)]/r!$ • $^{n}C_{0} = 1$ • $^{n}C_{n} = 1$ • $^{n}C_{r} = ^{n}C_{n-r}$ Where, $0 \le n - r \le n$ • $^{n+1}C_{r} = ^{n}C_{r} + ^{n}C_{r-1}$ • $^{n-1}C_{r} + ^{n-1}C_{r-1} = ^{n-1}C_{r}$ • $^{n}P_{r} = ^{n}C_{r} \cdot r!$ • $^{n}C_{1} + ^{n}C_{2} + ^{n}C_{3} + ^{n}C_{4} + + ^{n}C_{n}$ equals to $(2^{n} - 1)$ Some Important Tricks - • How to count no. parallelograms using n1 & n2 parallel lines intersecting each other = $^{n1}C_{2} \times ^{n2}C_{2}$ • How to count no. of lines that can be made using n points (no 3 or more points are collinear) Or How to find no. of chords in a circle having n points = $^{n}C_{2}$ • How to count no. of lines that can be made using n points out of which m points lie on the same line (collinear) = $^{n}C_{2} - ^{m}C_{2} + 1$	PRESENT VALUE (PV) PV = FV / $\left(1 + \frac{R}{100 * m}\right)^{T * m}$ ANNUITY 1. 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PV of Annuity \checkmark Annuity Regular (1st Payment at the end of 1st period) \checkmark Annuity Due (1st Payment at the beginning of 1st period) FV of Annuity (Regular) = C $\left[\frac{(1+r)^n - 1}{r}\right]$ (1+r) FV of Annuity (Regular) = C $\left[\frac{(1+r)^n - 1}{r}\right]$ (1+r) PV of Annuity (Regular) = C $\left[\frac{1 - \frac{1}{(1+r)^n}\right]$ FV of Annuity (Due) = C $\left[\frac{1 - \frac{1}{(1+r)^n}\right]$ (1+r) where, C = Cash flows per period r=Rate/100*m n = T*m PERPETUITY PV of perpetuity = C/R PV of growing perpetuity = C/(R-G) where, C = Cash flows per period R=Rate per period G=Growth rate NET PRESENT VALUE (NPV) NPV = PV of cash inflow – PV of cash outflow Decision Rule: If NPV > 0 Accept the Proposal If NPV = 0 Accept the Proposal DEPRECIATION WDV/Scrap value = Cost $\left(1 - \frac{R}{100}\right)^T$	called Geometric Progression. n th term of GP: $t_n = a r^{n-1}$ Where, $a = first term$ n = number of terms r = common ratio $t_n = last term/nth term$ Common ratio $= \frac{Any Term}{Preceding Term} = \frac{ar}{a}$ $= \frac{ar^2}{ar} = r$ If a, b, c are in GP we get $\frac{b}{a} = \frac{c}{b}$ which gives $b^2 = a c$, ($b = \sqrt{ac}$), b is called the geometric mean between a & c. $S_n = a (1 - r^n) / (1 - r)$ when $r < 1$ [Sum of GP of n terms] $S_n = a (r^n - 1) / (r - 1)$ when $r > 1$ [Sum of GP of n terms] where, $a = first term$ n = number of terms r = common ratio $a_n = last term/nth term$ $S_n = Sum of n terms$] Sim of infinite terms] $S^{\infty} = \frac{a}{1 - r}$, for $r < 1$. 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PV of Annuity \checkmark Annuity Regular (1st Payment at the end of 1st period) \checkmark Annuity Due (1st Payment at the beginning of 1st period) FV of Annuity (Regular) = C $\left[\frac{(1+r)^n - 1}{r}\right]$ FV of Annuity (Due) = C $\left[\frac{(1+r)^n - 1}{r}\right]$ (1+r) PV of Annuity (Due) = C $\left[\frac{1 - \frac{1}{(1+r)^n}}{r}\right]$ (1+r) PV of Annuity (Due) = C $\left[\frac{1 - \frac{1}{(1+r)^n}}{r}\right]$ (1+r) where, C = Cash flows per period $r = Rate/100^*m$ n = T*m PERPETUITY PV of growing perpetuity = C/(R-G) where, C = Cash flows per period $R = Rate per period$ R = Rate per period G = Growth rate NET PRESENT VALUE (NPV) NPV = PV of cash inflow – PV of cash outflow Decision Rule: If NPV > 0 Accept the Proposal If NPV = O Accept the Proposal If NPV = Not cash value = Cost $\left(1 - \frac{R}{100}\right)^T$ NOTES: In Loan Ques use PV of Annuity (Regular) Formula Loan Amount = Installment $\frac{\left[1 - \frac{1}{(1+r)^n}\right]}{r}$	called Geometric Progression. • n th term of GP: $t_n = a r^{n-1}$ Where, $a = first term$ n = number of terms r = common ratio $t_n = last term/nth term • Common ratio = \frac{Any Term}{Preceding Term} = \frac{ar}{a}= \frac{ar^2}{ar} = r• If a, b, c are in GP we get \frac{b}{a} = \frac{c}{b} whichgives b^2 = a c, (b = \sqrt{ac}), b is called thegeometric mean between a \& c.• S_n = a (1 - r^n) / (1 - r) when r < 1[Sum of GP of n terms]S_n = a (r^n - 1) / (r - 1) when r > 1[Sum of GP of n terms]where, a = first termn = number of termsr = common ratioa_n = last term/nth termS_n = Sum of n terms]Swe = \frac{a}{1 - r}, for r < 1.[Sum of infinite terms]DIFFERENTIATION & APPLICATION• \frac{d}{dx} (x^n) = nx^{n-1}• \frac{d}{dx} (c^{nx}) = ae^{nx}• \frac{d}{dx} (constant) = 0• \frac{d}{dx} (constant) = 0• \frac{d}{dx} (logx) = 1/x• \frac{d}{dx} f(x) = f'(x)• Product Rule: \frac{d}{dx} f(uv) = u'v + uv'• Quotient Rule: \frac{d}{dx} f(\frac{u}{v}) = \frac{u'v - uv'}{v^2}APPLICATIONCost Function = C(x)Average cost (AC) = TC/Output = C(x)/xMarginal Revenue = R'(x)Profit Function P(x) = R(x) - C(x)Marginal profit = P'(x)$	 Power Set: The collection of all possible subsets of a given set A is called the power set of A, to be denoted by P(A). 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If Marginal Revenue = R'(x) then Total cost $C(x) = \int C'(x)$ 6. If Marginal profit = P'(x) then Total revenue $R(x) = \int R'(x)$ 7. If Marginal profit = P'(x) then Total rotal PARTS 7. Total revenue R(x) = \int R'(x) 7. If Marginal profit = P'(x) then Total PARTS 7. Total revenue R(x) = \int R'(x) 7. The BEST III
of digits-1)! / Repetitions! The number of circular permutations of n different things chosen at a time is $(n - 1)!$ The number of ways of arranging n persons along a round table so that no person has the same two neighbours is $= \frac{1}{2}(n-1)!$ Number of necklaces formed with n beads of different colours = 1/2 $(n-1)!$ <u>COMBINATIONS</u> Number of combinations of n different things taken r at a time. Denoted by- $C_r = \frac{n!}{r!(n-r)!}$ & $0 \le r \le n$ Or $C_r = [n (n-1) (n-2)(n-r+1)]/r!$ $^{n}C_n = 1$ $^{n}C_r = ^{n}C_{n-r}$ Where, $0 \le n - r \le n$ $^{n+1}C_r = ^{n}C_r + ^{n}C_{r-1}$ $^{n}C_r + ^{n}C_{r+1} = ^{n+1}C_{r+1}$ $^{n-1}C_r + ^{n-2}C_{r-1} = ^{n}C_r$ $^{n}P_r = ^{n}C_r \cdot r!$ $^{n}C_1 + ^{n}C_2 + ^{n}C_3 + ^{n}C_4 + + ^{n}C_n$ equals to $(2^n - 1)$ Some Important Tricks - How to count no. parallelograms using n1 & n2 parallel lines intersecting each other = $^{n1}C_2 \times ^{n2}C_2$ How to count no. of lines that can be made using n points (no 3 or more points are collinear) Or How to find no. of chords in a circle having n points = $^{n}C_2$ How to count diagonals in a polygon with n sides = $^{n}C_2 - n$ How to count Triangles out of n Points No 3 are collinear = $^{n}C_3 - ^{m}C_3$ where, m = points lie on the same line	PRESENT VALUE (PV) PV = FV / $\left(1 + \frac{R}{100 * m}\right)^{T * m}$ ANNUITY 1. FV of Annuity \checkmark Annuity Regular (1 st Payment at the end of 1 st period) \checkmark Annuity Due (1 st Payment at the beginning of 1 st period) 2. PV of Annuity \checkmark Annuity Regular (1st Payment at the end of 1st period) \checkmark Annuity Que (1st Payment at the beginning of 1st period) FV of Annuity (Regular) = C $\left[\frac{(1+r)^n-1}{r}\right](1+r)$ PV of Annuity (Due) = C $\left[\frac{(1+r)^n-1}{r}\right](1+r)$ PV of Annuity (Due) = C $\left[\frac{1-\frac{1}{(1+r)^n}}{r}\right](1+r)$ where, C = Cash flows per period r=Rate/100*m n = T*m PERPETUITY PV of perpetuity = C/R PV of growing perpetuity = C/(R-G) where, C = Cash inflow – PV of cash outflow Decision Rule: If NPV > 0 Accept the Proposal If NPV > 0 Accept the Proposal If NPV = 0 Accept the Proposal DEPRECIATION WDV/Scrap value = Cost $\left(1 - \frac{R}{100}\right)^T$ NOTES: • In Loan Ques use PV of Annuity (Regular) Formula Loan Amount = Installment $\frac{\left[1 - \frac{1}{(1+r)^n}\right]}{r}$ • In Sinking Fund ques use FV of Annuity Formula • In valuation of bond ques use PV & PV of annuity(regular) formula	called Geometric Progression. • n th term of GP: $t_n = a r^{n-1}$ Where, $a = first term$ n = number of terms r = common ratio $t_n = last term/nth term • Common ratio = \frac{Any Term}{Preceding Term} = \frac{ar}{a}= \frac{ar^2}{ar} = r• If a, b, c are in GP we get \frac{b}{a} = \frac{c}{b} whichgives b^2 = a c, (b = \sqrt{ac}), b is called thegeometric mean between a \& c.• S_n = a (1 - r^n) / (1 - r) when r < 1[Sum of GP of n terms]S_n = a (r^n - 1) / (r - 1) when r > 1[Sum of GP of n terms]where, a = first termn = number of termsr = common ratioa_n = last term/nth termS_n = Sum of n terms]S^{\infty} = \frac{a}{1 - r}, for r < 1.[Sum of infinite terms]DIFFERENTIATION & APPLICATION• \frac{d}{dx} (a^n) = nx^{n-1}• \frac{d}{dx} (c^n) = nx^{n-1}• \frac{d}{dx} (constant) = 0• \frac{d}{dx} (logx) = 1/x• \frac{d}{dx} f(x) = f'(x)• Product Rule: \frac{d}{dx} f(uv) = u'v + uv'• Quotient Rule: \frac{d}{dx} f(\frac{u}{v}) = \frac{u'v - uv}{v^2}APPLICATIONCost Function =C(x)Average cost (AC) = TC/Output = C(x)/xMarginal Revenue = R'(x)Profit Function P(x) = R(x) - C(x)Marginal profit = P'(x)$	 Power Set: The collection of all possible subsets of a given set A is called the power set of A, to be denoted by P(A). No of elements in power set = n[P(A)] = 2ⁿ No. of elements in Power set of a power set n[P(P(A))] = 2^{2ⁿ} n(AXB) = n(A) × n(B) FORMULAS - n(AUBUC) = n(A) + n(B) + n(C) - n(A∩B) - n(B∩C) - n(C∩A) + n(A∩B∩C) [Not disjoint sets] n(AUBUC) = n(A) + n(B) + n(C) [If A and B are disjoint sets] n(AUB) = n(A) + n(B) - n(A∩B) [If A and B are not disjoint sets] n(AUB) = n(A) + n(B) - n(A∩B) [If A and B are disjoint sets] n(AUB) = n(A) + n(B) [If A and B are disjoint sets] n(AUB) = n(A) + n(B) [If A and B are disjoint sets] n(A∪B) = n(A) - n(A∩B) n(A'OB') = n[(A∪B)'] = n(S) - n(A∪B) (P ∪ Q)' = P' ∩ Q' (P ∩ Q)' = P' ∪ Q' FUNCTIONS One-One Function (Injective): Let f : A → B. If different elements in A have different images in B, then f is said to be a one-one or an injective function or mapping Into function: If in A → B, there exist even a single element in B having no pre-image in A, then f is said to be an into function. Onto function (Surjective): A function f defined from the set X to set Y (i.e. f : X → Y) is said to be an onto function if every element in the co-domain is mapped to by some element in its domain. Bijection (One-One onto): A mapping which is both injective and surjective is called a bijection. 	4. $\int (1/x) dx = \log x + C$ 5. $\int e^x dx = e^{xx} C$ 6. $\int e^{ax} dx = e^{ax}/a + C$ 7. $\int a^x dx = (a^x/\log a) + C; a>0, a\neq 1$ 8. $\int c f(x) dx can be written as cf(x) dx$ 9. $\int f(x) dx \pm g(x) dx can be written as cf(x) dx \pm fg(x) dx$ STANDARD FORMULA a) $\int \frac{d^x}{x^2 - a^2} = \frac{1}{2a} \log \frac{x - a}{x + a} + c$ b) $\int \frac{d^x}{d^2 - x^2} = \frac{1}{2a} \log \frac{x - a}{x + a} + c$ c) $\int \frac{dx}{\sqrt{x^2 - a^2}} = \log [x + \sqrt{x^2 + a^2}] + c$ d) $\int \frac{dx}{\sqrt{x^2 - a^2}} = \log [x + \sqrt{x^2 - a^2}] + c$ e) $\int e^x (f(x) + f'(x)) dx = e^x f(x) + c$ f) $\int \sqrt{x^2 + a^2} dx = \frac{x}{2} \sqrt{x^2 - a^2} - \frac{a^2}{2} \log(x + \sqrt{x^2 - a^2}) + c$ g) $\int \sqrt{x^2 - a^2} dx = \frac{x}{2} \sqrt{x^2 - a^2} - \frac{a^2}{2} \log(x + \sqrt{x^2 - a^2}) + c$ h) $\int \frac{f'(x)}{f(x)} dx = \log f(x) + c$ INTEGRATION BY PARTS $\int uv dx = u \int v dx - \int [\frac{d(u)}{dx} \int v dx] dx$ where u and v are two different functions of x INTEGRATION BY PARTS of the moment. Functions of x INTEGRATION BY PARTS if Marginal profit = P'(x) then Total cost $C(x) = \int C'(x)$ if Marginal profit = P'(x) then Total revenue $R(x) = \int R'(x)$ if Marginal profit = P'(x) then Total revenue $R(x) = \int R'(x)$ if Marginal profit = P'(x) then Total PARTS $\frac{POU' f(x)}{P'(x)} = \int P'(x) = \int P'(x)$ if Marginal profit = P'(x) then Total PARTS = C = R + R + R + R + R + R + R + R + R + R

BUSINESS MATHEMATICS CHART FOR CA FOUNDATION BY MAYANK MAHESHWARI

STATISTICS CHART BY MAYANK MAHESHWARI

STATISTICAL DESCRIPTION OF DATA

I. BASIC

- Meaning
- The Word "Statistics" has different meanings when used in "Singular" and "Plural" Senses.
- In **Plural sense** Statistics refers to the **data**, qualitative as well as quantitative.
- In Singular sense Statistics refers to the scientific method
- **Applications of Statistics**
- Economics
- Business Management
- Commerce and Industry
- **Characteristics (Attributes)**
- Aggregate of facts
- Affected to marked extent by large number of causes
- Expressed Numerically
- Reasonable percent of assurance
- Systematic manner
- Pre-defined purpose
- Limitations of Statistics
- It ignores the quality aspect
- No importance to an individual data
- Does not reveal real story
- Data should uniform and homogeneous

II. DATA

- Types of data Primary and Secondary Data
- Data which is collected & used for the first time is known as **Primary Data**
- Data as being already collected, is used by a different person or agency is secondary data
- Methods of collecting data
 - Interview Method
 - ✓ Personal Interview quick, accurate
 - Indirect Interview problem in reaching \checkmark
 - ✓ Telephone Interview less consistent,
 - wide coverage, non responses are high • Mailed Questionnaire – wide coverage, maximum
 - non-responses
 - Observation Method best accuracy, time consuming, laborious, best
 - method
 - Questionnaires used for larger enquiries
 - International sources
 - Government sources
 - Private and quasi-government Secondary Sources sources
 - Unpublished sources
- **Classification of data**
 - Chronological or Temporal or Time Series Data data are classified in respect of successive time points or intervals
 - Geographical or Spatial Series data Data arranged region wise
 - o Qualitative or Ordinal Data Data classified in respect of an attribute
 - **Quantitative or Cardinal Data** When the data is classified in respect of a variable
 - Frequency and Non-Frequency group ✓ Frequency – Qualitative & Quantitative
 - ✓ Non-frequency Chronological & Geographical
 - **III. PRESENTATION OF DATA**

- Line Diagram: When the data vary over time, we take recourse to line diagram.
 - ✓ Logarithmic and Ratio Charts: When the time series exhibit a wide of fluctuations.
 - ✓ Multiple line and Multiples Axis charts: Multiple line charts are used for representing two or more related time series data expressed in the same unit, and multiple - axis chart in somewhat similar situations if the variables are expressed in different units.
- Graphical Presentation The various types of graphical representation of a Frequency Distribution are as follows -
- Histogram or Area Diagram It is the most convenient way to represent a Frequency Distribution. With a Histogram, an idea of the Frequency Curve of the Variable under study can be obtained. A comparison among the frequencies for different Class Intervals is possible with Histograms
- Frequency Polygon A Frequency Curve can be regarded as 0 a limiting form of Frequency Polygon & Histogram.
 - Area of Histogram = Area of Polygon
- Ogives or Cumulative Frequency Graphs There are two types of Ogives –
 - ✓ **Less than type Ogives**: Plotting less than Cumulative Frequency
 - ✓ **More than type Ogives**: Plotting more than Cumulative Frequency
- Ogives may be considered for obtaining median, quartiles, deciles & percentiles graphically. Ogives are used for making short term projections

Particulars	Histogram	Bar diagram			
Space	No	Yes			
Mode	Yes	No			
Variable	Continuous series	Discrete & continuous series			
Width	Important	Not Important			

IV. FREQUENCY DISTRIBUTION

- Meaning: Frequency Distribution is a Tabular Representation of Statistical Data that distributes the total frequency to a number of classes.
- Width or Size or length of a Class Interval: The width of a Class Interval is the difference between the UCB and the LCB of that Class Interval. [Class Interval = UCB – LCB]
- Class Limit inclusive & exclusive series
- **Class Boundary** exclusive series only Mid-Point or Class Mark

Mid-Point =
$$\frac{UCL+LCL}{2}$$
 or $\frac{UCB+LCB}{2}$

- Frequency Density = Frequency of Given Class / Class width
- **Relative Frequency** = Class Frequency / Total Frequency **Percentage Frequency** = Relative Frequency x 100

THEORETICAL DISTRIBUTIONS

Discrete Probability Distributions – Binomial, Poisson distributions Continuous Probability Distribution – Normal distribution **BINOMIAL DISTRIBUTION**

 $P(x) = {}^{n}C_{x} p^{x} q^{n-x}$ where, n = no. of trials (n = 0, 1, 2, ..., n) x = Success required (x = 0, 1, 2, 3, ... n) p = Probability of success of single event

q = Probability of Failure of single event

Properties:

Primary

Ces

- Binomial distribution is bi-parametric. 2 parameters are (n and p)
- Mean = μ = np; Variance = σ^2 = npq; SD = $\sigma = \sqrt{npq}$
- Variance is always less than Mean
- Variance will be highest when p = q (i.e. p = q = 1/2) = n/4Mode = (n+1)p; if (n+1)p is non integer then mode = highest integer value. (i.e. Uni-modal); if (n+1)p is integer then Mode =

MEASURES OF CENTRAL TENDENCY

- Types of Continuous Series Types of Series • Individual Series • Inclusive Series
- Discrete Series • Exclusive Series • Continuous Series

 $\overline{x} = \frac{\Sigma x}{\Sigma}$

 $\overline{x} = \frac{\Sigma f x}{\Sigma f x}$

Properties of Mode

Individual series

Properties of GM

i.e. a

○ GM<AM

of index numbers

Harmonic Mean (HM)

Discrete & Continuous Series

• Combined HM = $\frac{n_1 + n_2}{\frac{n_1}{11} + \frac{n_2}{12}}$

• Weighted HM = $\frac{\Sigma w}{\Sigma^{\frac{w}{2}}}$

are covered.

QUARTILES

Quartiles divide the set

of observations into 4

equal parts

 Q_1, Q_2, Q_3

There are 3 Quartiles

'EQUAL' amount is invested

Other Partitional Values

set of observations.

0

Geometric Mean (GM)

Discrete or Continuous Series

• Change of Origin & Scale: If x and y are 2 variables related

Geometric Mean is the nth root of n terms. It is the best measure of

central tendency for ascertaining rate of change over a period of time

 $GM = (X_1 \times X_2 \times X_3 \times \dots \times X_n)^{1/n}$

 $GM = (X_1^{f1} \cdot X_2^{f2} \cdot X_3^{f3} \dots X_n^{fn})^{1/n}$

If all the observations are same, say a, then GM is also same.

GM of the product of 2 variables is the product of their GM.

i.e. if z = xy, then GM of Z = GM of x. GM of y

 \circ GM of the ratio of 2 variables is the ratio of the GM's of 2

• It is the best measure of central tendency for ascertaining the

• It is the most appropriate average to be used for construction

o It is the most suitable average to be used when it is desired

It is defined as the reciprocal of the AM of the reciprocals of a given

HM = $\frac{n}{\frac{1}{x_1} + \frac{1}{x_2} + \frac{1}{x_3} + \dots + \frac{1}{x_n}}$ OR HM = $\frac{n}{\sum_{x_1}^{1}}$

 $HM = \frac{1}{\sum_{i=1}^{f}}$

the harmonic mean of the observations is also same, i.e. k

• The harmonic mean has the least value when compared to the

• It is used primarily in averaging speeds when 'EQUAL' distances

• It is also used in averaging cost of commodity/ securities when

DECILES

Deciles divide the set of

observations into 10

equal parts.

Quartiles $(Q_k) - (Q_1, Q_2, Q_3)$

...., D9

There are 9 Deciles There are 99 Percentiles

D₁, D₂, D₃,

PERCENTILES

Percentiles divide the

set of observations into

100 equal parts.

P₁, P₂, P₃,, P₉₉

geometric mean and the arithmetic mean (i.e. AM > GM > HM)

If any one observation is 0, then HM is 'not defined'

average rate of change over a period of time

to give more weightage to smaller items

variables i.e. if z = x/y then GM of z = GM of x/GM of y

If any observation is zero (0) then GM is not defined

as y = a + bx, then Y_(mo) = a + b.X_(mo)

Mode = 3 Median – 2 Mean

Central tendency is an average which represent the characteristics of the entire data and help us to compare the given data with another data. This average has a tendency to be somewhere at the centre and hence called Measure of Central Tendency.

DIFFERENT MEASURES OF CENTRAL TENDENCY

Arithmetic Mean (AM)	
Individual Series:	

Discrete or Continuous Series:

Properties of AM

- \circ If all the observations are same, say 'k', then the AM is also 'k'
- The algebraic sum of deviations of the given set of observations taken from the AM is always **ZERO.** i.e. $\sum f(x - \bar{x}) = 0$
- o (Change of Origin) If each observation of a data is increased or decreased by a constant 'k', then the AM of new data also gets increased or decreased by 'k'
- (Change of Scale) If each observation of a data is multiplied or divided by a constant 'k', then the AM of new data also gets by multiplied or divided by 'k'
- (Change of Origin & Scale) AM is affected due to change of origin and/or scale which implies that if the original variable 'x' is changed to another variable 'y' by affecting a change of origin, say a, and change of scale, say b, of x, i.e. y = a + bx, then AM of y is given by $\overline{y} = a + b\overline{x}$
- The sum of Square of deviations of given set of observations is minimum when taken from **AM**. i.e. $\sum (x - \bar{x})^2$ is minimum **Individual Series** Correcting incorrect mean 0
- Step 1: Calculate wrong total ($\bar{x} \times n$) Step 2: Calculate correct total = Wrong total - wrong
- observations + correct observations Step 3: Correct mean = $\frac{correct correct}{no. of observations}$
- If there are two groups containing n_1 and n_2 observations and \bar{x}_1 Properties of HM and \bar{x}_2 as the respective arithmetic means, then the **combined** • If all the observation taken by a variable are same, say k, then **AM** is given by

$$\bar{x} = \frac{\bar{x}_1 n_1 + \bar{x}_2 n_2}{n_1 + n_2}$$

• Weighted AM =
$$\bar{x}_w = \frac{w_i x_1 + w_2 x_2 + \dots + w_n x_n}{w_1 + w_2 + \dots + w_n}$$
 or $\bar{x}_w = \frac{\Sigma w x}{\Sigma w}$

Median (Positional Average)

Median in case of Discrete Series

Median in case of Continuous Series

class is called median class.

Step 1: Prepare 'less than' c.f. distribution

Step 2: Find n/2, where n = no. of observations

Step 1: Prepare 'less than' c.f. distribution

Step 2: Find (n+1)/2, where n = no. of observations

- Median in case of Individual Series
- In case of odd observations, Median = Middle Value or (n+1)/2 observation

In case of even observations, Median = Average of Middle two

Step 3: See the c.f. just greater than equal to $(n+1)/2^{th}$ observation.

Values or Average of n/2 and n/2+1 observation

Step 4: The variable corresponding to the c.f. is the median.

Step 3: See the c.f. just greater than equal to n/2th observation.

Step 4: Find the class corresponding to the c.f. obtained in Step 3. This

- Textual Presentation This method comprises presenting data with the help of a paragraph or a number of paragraphs. This type of presentation can be taken as the first step towards the other methods of presentation. It is dull, monotonous and comparison between different observations is not possible
- **Tabular Presentation** There are two types of table Simple & Complex.

The Table under consideration should be divided into Caption, Box-head, Stub and Body. Caption is the upper part of the table, describing the columns and sub-columns, if any. The Box-head is the entire upper part of the table which includes columns and subcolumn numbers, unit(s) of measurement along with caption. Stub is the left part of the table providing the description of the rows. The body is the main part of the table that contains numerical figures.

• It facilitates comparison between rows and columns.

• Complicated data can also be represented using tabulation.

• It is a must for diagrammatic representation.

- Without tabulation, Statistical Analysis of data is not possible
- Diagrammatic Presentation An attractive representation of statistical data is provided by Charts, Diagrams and Pictures. Unlike the first two methods of representation of data, diagrammatic representation can be used for both the educated section and uneducated section of the society. Furthermore, any • hidden trend present in the given data can be noticed only in this mode of representation. Diagrams can be (B.P.L) - Bar Diagram, Pie Chart and Line Diagram

• Bar Diagram: Rectangle of equal width & usually of varying Properties: length. Bar Diagrams may be -(a) Horizontal Bar Diagram (used for qualitative data or data varying over space), or (b) Vertical Bar Diagram (used for quantitative data or time series data).

• Pie diagram: This type of diagram shows the components of a variate as parts of a Circle.

(n+1)p & (n+1)p – 1 (i.e. Bi-modal) **POISSON DISTRIBUTION** $P(x) = \frac{e^{-m} m^x}{x!}$; where, e = exponential function (e = 2.71828) m = Average or mean = np = μ x = no. of success required $(0,1,2,3,...,\infty)$ **Properties:**

It is Uni-parametric. 1 parameter is m Mean = μ = m; Variance = σ^2 = m; SD = $\sigma = \sqrt{m}$ Mode = m, if m integer, then mode = m, m-1 (bi-modal); if m non-integer, then mode = m (uni-modal) NORMAL DISTRIBUTIONS $F(x) = \frac{1}{\sigma\sqrt{2\mu}} e^{\frac{-1}{2}\left(\frac{x-\mu}{\sigma}\right)^2} \text{ for } -\infty < x < \infty, \text{ where, } \sigma = \text{S.D., } \mu = \text{mean}$

A function f(x) is Probability Density Function (PDF) if –

 $F(x) \ge 0, -\infty < x < +\infty$ ii. $\int_{-\infty}^{\infty} f(x) \, dx = 1$

The normal distribution curve is a bell-shaped curve.

At the center of the curve lies Mean, Median & Mode (i.e. μ = Mean, Median & Mode)

Normal distribution curve is Uni-modal

The curve never touches the x-axis

The total area under the curve = 1 or 100%

The point of inflection are $\mu + \sigma \& \mu - \sigma$

For a standard normal variate, value of Mean = 0, SD = 1

The skewness of the normal distribution curve is zero

The normal distribution has 2 parameters i.e. $\mu \& \sigma$

• Q1 = μ - 0.675 σ ; Q3 = μ + 0.675 σ

QD : MD : SD = 10 : 12 : 15; MD = 0.8 σ ; QD = 0.675 σ

If X and Y are 2 independent normal variables with mean as a &

b and SD as x & y, then normal distribution (X+Y) is distributed Mean = a+b & SD = $\sqrt{x^2 + y^2}$ with

Step5: Apply the following formula Median = $l + \frac{2}{2} \times h$ Where, I = lower limit of median class

> c = c.f. of the class preceding the median class f = frequency of the median class h = size or width of the median class

Properties of Median

- The sum of absolute deviations is minimum when the deviations are taken from the **median.** i.e. $\sum |x - A|$ is minimum, where A = median
- (Change of Origin & Scale) If x and y are two variables, to be related by y = a + bx for any two constants a and b, then the median of y is given by $y_{me} = a + bx_{me}$

• Mode

Mode is the value which occurs maximum number of times. Therefore, it is also called as fashionable average **Individual Series** An observation repeated maximum number of times. **Discrete Series** Observation having Highest frequency. **Continuous Series** Step 1: Find Modal Class (i.e. Class with highest frequency) Step 2: Apply following formula: Mode = $l + \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \times h$ Where, I = lower limit of modal class.

 f_1 = frequency of modal class f_0 = preceding frequency f_2 = Succeeding frequency, h = height of modal class

Computation: Individual Series Step 1: Arrange data in order Step 2: Find the rank of $\frac{K(n+1)}{4}$ Step 3: Corresponding Variable is Quartile. **Discrete Series** Step 1: Arrange data in order Step 2: Prepare c.f. distribution Step 3: Find the rank of $\frac{K(n+1)}{4}$ Step 4: Then find the c.f. just greater than equal to $\frac{K(n+1)}{k}$ Step 5: Corresponding Variable is Quartile. **Continuous Series** Step 1: Prepare c.f. distribution Step 2: Find $\frac{\kappa n}{\kappa}$ Step 3: See the c.f. just greater than equal to $\frac{\kappa n}{r}$ Step 4: Find the Quartile class Step 5: Apply the formula:

Where, I = lower limit of Quartile class c = c.f. of the class preceding the Quartile class f = frequency of the Quartile class h = size or width of the Quartile class Note: For computation of Deciles, use same steps as used in Quartile calculation, just replace 4 with 10. Note: For computation of Percentiles, use same steps as used in Quartile calculation, just replace 4 with 100. Relationship between AM, GM & HM • When observations are unequal, positive & greater than zero,

AM > GM > HM always.

- If all the observations are equal, AM = GM = HM
- \circ AM x HM = (GM)²

STATISTICS CHART FOR CA FOUNDATION BY MAYANK MAHESHWARI

MEASU	RES O	F DISPERSION		IV. S
The degree to which numer	ical da	ta tend to spread about an	It is de	efined as the roo
average value is called the d	are ta	ken from A.M.		
High variation/Dispersion -		Variance		
Low variation/ Dispersion -	G	OOD	Calcu	lation:
Absolute Measure		Relative Measure		
Absolute measures are depe	ndent	Relative measure of dispersion are		$\sum (x - x)$
on the unit of the variable	under	unit free.	3	S.D. or $o = \sqrt{-n}$
consideration				
Absolute measures are	not	For comparing 2 or more		D
considered for comparison.		distributions, relative measures are	сг	$\sum f(x-x)$
Absolute measures are ea	sv to	Relative measures are difficult to	5.6	\sqrt{n}
compute and understand.	<i>Sy</i> 10	compute and understand		
Types of Measures of Dispersi	~	· ·		Coef
Absolute Measure		Relative Measure		
Range	•	Coefficient of Bange		
Quartile Deviation	•	Coefficient of Quartile Deviation	Prone	erties of S.D.
Mean Deviation	•	Coefficient of Mean Deviation	liope	
Standard Deviation	•	Coefficient of Variation	0 5	5.D. of first n nat
	D۸	NGE		$D = \frac{2}{\sigma} M D$
Range is the simplest metho	d of c	omputing the dispersion		3 10.0
Range is the simplest metho	Range	= 1 - S	0 5	S.D. of 2 number
where I = Larg	est val	lue. S = Smallest value		Combined S.D
Coefficier	nt of P	$\frac{L-S}{S} \times 100$		Johnbined S.D
		L+S 100	۱ ۱	where, $d_1 = \bar{x}_1$
Properties of Range:			9	$S_1 = S.D. of 1^{st} Gr$
 Range is based on 2 ex ill defined 	treme	values of the observation & hence	r	n_1 , n_2 = No. of ob
\sim It is not possible to con	onuto	range in case of open-ended		
distribution	ipute	range in case of open-ended	Merit	s of S.D.
Merits of Bange:				t is the best me
\circ It is easy to calculate a	nd und	lerstand		t considers all o
\circ It requires minimum ti	me to	calculate		t is rigidly define
De-merits of Range:				t is useful for tu
\circ It is not based on all ob	servat	ions	De-m	erits of S.D.
 Range is a poor measu 	re of d	ispersion		t cannot ha corr
		·······		listributions
II. QUARTILE DEVIATIO	N (SEN	AI INTER QUARTILE RANGE)	Comn	non properties
QUA	RHLES	(Q_1, Q_2, Q_3)		MOD are LINAFF
It is defined as half of the de	eviatio	n between the upper Quartile &		They CHANGE in
Lower Quartile of the distric	oution.	$0_{2} = 0_{2}$		f all the observa
	Q.D. =	$=\frac{\sqrt{3}}{2}$		f any 2 constant
Coefficien	t of Q.	$D_{-} = \frac{Q_3 - Q_1}{Q_1 + Q_2} \times 100$	t	hen.
	C	$Q_3 + Q_1$	Comp	utation is as fol
		$\frac{Q_3 - Q_1}{Q_3 - Q_1}$		M
Coefficient c	of Q.D.	$=\frac{2}{Median/Q_2} \times 100$		Range
Coefficient o	of O.D.	$= \frac{QD}{2} \times 100$		Quartile Deviat
Inter Ou	artila	$Median/Q_2$		Mean Deviation
	$-\Omega_{a} =$	$a_{1}g_{2} = Q_{3} = Q_{1}$		Standard Devia
Properties of Q.D.	4 2	¥2 ¥1		
 It is best suited measure 	re of d	ispersion for an open-end	Proba	bility of n even
distribution.			event	in a Random Ex
• It is based on middle 5	0% of t	the values of the distribution		$D(\Lambda) = \frac{Occi}{C}$
• First 25% & last 25% va	lues a	re left out.		F(A)
Merits of Q.D.			Prope	rty & Formulas
o It is simple to understa	nd and	d calculate	• P(A) + $P(A') = 1, or$
• It is superior to Range			• P(AUB) = P(A) + P(A)
 It can be computed for 	distri	oution with Open-end classes	• P(AUB) = P(A) + P(A)
 Q.D. is not affected by 	extren	ne values	• P(AUBUC) = P(A) -
De-merits of Q.D.			P(A∩B∩C) [not m
 It is not based on all th 	• P(AUBUC) = P(A) -		

IV. STANDARD DEVIATION (
$$\sigma$$
)
the root mean square deviation when the deviations
A.M.
iance is Square of S.D. (i.e. Variance = σ^2)
Individual Series
 $\sqrt{\frac{Y(x-X)^2}{n}} OR = \sqrt{\frac{xx^2}{n} - (\frac{x}{n})^2} OR = \sqrt{\frac{xx^2}{n} - (\bar{x})^2}$
Discrete & Continuous series
 $\frac{Y(x-X)^2}{n} OR = \sqrt{\frac{xx^2}{n} - (\frac{x}{n})^2} OR = \sqrt{\frac{xx^2}{n} - (\bar{x})^2}$
Coefficient of Variation = $\frac{S.D}{A.M.}$
D.
Coefficient of Variation = $\frac{S.D}{A.M.}$
D.
Coefficient of S.D. = $\frac{S.D}{A.M.}$
D.
Coefficient of S.D. = $\frac{S.D}{A.M.}$
D.
Coefficient of S.D. = $\frac{S.D}{A.M.}$
D.
 $M.D. = \frac{4}{5}\sigma$
 $S.D. = \sqrt{\frac{\pi^2-1}{122}}$
 $M.D. = \frac{4}{5}\sigma$
 $S.D. = \sqrt{\frac{\pi^2-2}{n}},$
 $r_1 = \pi^2, d_2 = \frac{x_2 - \bar{x}}{n},$
 $r_1 = \frac{x}{n}, d_2 = \frac{x_2 - \bar{x}}{n},$
 $r_1 = \frac{x}{n}, d_2 = \frac{x}{2} - \bar{x},$
 $r_1 = x^2, d_2 = \frac{x}{2} - \bar{x},$
 $r_2 = Combined mean$
 $r_2 = Combined mean$
 $r_2 = 1 = \frac{1}{\sqrt{\frac{2C-\pi}{n}}}$
Where, $c = no.$ of baservations = 1
Property of Correlation
 $r_c = \pm \sqrt{\frac{2C-\pi}{n}}$
Where, $c = no.$ of playervations - 1
Property of Correlation
 $r_c = \pm \sqrt{\frac{2C-\pi}{n}}$
Where, $c = no.$ of playervations - 1
Property of Correlation
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Where, $c = no.$ of playervations - 1
Property of Correlation
 $r_c = \pm \sqrt{\frac{2C-\pi}{n}}$
Where, $c = no.$ of playervations - 1
Property of Correlation
 $r_c = \pm \sqrt{\frac{2C-\pi}{n}}$
Where, $c = no.$ of playervations - 1
Property of Correlation
 $r_c = \frac{1}{|m|/|d|}$, r_{xy}
Note: Coefficient of correlation between $x \leq y$
 $r_{ca} = \frac{1}{|m|/|d|}$, r_{xy}
Note: Coefficient of ordetermination
 $1-r^2$ coefficient of non-determination
 $1-r^2$ coefficient of non-determin

utation is as follows:			REGRESSION		
MOD	Value		Regression is concerned with estimating the value of DEPE		
Range	$R_y = b $. R_x		Variable Corresponding to a known INDEPENDENT Variab		
Quartile Deviation	$QD_y = b . QD_x$		In other words, known variable is independent variable and		
Mean Deviation	$MD_y = b \cdot MD_x$		unknown variable is dependent variable.		
Standard Deviation	$SD_y = b .SD_x$		Regression Coefficient are byx, bxy		
DDODAD			b _{YX}	b _{XY}	
PROBABILITY bility of n events refers to the chance of occurrence of such in a Random Experiment. $P(A) = \frac{Occurrence of favourable event A}{OR} = \frac{n(A)}{n(A)}$		$\mathbf{b}_{YX} = \frac{n\Sigma XY - (\Sigma X)(\Sigma Y)}{n\Sigma X^2 - (\Sigma X)^2}$	$\mathbf{b}_{XY} = \frac{n\Sigma XY - (\Sigma X)(\Sigma Y)}{n\Sigma Y^2 - (\Sigma Y)^2}$		
		$\mathbf{b}_{YX} = r \frac{\sigma_y}{\sigma_x}$	$\mathbf{b}_{XY} = r \frac{\sigma_x}{\sigma_y}$		
P(A) – Total outcom	$\frac{1}{nes}$ OR $-\frac{1}{n(S)}$		here, r = Coefficient of	here, r = Coefficient of	
rty & Formulas –			correlation	correlation	
A) + P(A') = 1, or P(A') = 1 - P(A)		$\mathbf{b}_{YX} = \frac{Cov(x,y)}{(\sigma x)^2}$	$\mathbf{b}_{XY} = \frac{Cov(x,y)}{(\sigma y)^2}$		
AUB) = $P(A) + P(B)$ [mutually exclusive events] AUB) = $P(A) + P(B) - P(A \cap B)$ [not mutually exclusive events]			Regression Equation		
			Y depends on X	X depends on Y	
$A \cup B \cup C = P(A) + P(B) + P(C) - P(A \cap B) - P(B \cap C) - P(A \cap C) + A \cap B \cap C$ $A \cap B \cap C = P(A) + P(B) + P(C) $ $A \cup B \cup C = P(A) + P(B) + P(C) $ $A \cup B \cup C = P(A) + P(B) + P(C) $ $A \cup B \cup C = P(A) + P(B) + P(C) $		Y on X	X on Y		
			General Form:	General Form:	
			Y = a + bX	X = a + bY	

LALYSISINDEX NUMBERpetween 2 variables.
retween 2 variables.
tween 2 variables.
tween 2 variables.
tween 2 variables.
tween 2 variables.
treated to production, etc.
Expressed in Percentage, Measures of Net Changes, Measure
change over a period of time
What are the types of Index Numbers?ammatic method to
o measure the extent
o measure the extent• Price Index Numbers - Shows movement in price levels
between 2 periods- It is also known as
o measure the extent
o measure the extent
(
$$\overline{y}$$
)• Quantity Index Numbers - Shows movement in Value levels
between 2 periods- It is also known as
(\overline{y})• Origonal to the price index for time 1 on 0.
Here, P_0 = Base year price, P_1 = Current year price
 P_0 : 5 Current year price / Base year price, P_1 = Current year price
 P_0 : 5 Current year price / Base year price, P_1 = Current year price
 P_0 : 5 Current year price / Base year price, P_1 = Value Index
Numberswpiled to identify the
 $(\overline{y})^{2^2}$
 $(\overline{y})^{2^2}$ • The ratio of the price of a single commodity in a given period to
its price in other period is called the Price Relative.
Price relative = P_1/P_0^{+100}
• Index Numbers are constructed from the sample
• Weights play an important part in construction of Index
Numbersnumbers
on of the 2 variables.
the best average for construction of Index Number is GM. But in
general practice AM is used.
• GM makes index number time reversable $P_{01} \rightarrow P_{10}$
• Pure numbers are used to measure economic strength
• Purchaing power of Money = $1/Price Index$
• Cost of Living index is Price Index
• Cost of Living index is Price Index
• Cost of Living index is Price Index
• Drice Index Poin = $\frac{2P_0}{R_0} \times 100$
here, $\sum P_1 = Sum of all commodit$

✓ Fisher's Ideal Price Index →
$$P_{01} = \sqrt{\frac{\Sigma p_1 q_0}{\Sigma p_0 q_0} \times \frac{\Sigma p_1 q_1}{\Sigma p_0 q_1}} \times 100$$

OR
$$P_{01} = \sqrt{L * P}$$

- ✓ Dorbish & Bowley's Price Index $P_{01} = \left[\frac{\Sigma p_1 q_0}{\Sigma p_0 q_0} + \frac{\Sigma p_1 q_1}{\Sigma p_0 q_1}\right]/2 * 100 \text{ OR } P_{01} = \frac{L+P}{2}$
- Note: - The result obtained by Marshall Edgeworth method is closest to Fisher's Index
 - Fisher's Ideal Index is GM of Laspeyre's & Paasche's Index

III. MEAN DEVIATION (AVERAGE DEVIATION) • P(. Mean Deviation is the A.M. of the absolute deviation of the • P(observations from an appropriate measure of central tendency (i.e. Types Mean, Median or Mode)

M.D. =
$$\frac{\sum |x-A|}{n} = \frac{\sum |D|}{n}$$
 (Individual Series

• It is not suitable for further mathematical treatment

M.D. = $\frac{\sum f |x-A|}{n} = \frac{\sum f |D|}{n}$ (Discrete & Continuous Series) Where, A = Mean, Median or Mode D = X - A

Coefficient of M.D. = $\frac{MD}{A} \times 100$

Property of M.D.

• The M.D. is minimum when the deviations are taken from Median.

Merits of M.D.

- It is based on each and every observation
- It is rigidly defined
- It is easy to calculate and understand
- As compared with S.D., it is less affected by extreme observations

De-merit of M.D.

- Algebraic signs are ignored
- o It is not suitable for further mathematical treatment
- It cannot be computed for distributions with open ended classes

All birds find shelter during the rain. But eagle avoids the rain by flying above the clouds. Be an Eagle **ALL THE BEST!!**

CHART PREPARED BY MAYANK MAHESHWARI

• $P(B-A) = P(B) - P(A \cap B)$ [Probability of only B]	ner
• $P(A \cap B) = P(AB) = P(A \text{ and } B)$ all are same	Poir
• $P(AUB) = P(A \text{ or } B) = P(A+B)$ all are same	$y - \overline{y} =$
Types of events	Properties of R
 Independent Event – If outcome of one event does not influence 	 Coefficien
the occurrence of the other event.	of ORIGIN
$P(A \cap B) = P(A) \times P(B); P(A \cap B') = P(A) \times P(B'); P(A' \cap B) = P(A') \times P(B)$	Chang
$P(A' \cap B') = P(A') \times P(B')$; $P(A \cap B \cap C) = P(A) \times P(B) \times P(C)$	Chai
• Mutually exclusive events – If occurrence of one event prevents	
the occurrence of the other events.	
Therefore, $P(A \cap B) = 0$; $P(A \cap B \cap C) = 0$; $P(A \cup B) = P(A) + P(B)$	
• Mutually exhaustive events – It means that the events together	 Relationsl
make up everything that can happen.	
P(AUB) = 1; P(AUBUC) = 1	\circ r, b _{yx} , b _{xy}
Mutually exclusive & exhaustive events	 Both regret
P(AUBUC) = P(A) + P(B) + P(C) [when exclusive]	their MEA
P(AUBUC) = 1 [when exhaustive]	
$P(\Lambda) + P(R) + P(C) = 1$ [when exclusive & expansion]	
F(A) + F(B) + F(C) = 1 [when exclusive & exhaustive]	CALCULATOR I
Odd in Favour & Odd against	Find a ⁿ
Odd in Favour & Odd against Odd in favour = Favourable outcomes : Unfavourable outcomes	Find a ⁿ Steps
Odd in Favour & Odd against Odd in favour = Favourable outcomes : Unfavourable outcomes Odd against = Unfavourable outcomes : Favourable outcomes	Find a ⁿ Steps - type a
Odd in Favour & Odd against Odd in favour = Favourable outcomes : Unfavourable outcomes Odd against = Unfavourable outcomes : Favourable outcomes Total outcomes = Favourable + Unfavourable	Find a ⁿ Steps - type a - Press ×
Odd in Favour & Odd against Odd in favour = Favourable outcomes : Unfavourable outcomes Odd against = Unfavourable outcomes : Favourable outcomes Total outcomes = Favourable + Unfavourable Conditional Probability	Find a ⁿ Steps - type a - Press × - Press = (n-1
Odd in Favour & Odd against Odd in favour = Favourable outcomes : Unfavourable outcomes Odd against = Unfavourable outcomes : Favourable outcomes Total outcomes = Favourable + Unfavourable Conditional Probability $P(B/A) = \frac{P(A \cap B)}{P(A)}; P(A/B) = \frac{P(A \cap B)}{P(B)}$	Find a ⁿ Steps - type a - Press × - Press = (n-1
Odd in Favour & Odd against Odd in favour = Favourable outcomes : Unfavourable outcomes Odd against = Unfavourable outcomes : Favourable outcomes Total outcomes = Favourable + Unfavourable Conditional Probability $P(B/A) = \frac{P(A \cap B)}{P(A)}; P(A/B) = \frac{P(A \cap B)}{P(B)}$ Statistical Definition of Probability	Find a ⁿ Steps - type a - Press × - Press = (n-1
Odd in Favour & Odd against Odd in favour = Favourable outcomes : Unfavourable outcomes Odd against = Unfavourable outcomes : Favourable outcomes Total outcomes = Favourable + Unfavourable Conditional Probability $P(B/A) = \frac{P(A \cap B)}{P(A)}; P(A/B) = \frac{P(A \cap B)}{P(B)}$ Statistical Definition of Probability Mean = Expected Value = $\mu = F(x) = \Sigma P(X) X \text{ or } \Sigma B_{x} X_{y}$	Find a ⁿ Steps - type a - Press × - Press = (n-1
Odd in Favour & Odd against Odd in Favour & Odd against Odd in favour = Favourable outcomes : Unfavourable outcomes Odd against = Unfavourable outcomes : Favourable outcomes Total outcomes = Favourable + Unfavourable Conditional Probability $P(B/A) = \frac{P(A \cap B)}{P(A)}; P(A/B) = \frac{P(A \cap B)}{P(B)}$ Statistical Definition of Probability Mean = Expected Value = $\mu = E(x) = \Sigma P(X).X$ or $\Sigma R_f.X_i$ Probability = $P(X) = P(X_i) = R_f: Variable = X = X_i$	Find a ⁿ Steps - type a - Press × - Press = (n-1 Find a ⁿ where r integer
Odd in Favour & Odd against Odd in Favour & Odd against Odd against = Unfavourable outcomes : Unfavourable outcomes Odd against = Unfavourable outcomes : Favourable outcomes Total outcomes = Favourable + Unfavourable Conditional Probability $P(B/A) = \frac{P(A \cap B)}{P(A)}; P(A/B) = \frac{P(A \cap B)}{P(B)}$ Statistical Definition of Probability Mean = Expected Value = $\mu = E(x) = \Sigma P(X).X$ or $\Sigma R_f.X_i$ Probability = $P(X) = P(X_i) = R_f;$ Variable = $X = X_i$ Expected value of x^2 in given by: $E(X_i^2) = \Sigma P(X_i) X_i^2$	Find a ⁿ Steps - type a - Press × - Press = (n-1) Find a ⁿ where r integer Steps
Odd in Favour & Odd against Odd in Favour & Odd against Odd against = Unfavourable outcomes : Unfavourable outcomes Odd against = Unfavourable outcomes : Favourable outcomes Total outcomes = Favourable + Unfavourable Conditional Probability $P(B/A) = \frac{P(A \cap B)}{P(A)}; P(A/B) = \frac{P(A \cap B)}{P(B)}$ Statistical Definition of Probability Mean = Expected Value = $\mu = E(x) = \Sigma P(X).X$ or $\Sigma R_f.X_i$ Probability = $P(X) = P(X_i) = R_f;$ Variable = $X = X_i$ Expected value of x^2 in given by: $E(X_i^2) = \Sigma P(X_i).X_i^2$ Variance = $\sigma^2 = E(x_i - \mu)^2 = E(x_i^2) - \mu^2 = \Sigma P(X_i).X_i^2 - \mu^2$	Find a ⁿ Steps - type a - Press × - Press = (n-1) Find a ⁿ where r integer Steps - type a
Odd in Favour & Odd against Odd in favour = Favourable outcomes : Unfavourable outcomes Odd against = Unfavourable outcomes : Favourable outcomes Total outcomes = Favourable + Unfavourable Conditional Probability $P(B/A) = \frac{P(A \cap B)}{P(A)}; P(A/B) = \frac{P(A \cap B)}{P(B)}$ Statistical Definition of Probability Mean = Expected Value = $\mu = E(x) = \Sigma P(X).X$ or $\Sigma R_f.X_i$ Probability = $P(X) = P(X_i) = R_f;$ Variable = $X = X_i$ Expected value of x^2 in given by: $E(X_i^2) = \Sigma P(X_i).X_i^2$ Variance = $\sigma^2 = E(x_i - \mu)^2 = E(x_i^2) - \mu^2 = \Sigma P(X_i).X_i^2 - \mu^2$ Properties	Find a ⁿ Steps - type a - Press × - Press = (n-1 Find a ⁿ where r integer Steps - type a - Press V 12 times
Odd in Favour & Odd against Odd in Favour & Odd against Odd against = Unfavourable outcomes : Unfavourable outcomes Odd against = Unfavourable outcomes : Favourable outcomes Total outcomes = Favourable + Unfavourable Conditional Probability $P(B/A) = \frac{P(A \cap B)}{P(A)}; P(A/B) = \frac{P(A \cap B)}{P(B)}$ Statistical Definition of Probability Mean = Expected Value = $\mu = E(x) = \Sigma P(X).X \text{ or } \Sigma R_f.X_i$ Probability = $P(X) = P(X_i) = R_f; Variable = X = X_i$ Expected value of x^2 in given by: $E(X_i^2) = \Sigma P(X_i).X_i^2$ Variance = $\sigma^2 = E(x_i - \mu)^2 = E(x_i^2) - \mu^2 = \Sigma P(X_i).X_i^2 - \mu^2$ Properties • $E(x + y) = E(x) + E(y); E(x - y) = E(x) - E(y); E(xy) = E(x) \times E(y)$	Find a ⁿ Steps - type a - Press × - Press = (n-1) Find a ⁿ where r integer Steps - type a - Press √ 12 tin - Minus 1 =
Odd in Favour & Odd against Odd in Favour & Odd against Odd in favour = Favourable outcomes : Unfavourable outcomes Odd against = Unfavourable outcomes : Favourable outcomes Total outcomes = Favourable + Unfavourable Conditional Probability $P(B/A) = \frac{P(A \cap B)}{P(A)}$; $P(A/B) = \frac{P(A \cap B)}{P(B)}$ Statistical Definition of Probability Mean = Expected Value = $\mu = E(x) = \Sigma P(X).X \text{ or } \Sigma R_f.X_i$ Probability = $P(X) = P(X_i) = R_f$; Variable = $X = X_i$ Expected value of x^2 in given by: $E(X_i^2) = \Sigma P(X_i).X_i^2$ Variance = $\sigma^2 = E(x_i - \mu)^2 = E(x_i^2) - \mu^2 = \Sigma P(X_i).X_i^2 - \mu^2$ Properties • $E(x + y) = E(x) + E(y); E(x - y) = E(x) - E(y); E(xy) = E(x) \times E(y)$ • $E(k.x) = k.E(x)$ [Change of scale]	Find a ⁿ Steps - type a - Press × - Press = (n-1) Find a ⁿ where r integer Steps - type a - Press V 12 tin - Minus 1 = - × n = - Add 1 -
Odd in Favour & Odd against Odd in favour = Favourable outcomes : Unfavourable outcomes Odd against = Unfavourable outcomes : Favourable outcomes Total outcomes = Favourable + Unfavourable Conditional Probability $P(B/A) = \frac{P(A \cap B)}{P(A)}$; $P(A/B) = \frac{P(A \cap B)}{P(B)}$ Statistical Definition of Probability Mean = Expected Value = $\mu = E(x) = \Sigma P(X) \cdot X$ or $\Sigma R_f \cdot X_i$ Probability = $P(X) = P(X_i) = R_f$; Variable = $X = X_i$ Expected value of x^2 in given by: $E(X_i^2) = \Sigma P(X_i) \cdot X_i^2$ Variance = $\sigma^2 = E(x_i - \mu)^2 = E(x_i^2) - \mu^2 = \Sigma P(X_i) \cdot X_i^2 - \mu^2$ Properties • $E(x + y) = E(x) + E(y)$; $E(x - y) = E(x) - E(y)$; $E(xy) = E(x) \cdot x E(y)$ • $E(k.x) = k \cdot E(x)$ [Change of scale] • Variance of a constant k is V(k) = 0	Find a ⁿ Steps - type a - Press × - Press = (n-1) Find a ⁿ where r integer Steps - type a - Press V 12 tin - Minus 1 = - × n = - Add 1 = - Press × 12 tin - Press × 12 tin
Odd in Favour & Odd against Odd in favour = Favourable outcomes : Unfavourable outcomes Odd against = Unfavourable outcomes : Favourable outcomes Total outcomes = Favourable + Unfavourable Conditional Probability $P(B/A) = \frac{P(A \cap B)}{P(A)}; P(A/B) = \frac{P(A \cap B)}{P(B)}$ Statistical Definition of Probability Mean = Expected Value = $\mu = E(x) = \Sigma P(X).X \text{ or } \Sigma R_f.X_i$ Probability = $P(X) = P(X_i) = R_f; Variable = X = X_i$ Expected value of x^2 in given by: $E(X_i^2) = \Sigma P(X_i).X_i^2$ Variance = $\sigma^2 = E(x_i - \mu)^2 = E(x_i^2) - \mu^2 = \Sigma P(X_i).X_i^2 - \mu^2$ Properties • $E(x + y) = E(x) + E(y); E(x - y) = E(x) - E(y); E(xy) = E(x) x E(y)$ • $E(k.x) = k.E(x)$ [Change of scale] • Variance of a constant k is V(k) = 0	Find a ⁿ Steps - type a - Press × - Press = $(n-1)^{n-1}$ Find a ⁿ where r integer Steps - type a - Press $\sqrt{12}$ tin - Minus 1 = - × n = - Add 1 = - Press ×= 12 tin

• $P(A-B) = P(A) - P(A \cap B)$ [Probability of only A]

here b = byxPoint Form: $y - \overline{y} = b_{yx}(x)$ Properties of Regression \circ Coefficient of Regression \circ Relationship betw \circ r, byx, bxy all 3 beat	$\frac{x}{2} = \overline{x}$ on gression rem ANGES due f gin \rightarrow No Ch cale \rightarrow Char buv = bvu = veen r, b _{YX} , b r ² = ars the same	$x - \frac{1}{2}$ hains UNCH to change of hange in Regrine by $\frac{M_x}{M_y}$ = $b_{XY} \cdot \frac{M_y}{M_x}$ by (Most Im by $x \cdot b_{XY}$ e sign.	here b = b_{XY} Point Form: $\overline{x} = b_{Xy}(y - \overline{y})$ IANGED due to change of SCALE. gression Coefficient ession Coefficient	 Fisher We Us Methods of All methods Just interch Value Index two periods Note: It is u
• Both regression li their MEANS. i.e.				
Find a ⁿ	Find 1/(a ⁿ)		Find a ^{1/n}	Test of Ade
Steps	Steps		Steps	There are fo
- type a	- type a		- type a	Unit T
- Press ×	- Press÷		 Press √ 12 times 	formu
- Press = (n-1) times	- Press =	(n times)	- Minus 1 =	Time
			- ÷ n =	Paasc
			- Auu I – - Press x= 12 times	Factor
Find a ⁿ where n is non	Find Scrap y	alue in	Find log	satisfi
integer	depreciatio	n ques.	Ŭ	Circul
Steps	Steps		Steps	or Paa
- type a	- (1-Dep %)	- Enter number	mean
 Press V 12 times Minus 1 – 	- Press ×	t of	 Press V 13 times Minus 1 	Tixed
- x n =	- Type cos machine		- willius 1 - x 3558	Othor imp
- Add 1 =	- Press = (r	n times)	× 3330	other imp.
 Press ×= 12 times 	(,	,		CPI, CII, RPI
				Real Wages

OR

 $\sigma_x \sigma_y$

|2c - n|

+ bx & v = c + dy

 $r_{xy} = \frac{b \times d}{|b| \times |d|} \cdot r_{xy}$

eighted average of price/quantity relative Using AM \rightarrow P₀₁ = $\frac{\Sigma WP}{\Sigma W}$ where P = $\frac{P_1}{P_0} \times 100$ Using GM \rightarrow P₀₁ = $AL \left[\frac{\Sigma W \log P}{\Sigma W} \right]$ where P = $\frac{P_1}{P_0} \times 100$ f constructing Index Numbers (Quantity Index Q₀₁) s and formulas are same to determine Q₀₁ nange p with q and q with p. x Numbers (V₀₁) numbers shows the movement in value levels between Value = Price x Quantity used for computing growth rate in the economy. Value Index $\rightarrow V_{01} = \frac{\Sigma p_1 q_1}{\Sigma p_0 q_0} \times 100$ $V_{01} = \frac{OR}{\frac{\Sigma V_1}{\Sigma V_0}} \times 100$ Here, $V_1 = \Sigma p_1 q_1 \& V_0 = \Sigma p_0 q_0$ equacy our tests of adequacy: **Fest** - Except for the simple average method all other ulae satisfy this test reversal test - $P_{01} \times P_{10} = 1 - Laspeyre's$ method and che's method do not satisfy this test **r Reversal test** - $P_{01} \times Q_{01} = V_{01}$ - Only Fisher's Index ies Factor Reversal test lar test - $P_{01} \times P_{12} \times P_{20} = 1$ - This test is not met by Laspeyres, asche's or the Fisher's ideal index. The simple geometric of price relatives and the weighted average method with weights meet this test. This test is extension of Time sal Test. Formulas-Consumer Price Index (CPI), $=\frac{\Sigma p_1 q_0}{1} \times 100,$ Cost of Living Index (CII), $= \frac{\sum p_0 q_0}{\sum p_0 q_0} \times 100,$ $= \frac{\text{Money wages}}{2} \times 100$ Real Price Index (RPI) CII